

# End-to-end optimized image compression

**Johannes Ballé**

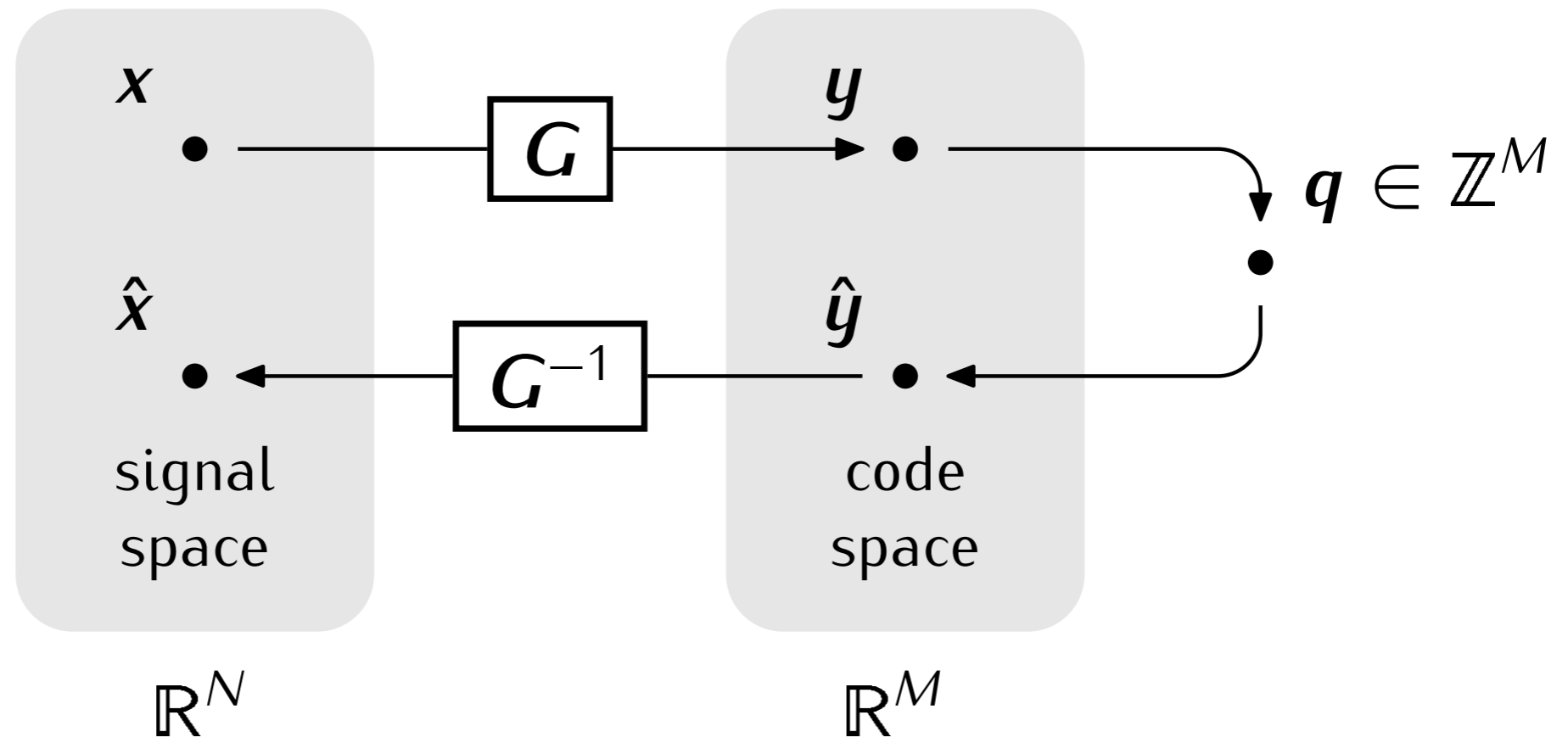
Center for Neural Science, NYU  
Howard Hughes Medical Institute  
(now with Google Inc.)

*joint work with:*

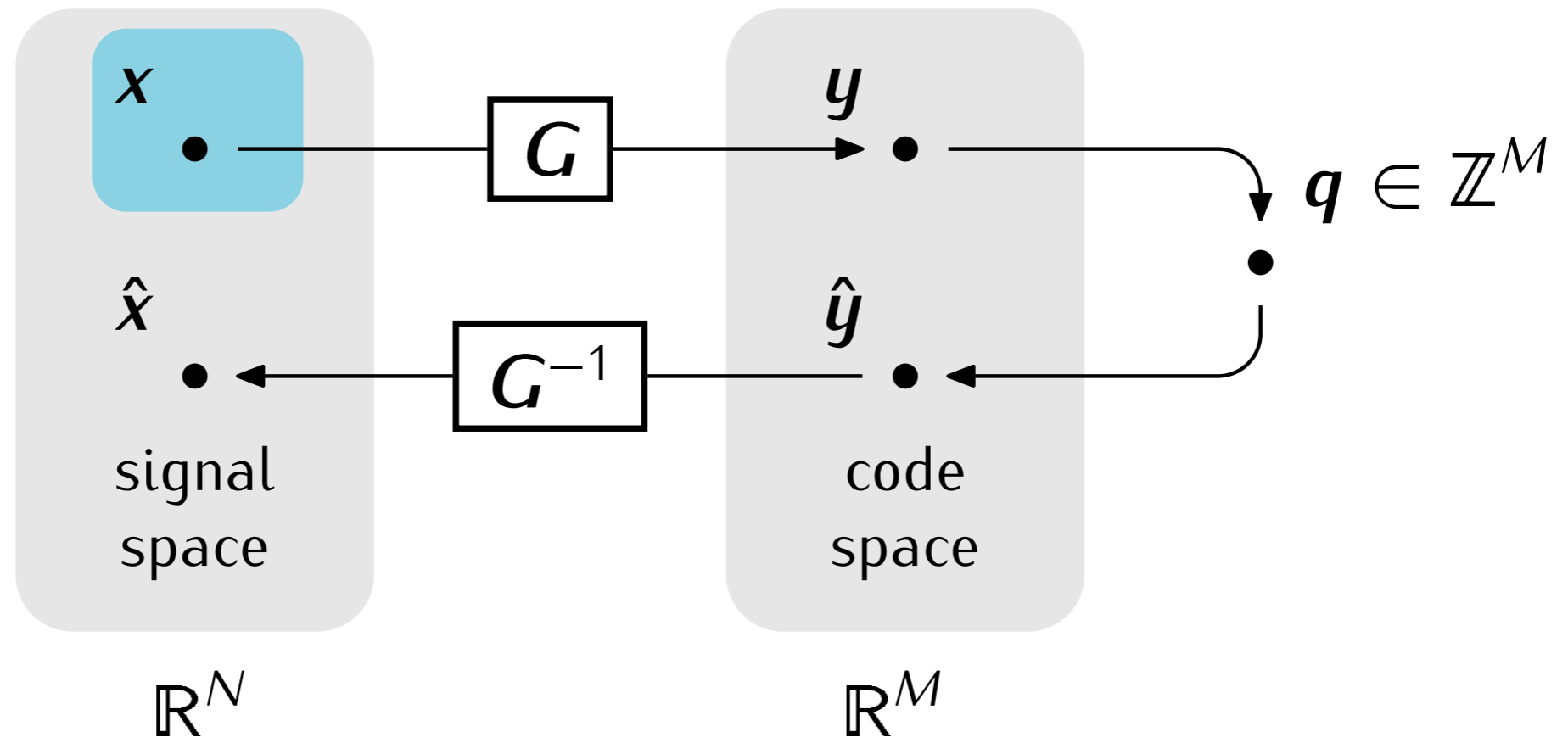
**Valero Laparra**, Universitat de València  
**Eero P. Simoncelli**, CNS/Courant Institute/HHMI



# Linear transform coding

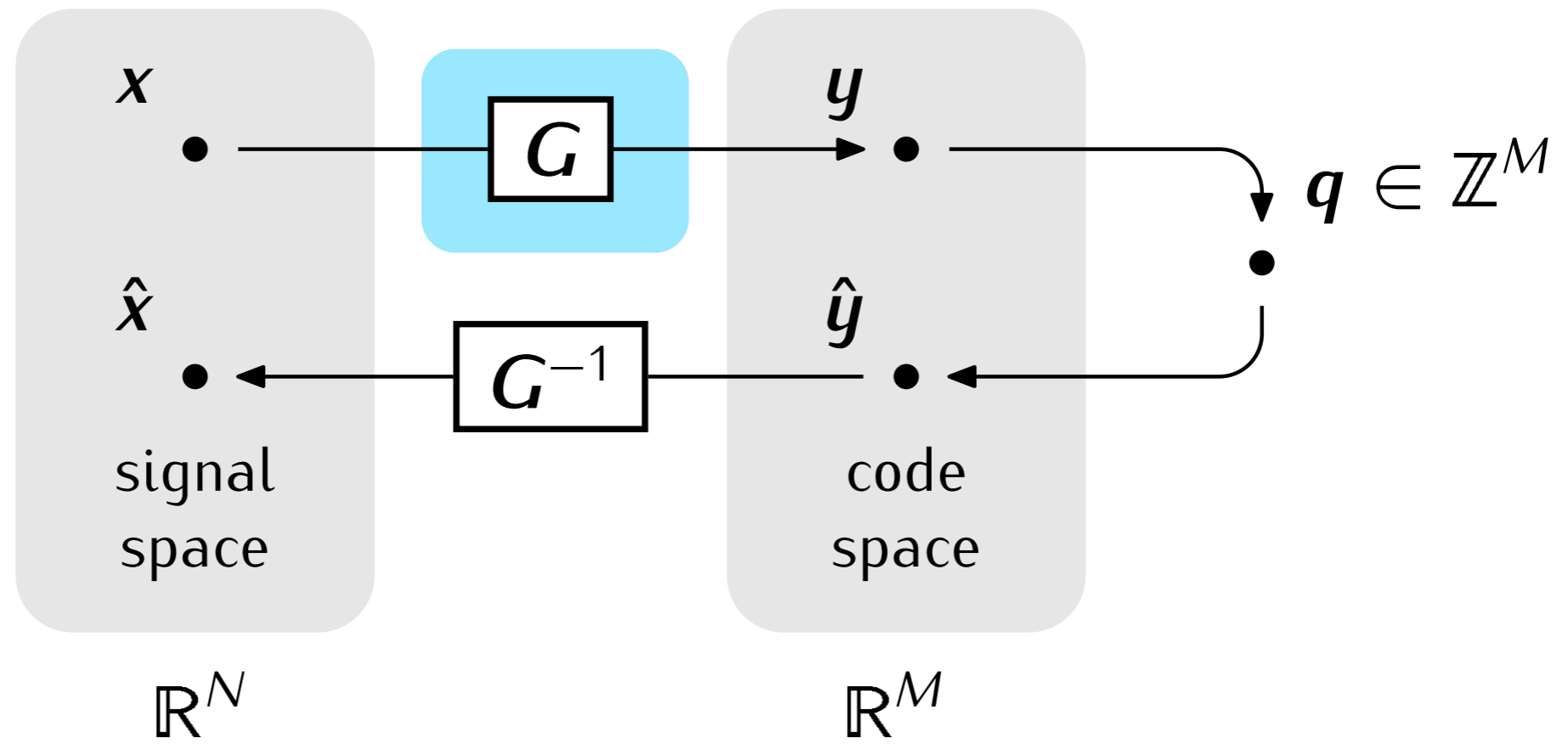


# Linear transform coding

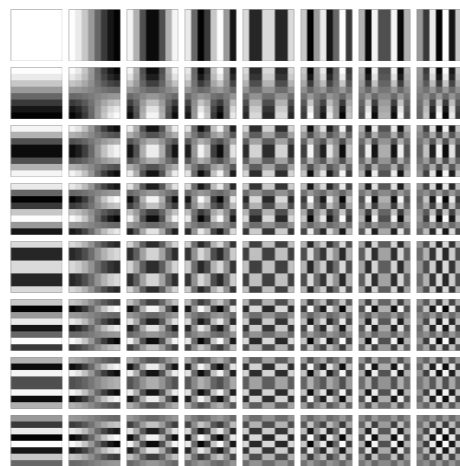


$x$

# Linear transform coding

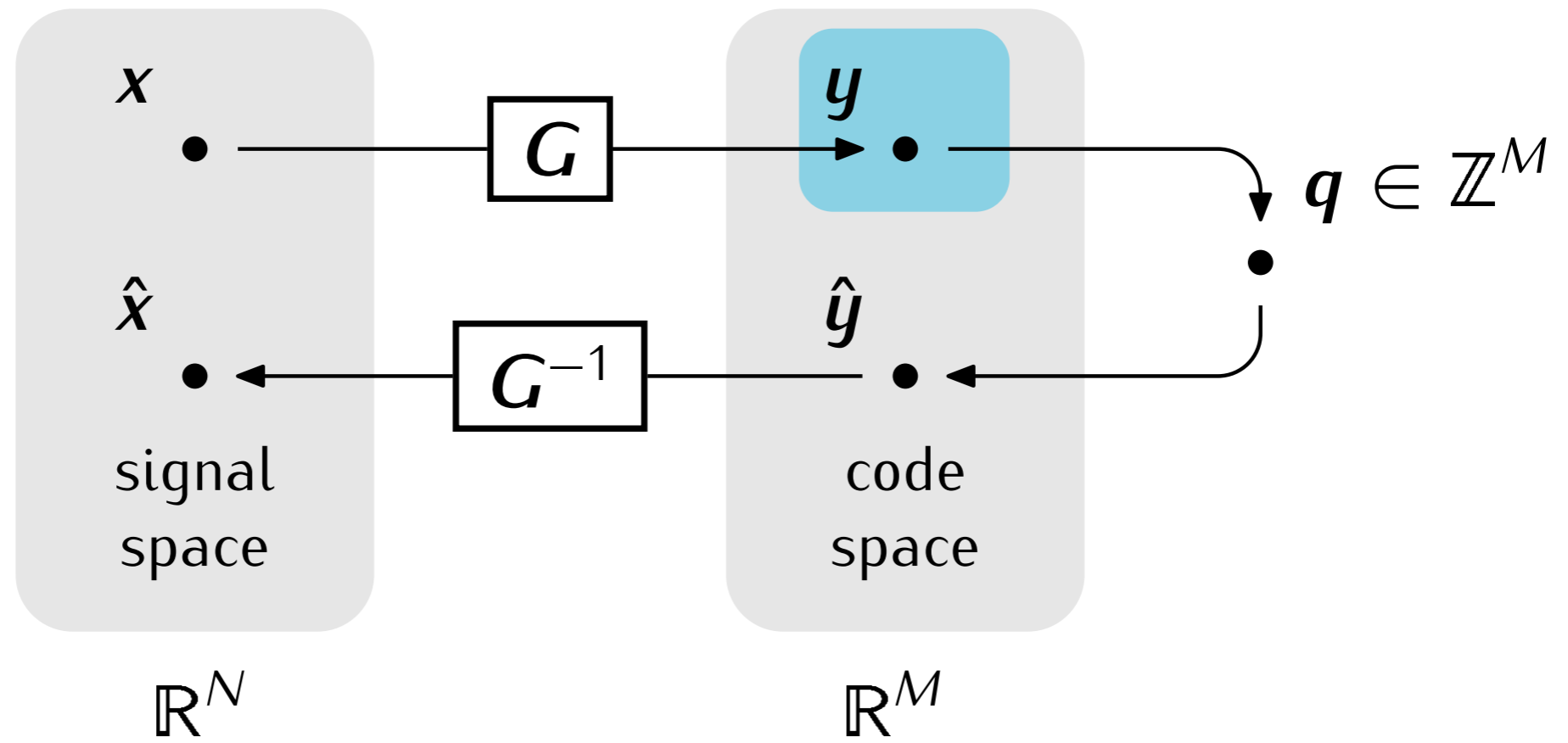


$x$

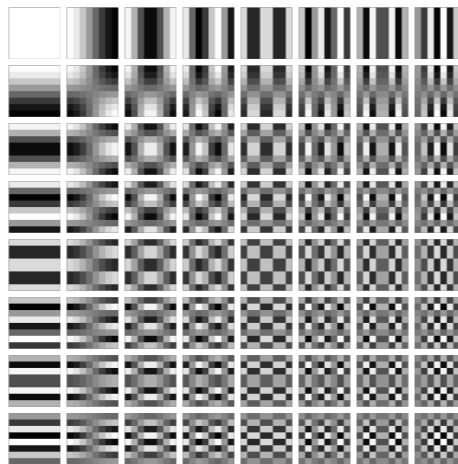


$G$

# Linear transform coding

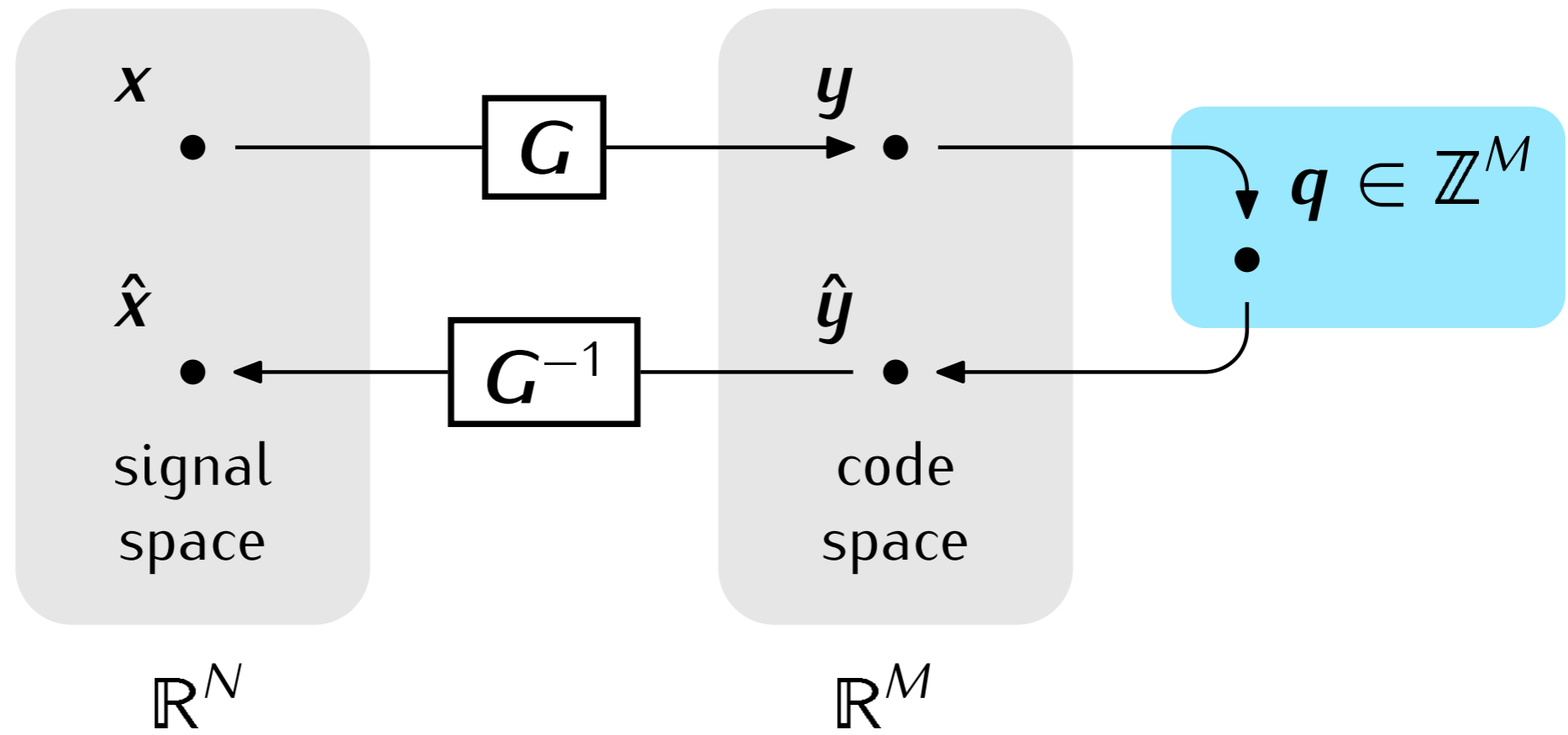


$x$

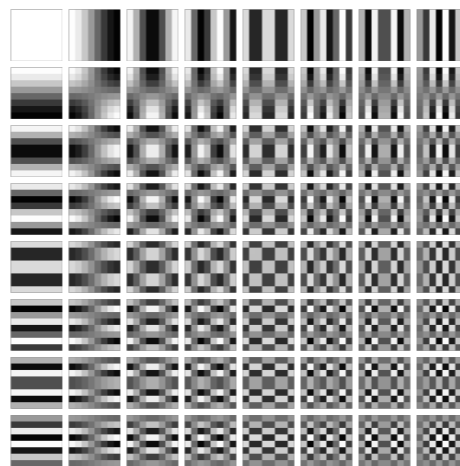


$G$

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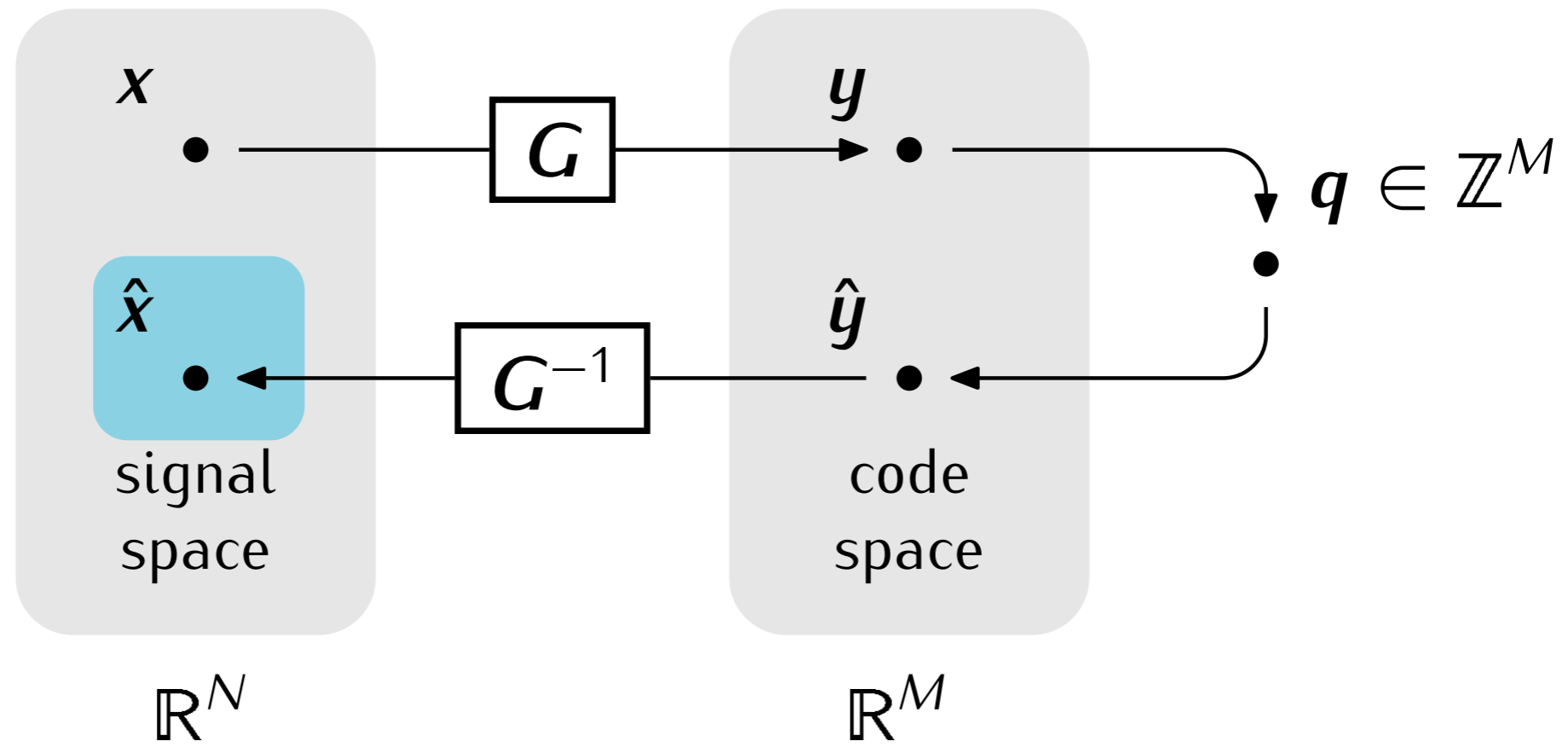


$x$

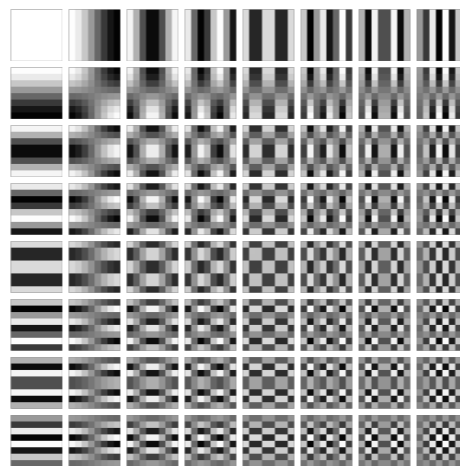


$G$

# Linear transform coding



$x$



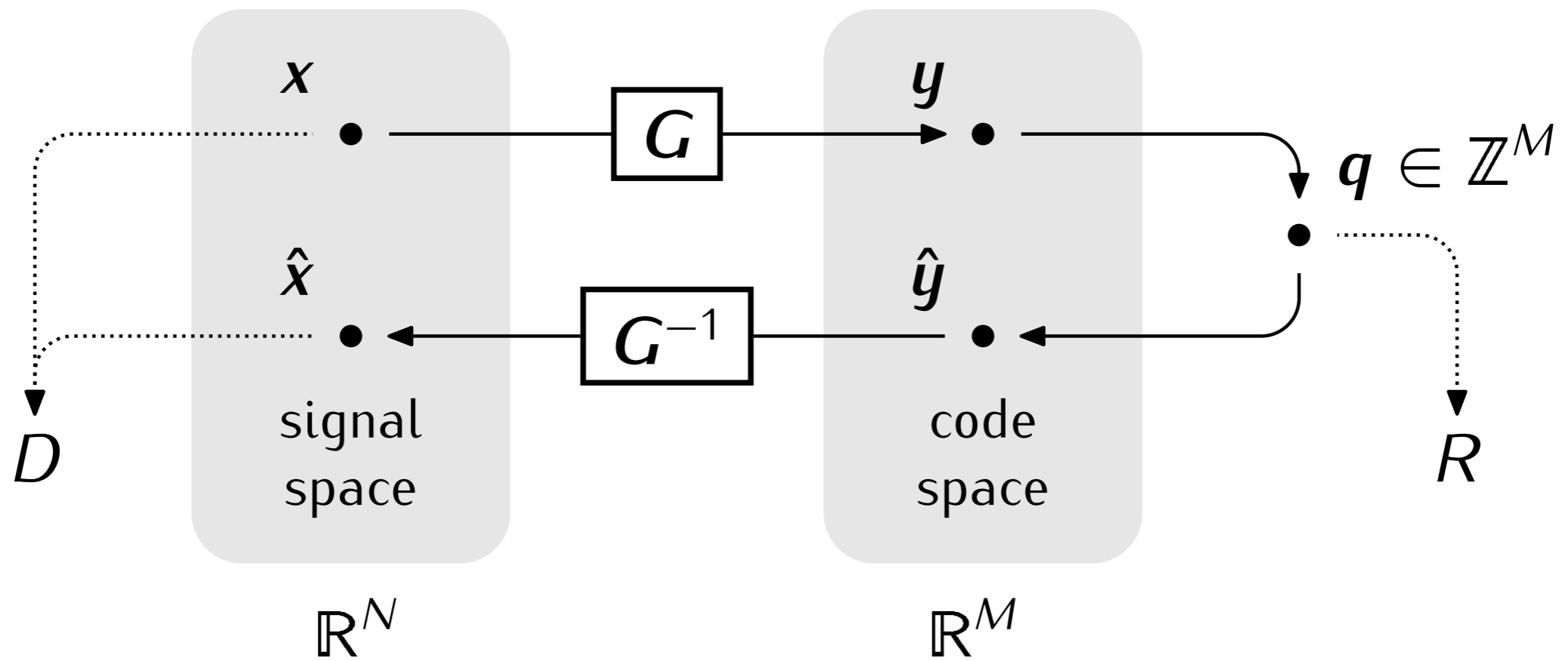
$G$



$\hat{x}$



# Linear transform coding



$D$ : distortion, e.g. mean squared error

$R$ : rate, ideally close to Shannon entropy of  $q$

rate: 0.17 bits/pixel



rate: 0.12 bits/pixel



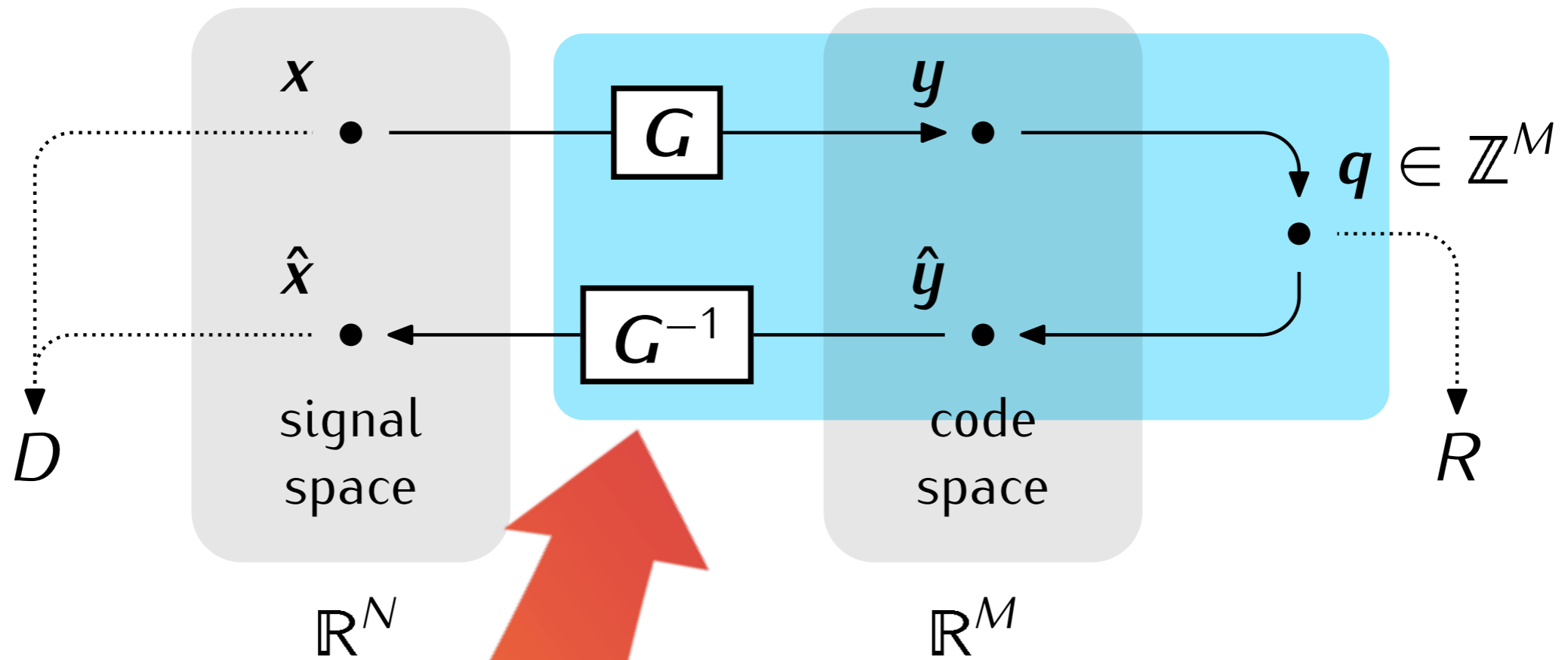
coarser quantization: lower rate, higher distortion

rate: 0.32 bits/pixel



finer quantization: higher rate, lower distortion

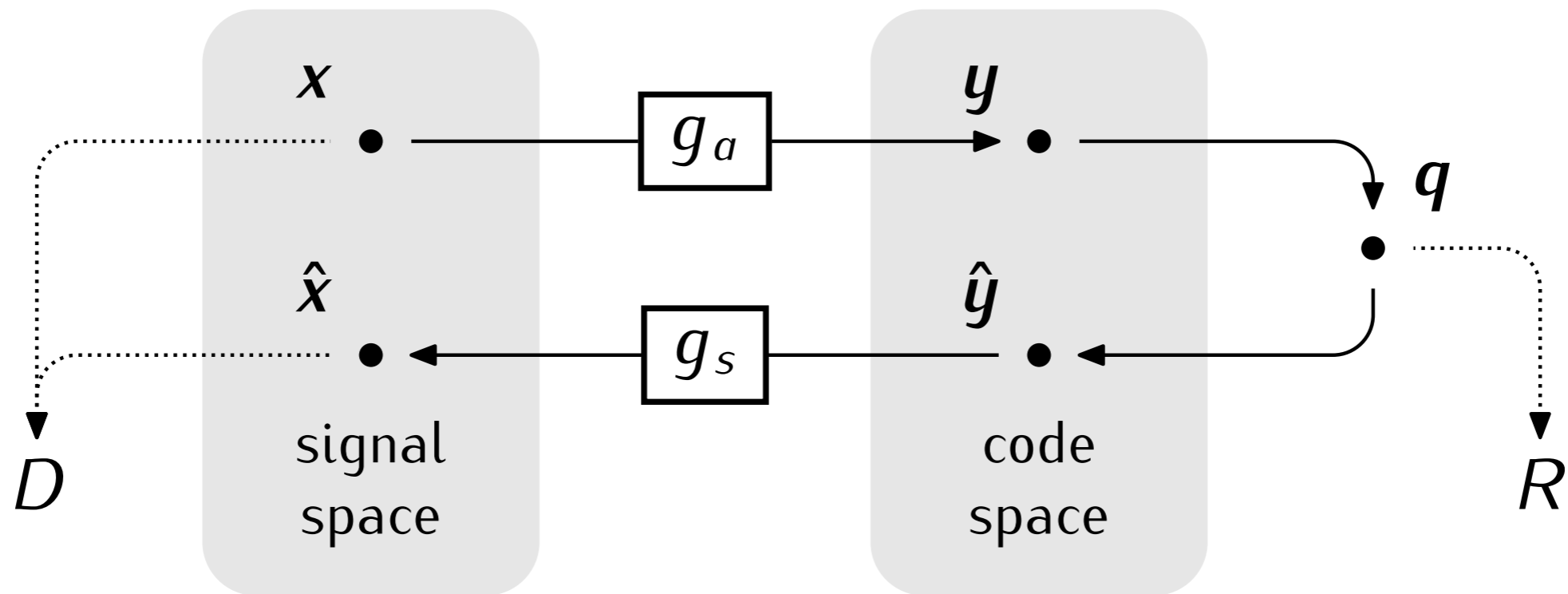
# Linear transform coding



decades of engineering:

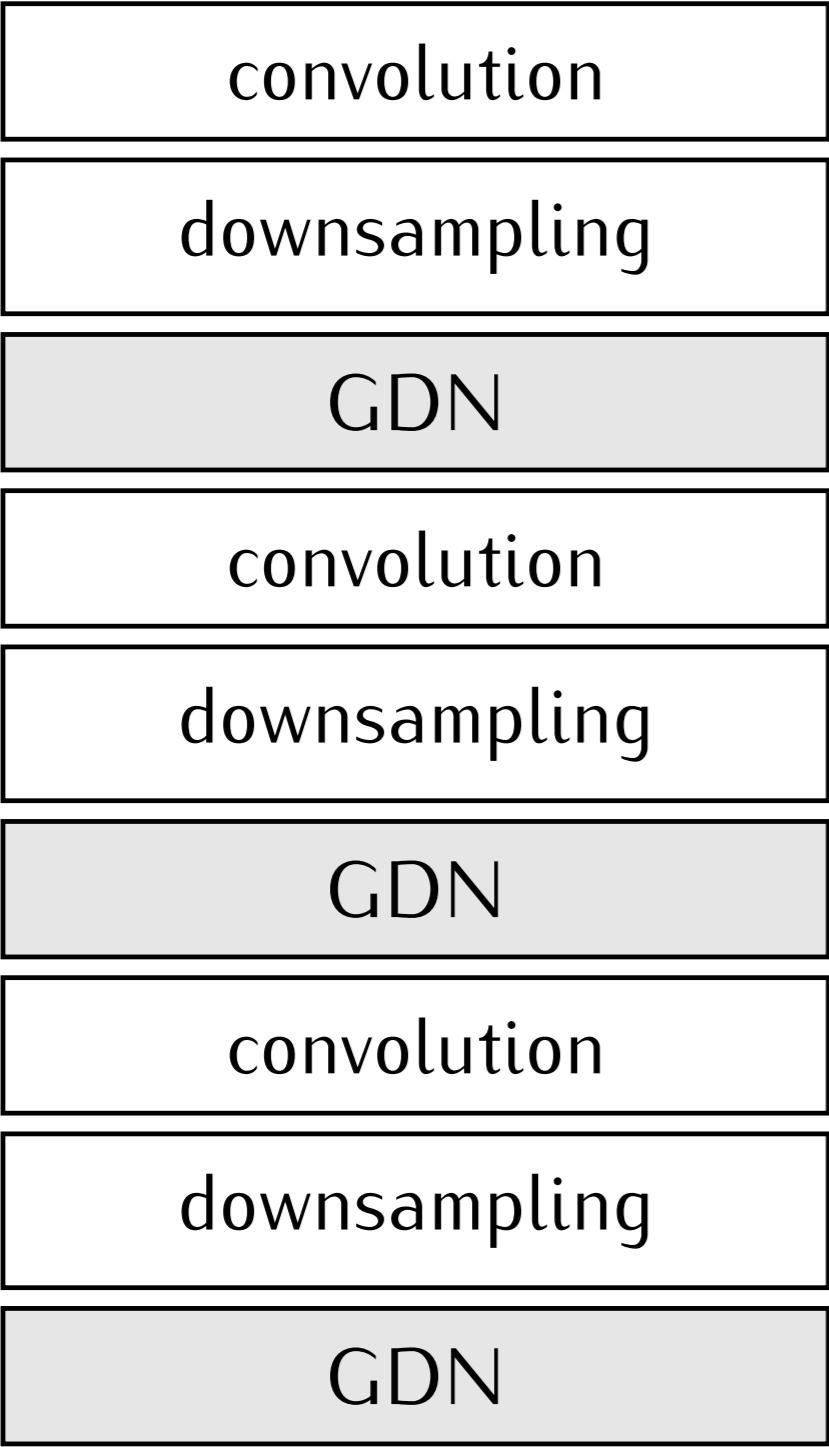
improved transforms, non-uniform quantization, inter/intra prediction, deblocking, adaptive partitioning, etc.

# Nonlinear transform coding



$g_a, g_s$ : multivariate, parametric nonlinear functions  
(if it helps, think of them as neural networks)

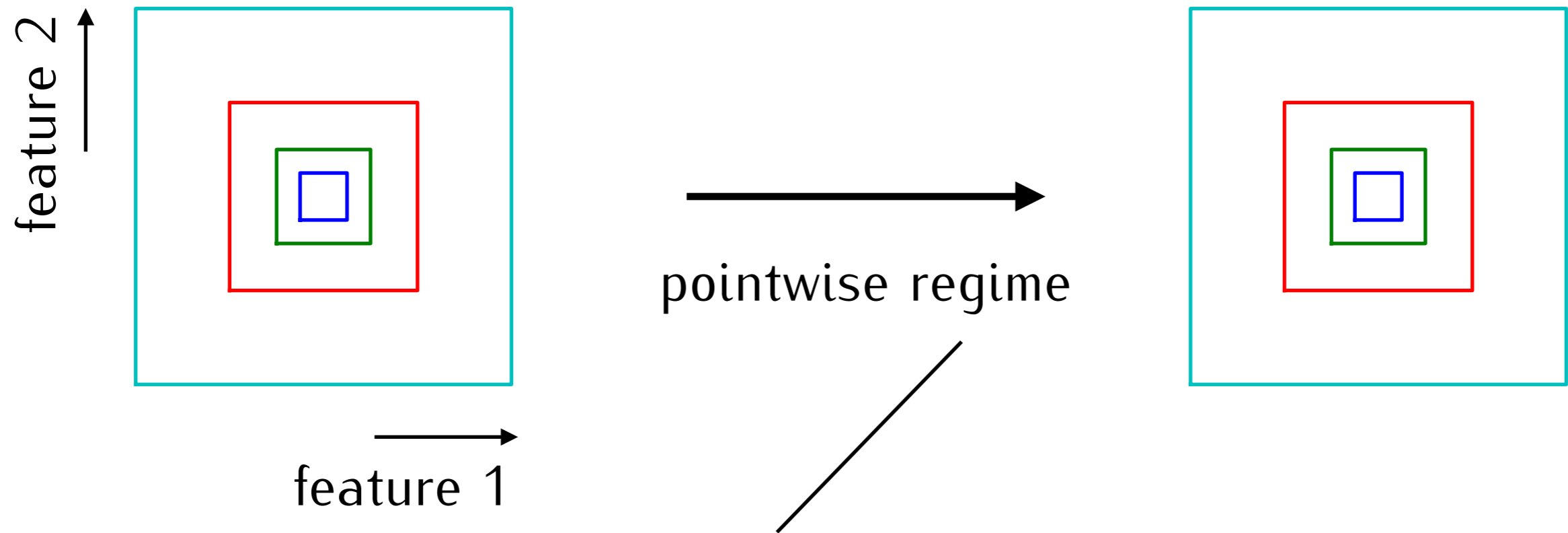
# Architecture of transformation



generalized divisive normalization

$$u_i = \frac{w_i}{\sqrt{\beta_i + \sum_j \gamma_{ij} |w_j|^2}}$$

# Generalized divisive normalization (GDN)

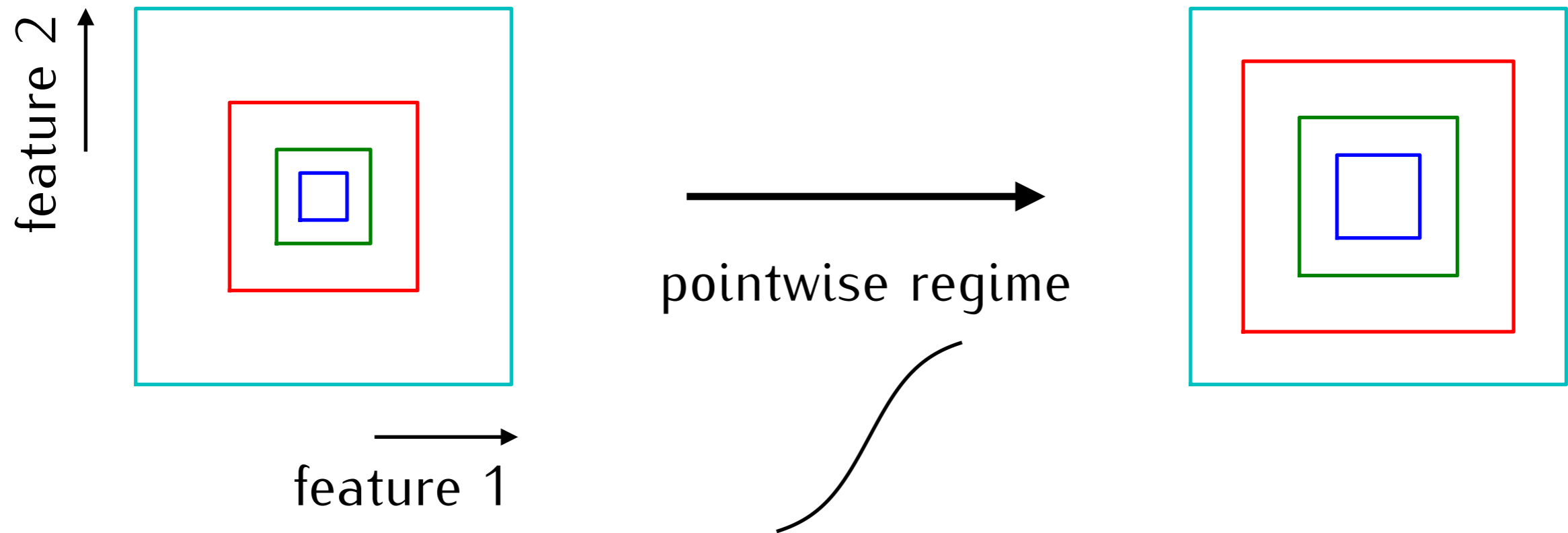


generalization of:

- sigmoid-type nonlinearities
  - local response normalization (LRN)
- see our ICLR 2016 paper for details



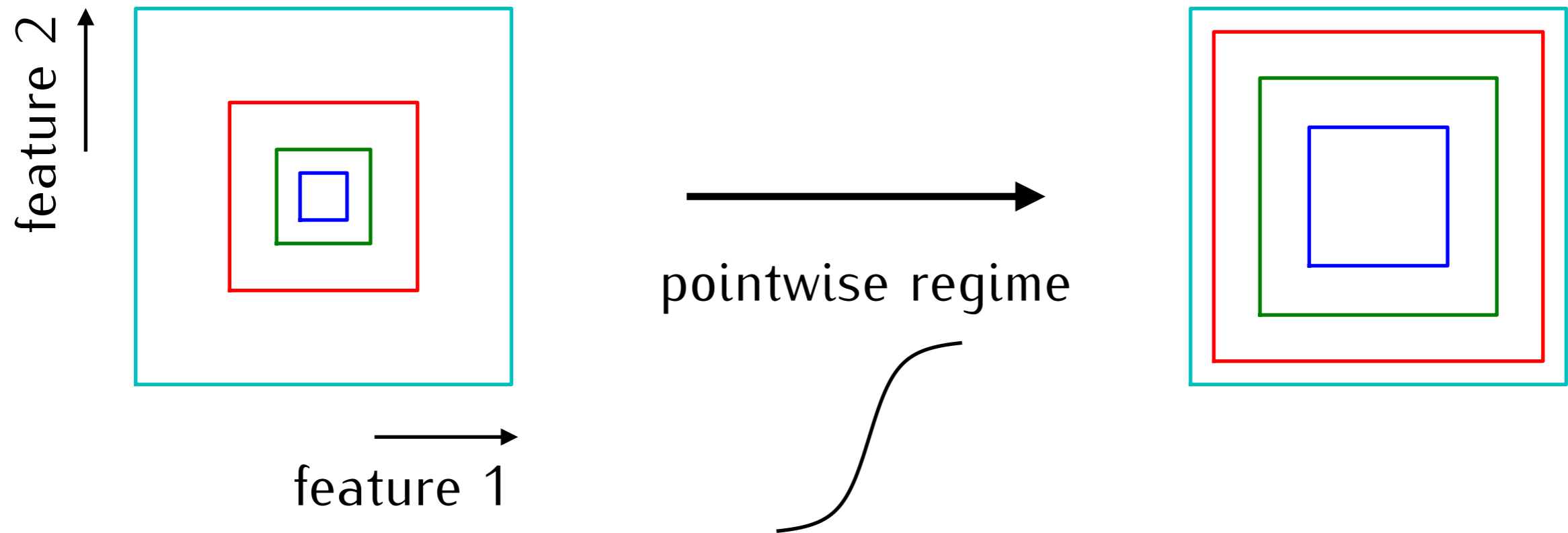
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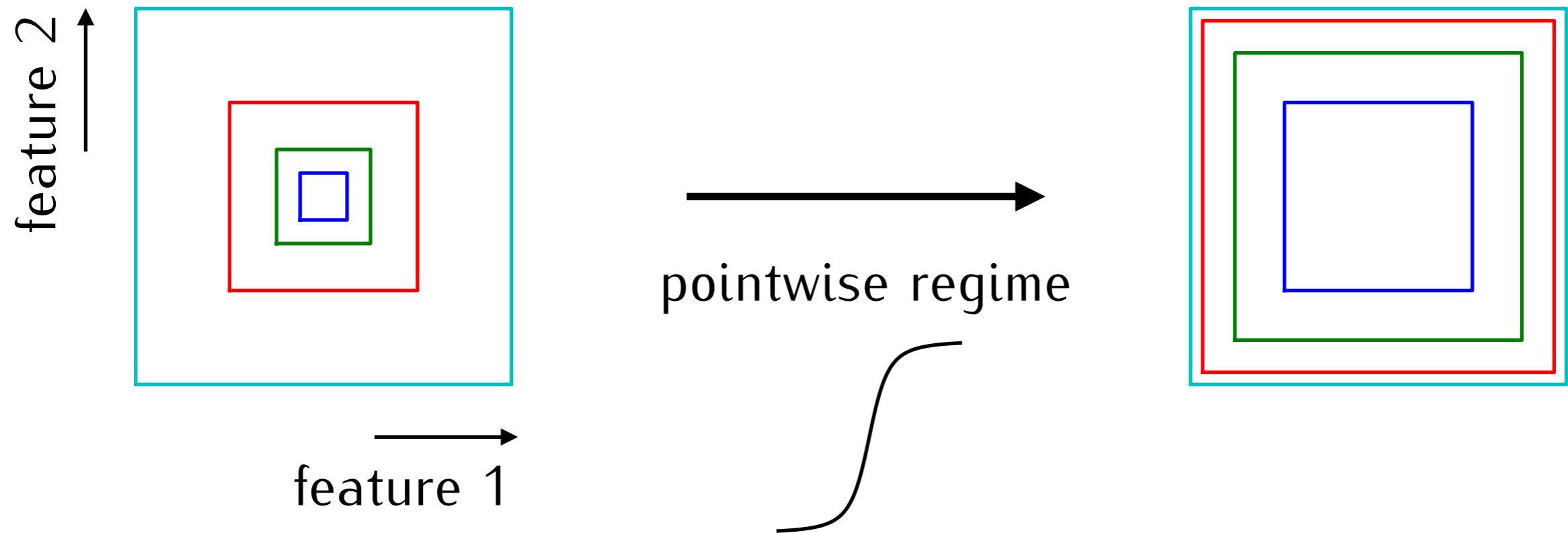
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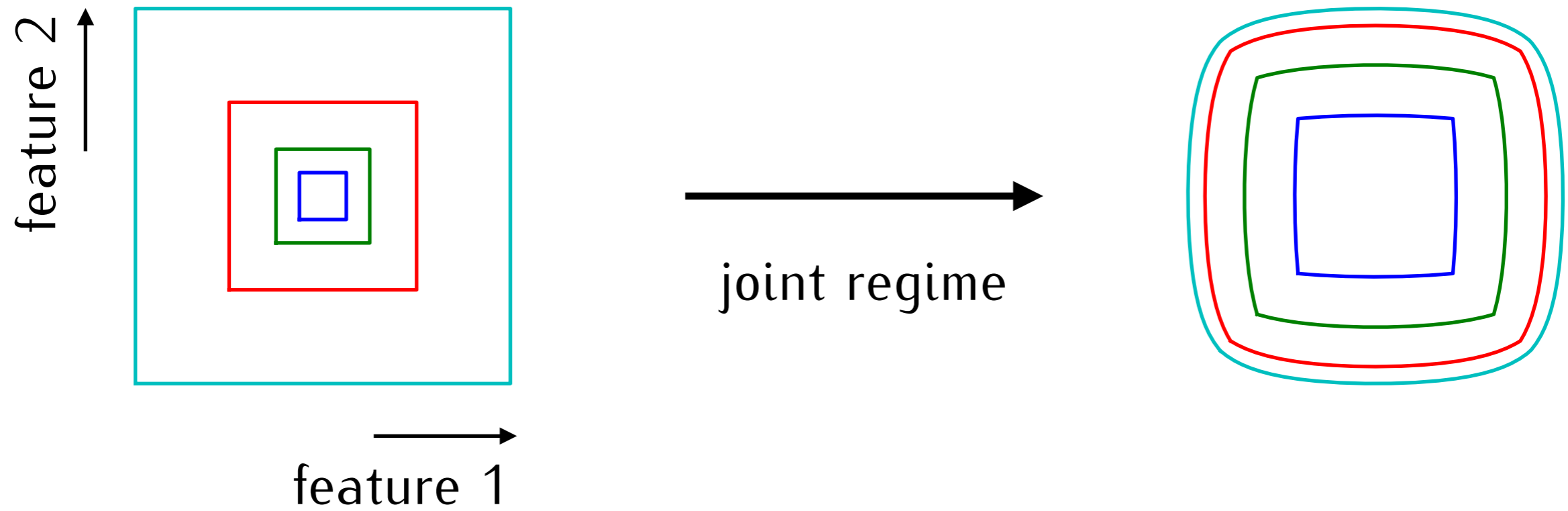
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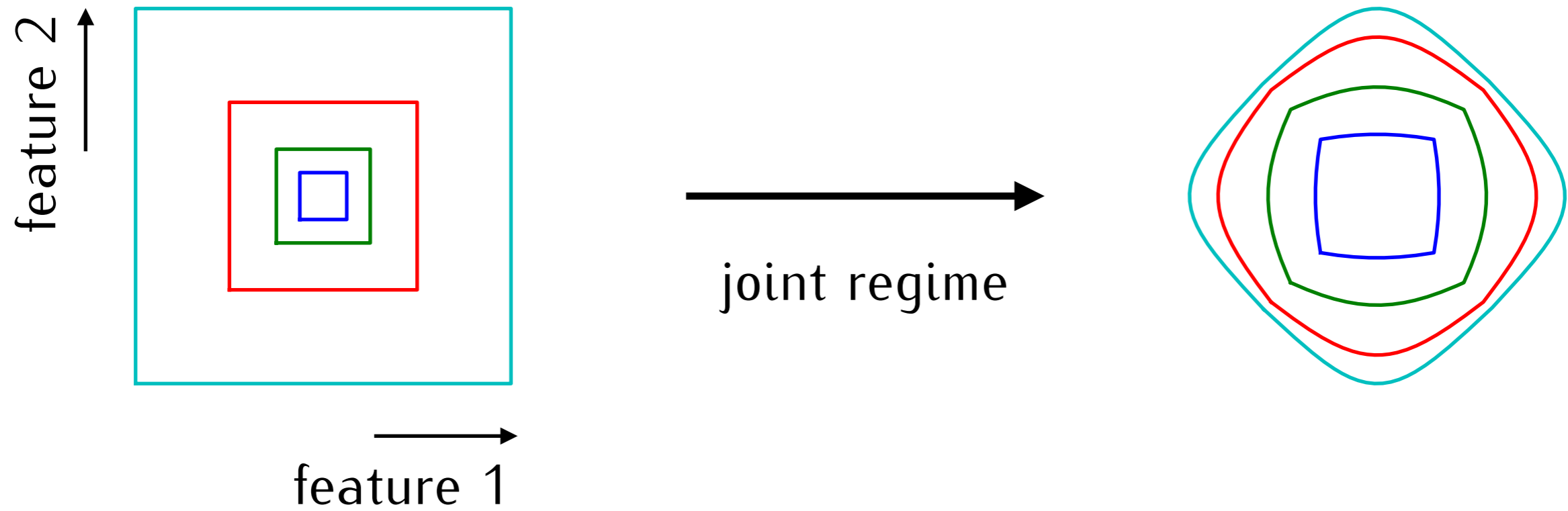
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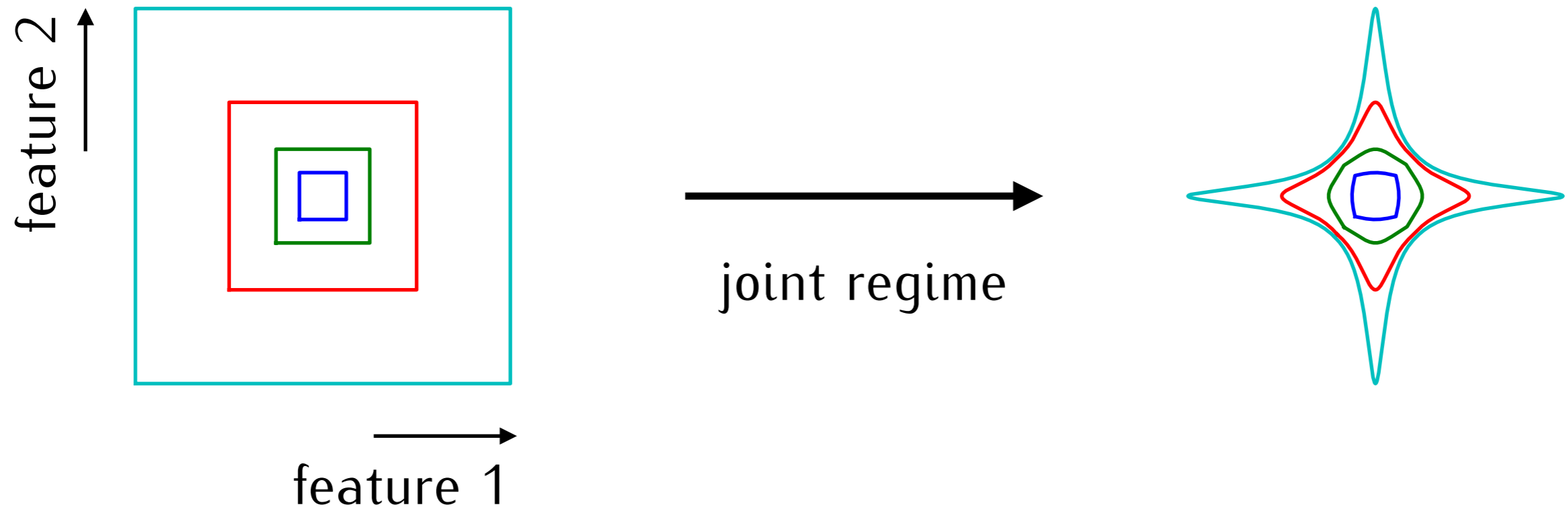
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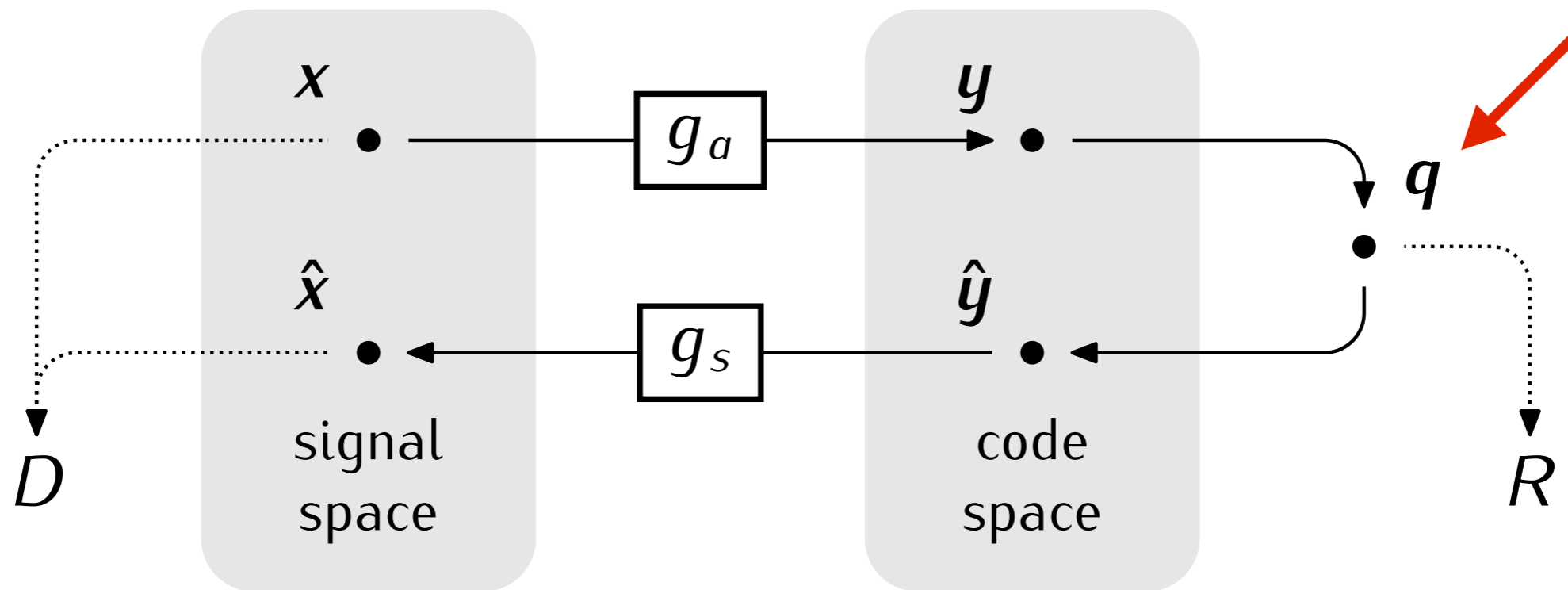
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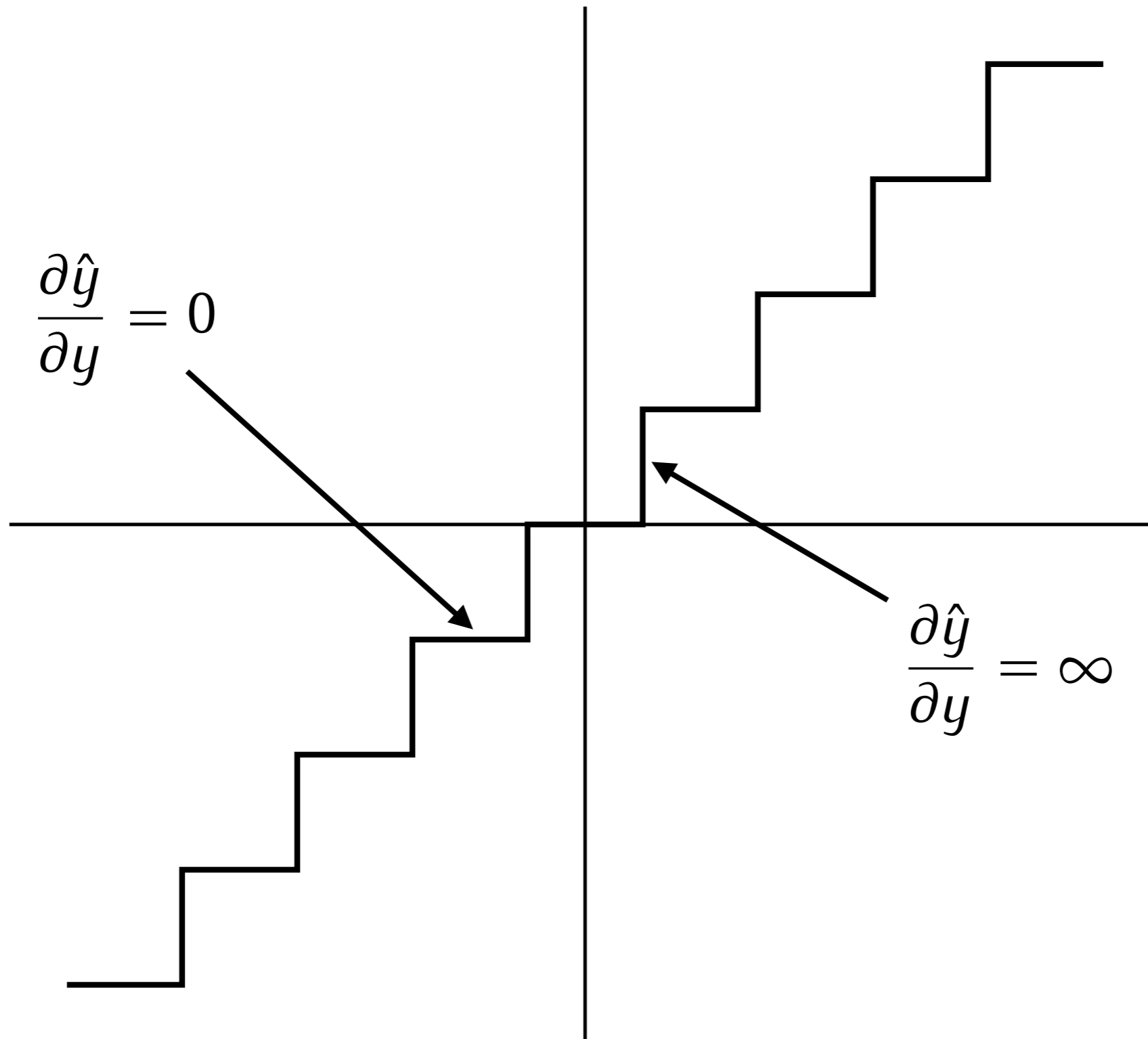
# Nonlinear transform coding



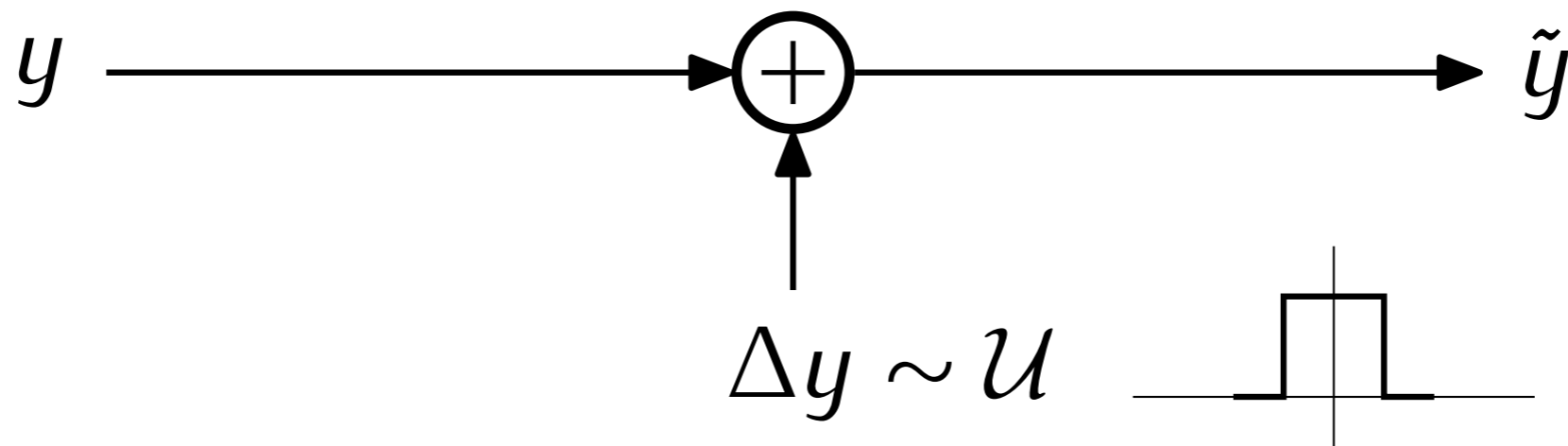
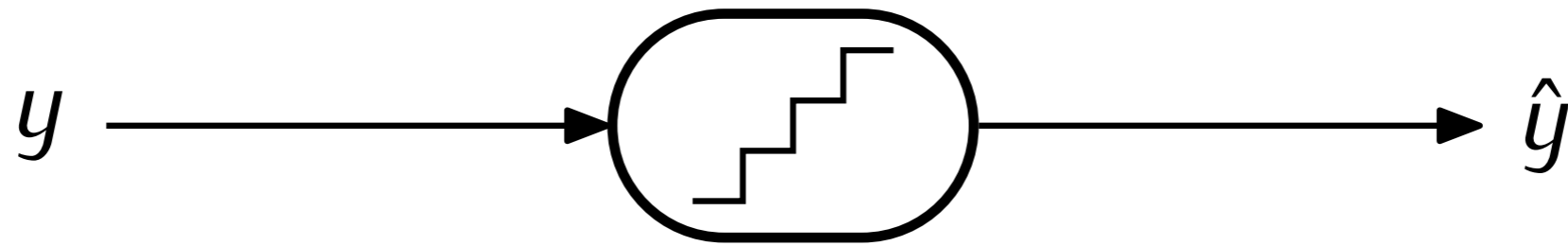
optimize  $g_a, g_s$  for rate and distortion numerically

$$L[g_a, g_s, P_q] = \underbrace{-\mathbb{E}[\log_2 P_q]}_R + \lambda \underbrace{\mathbb{E}[d(x, \hat{x})]}_D$$

gradient is zero *almost everywhere*







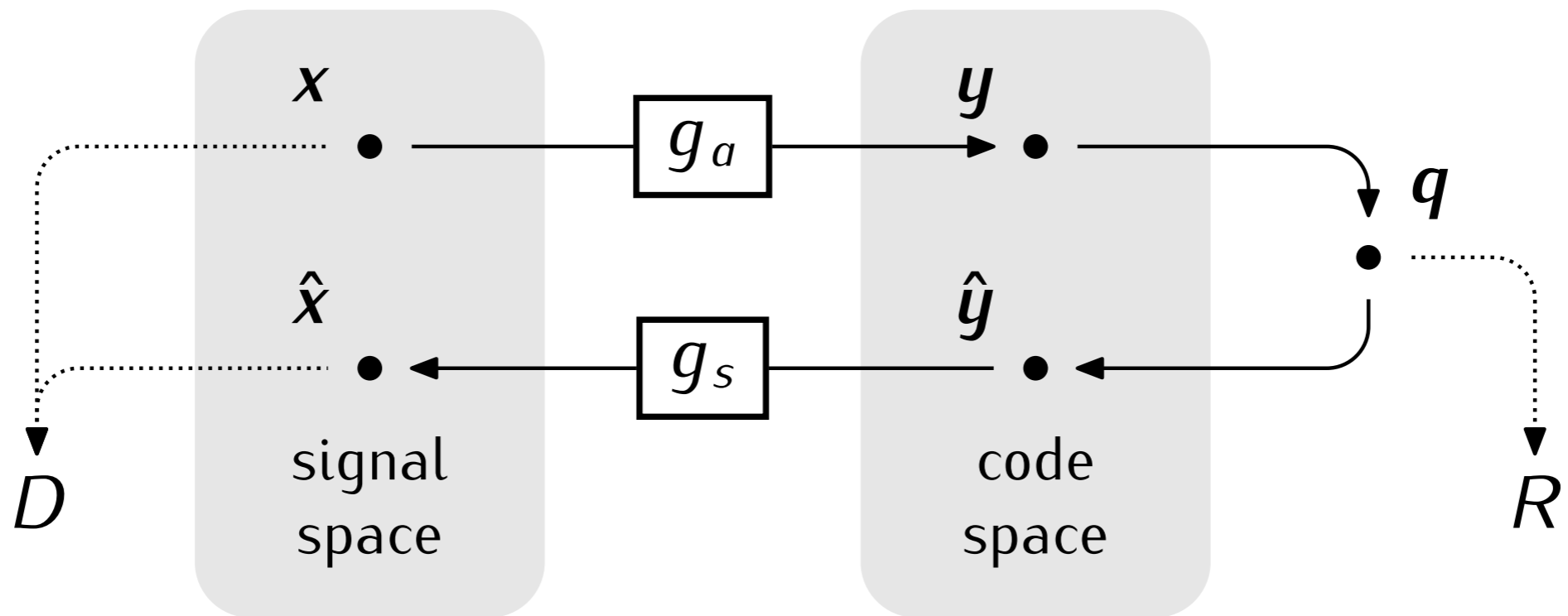
differentiable and continuous  
stochastic approximation

other approaches:

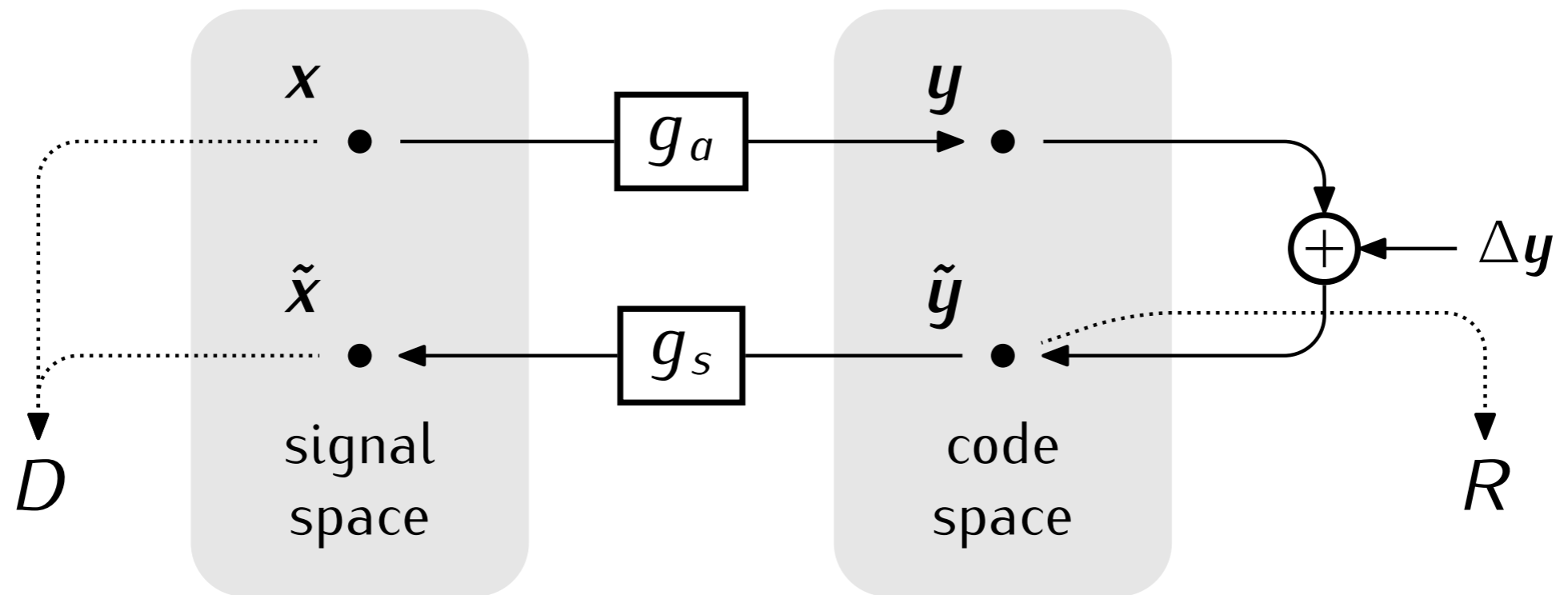
Theis et al., 2017

Jang et al., 2017

Maddison et al., 2017



$$L = \mathbb{E} \left[ - \sum_i \log_2 P_{q_i}(q_i) + \lambda \|\hat{\mathbf{x}} - \mathbf{x}\|_2^2 \right]$$



proxy loss:

$$L = \mathbb{E} \left[ - \sum_i \log_2 p_{\tilde{\mathbf{y}}_i}(\tilde{\mathbf{y}}_i) + \lambda \|\tilde{\mathbf{x}} - \mathbf{x}\|_2^2 \right]$$

**Wait! Isn't this just an autoencoder?**

(Yes and no.)

Proxy RD:

rate

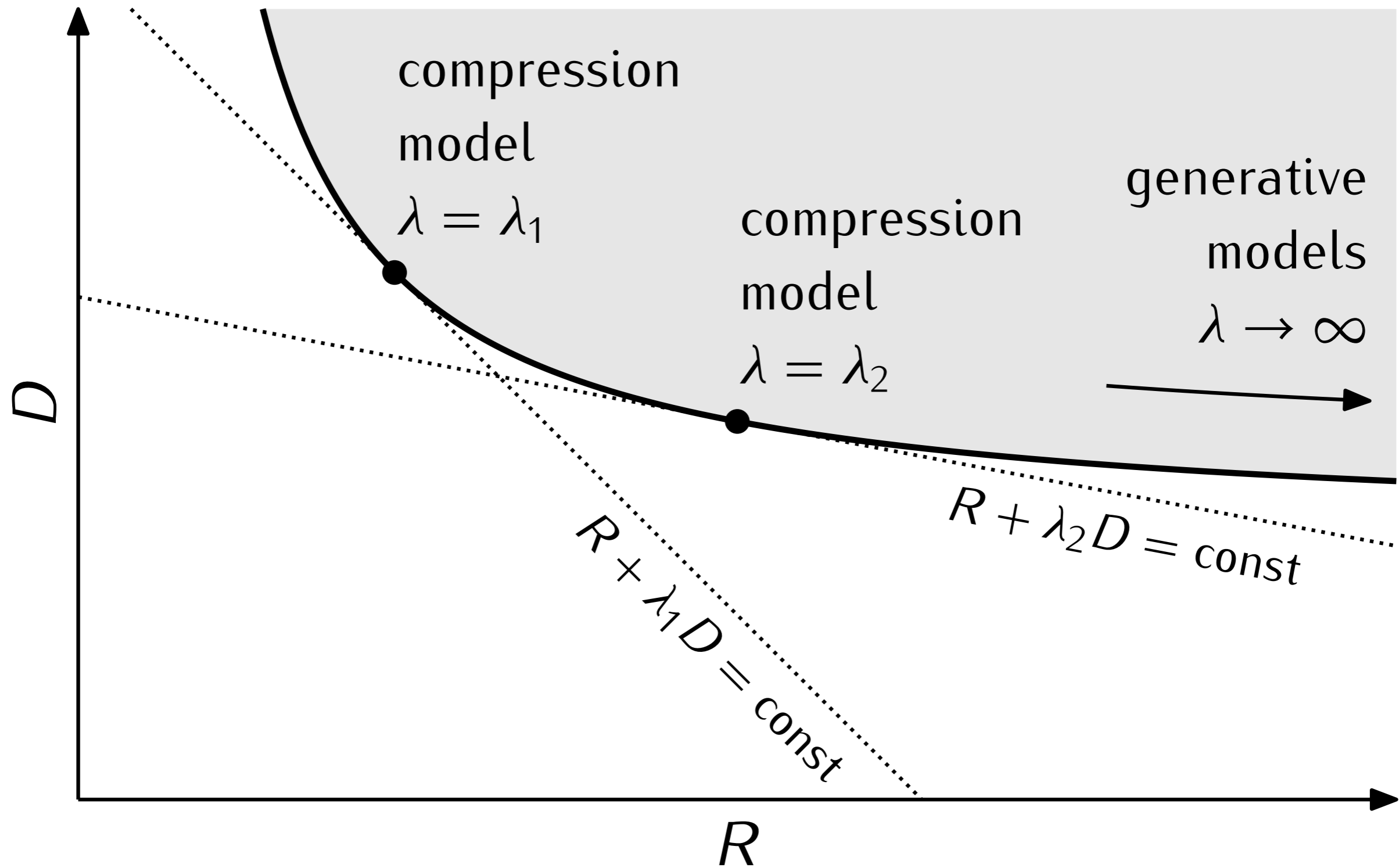
distortion

$$L = \mathbb{E} \left[ - \sum_i \log_2 p_{\tilde{y}_i}(\tilde{y}_i) + \lambda \|\tilde{\mathbf{x}} - \mathbf{x}\|_2^2 \right]$$

Variational AE:

log prior

log likelihood



# Results

original





JPEG @ 0.119 bits/px



JPEG 2000 @ 0.107 bits/px



proposed @ 0.106 bits/px





original



proposed

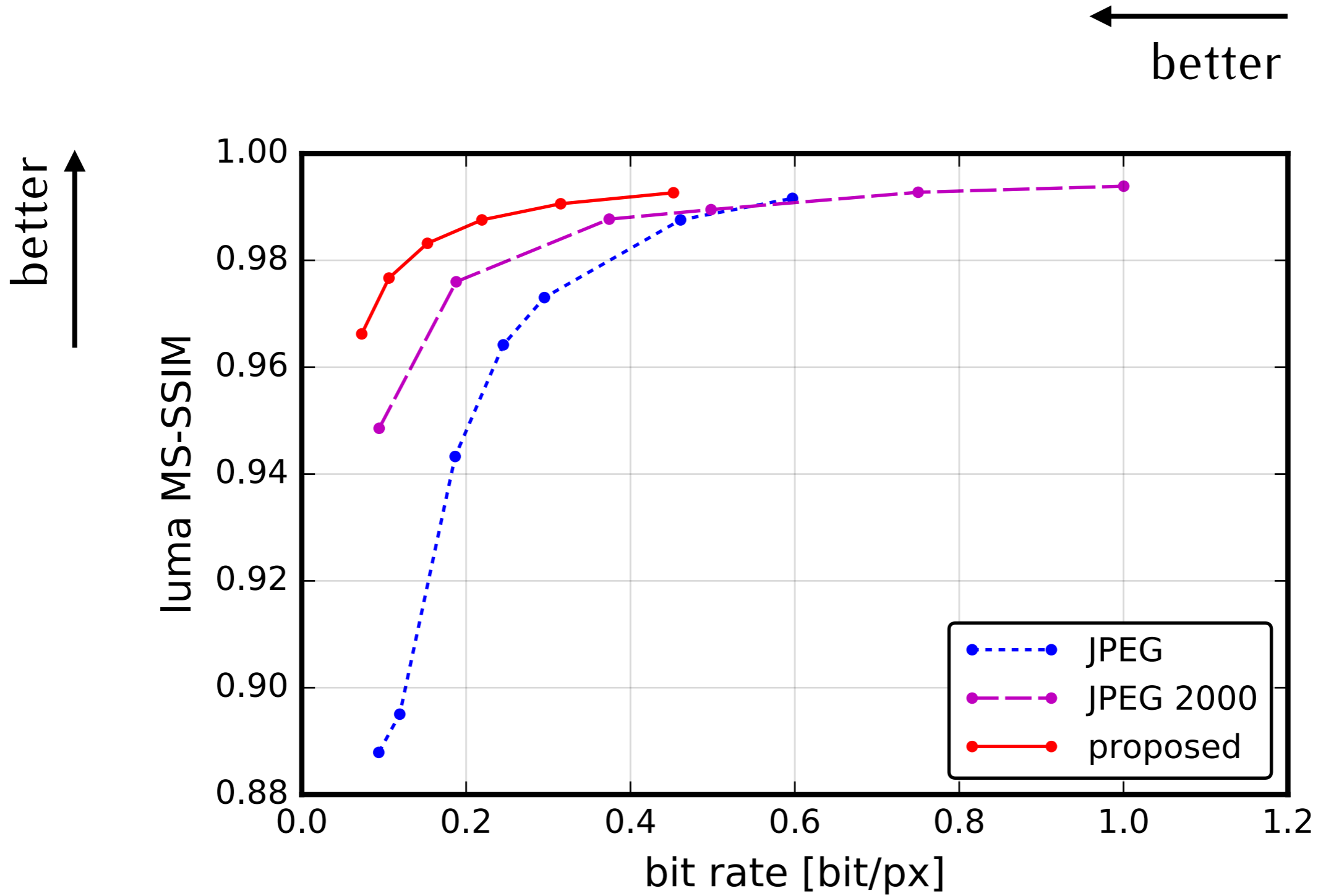


JPEG



JPEG 2000

# We consistently outperform JPEG 2000





original





JPEG @ 0.170 bits/px



JPEG 2000 @ 0.167 bits/px





proposed @ 0.167 bits/px



original



proposed



JPEG



JPEG 2000

Thanks!



More images, metrics, and the model parameters:  
<http://www.cns.nyu.edu/~lcv/iclr2017/>

Comparison to compression state-of-the-art (BPG):  
come to our poster tomorrow morning!