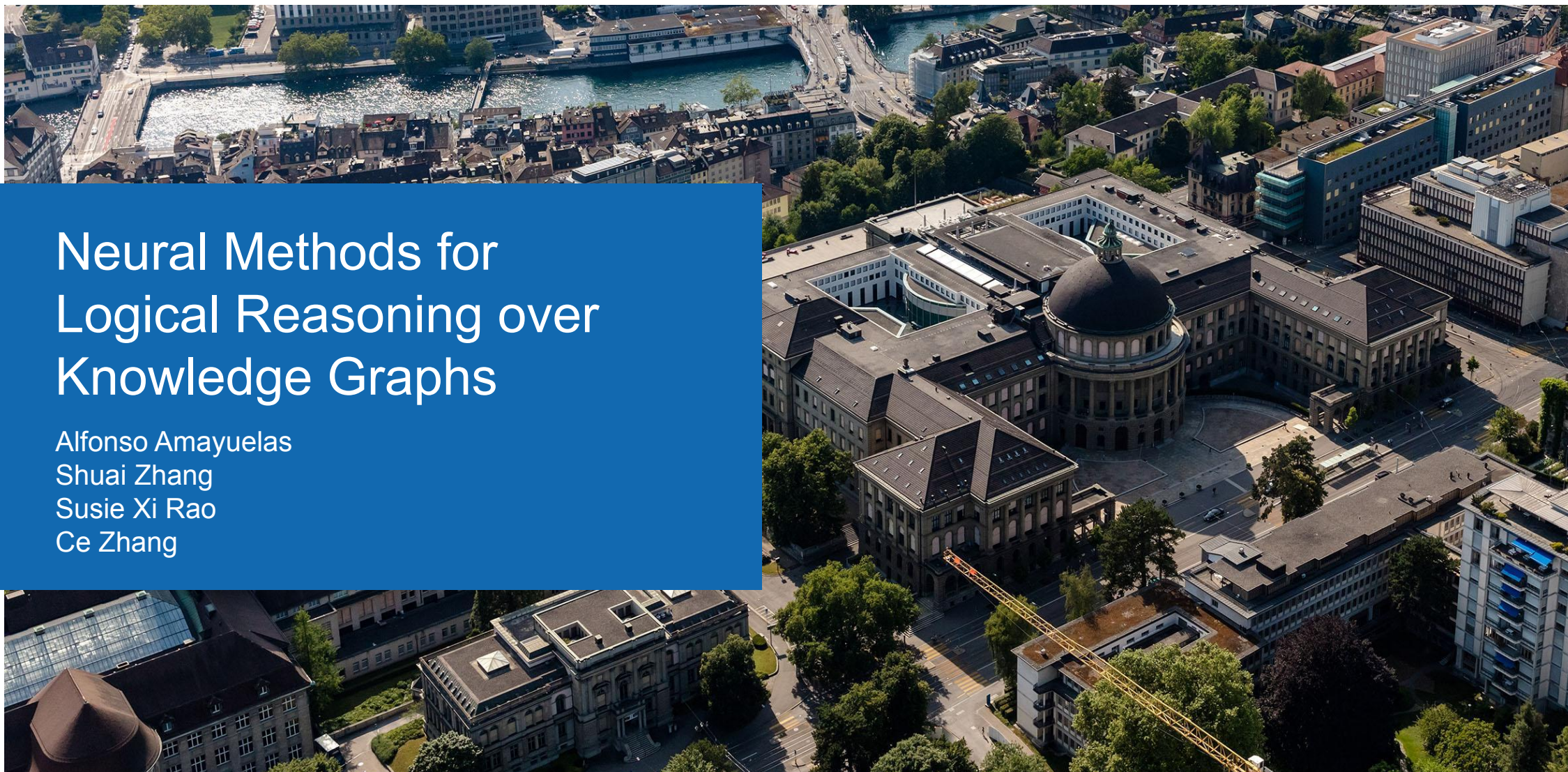
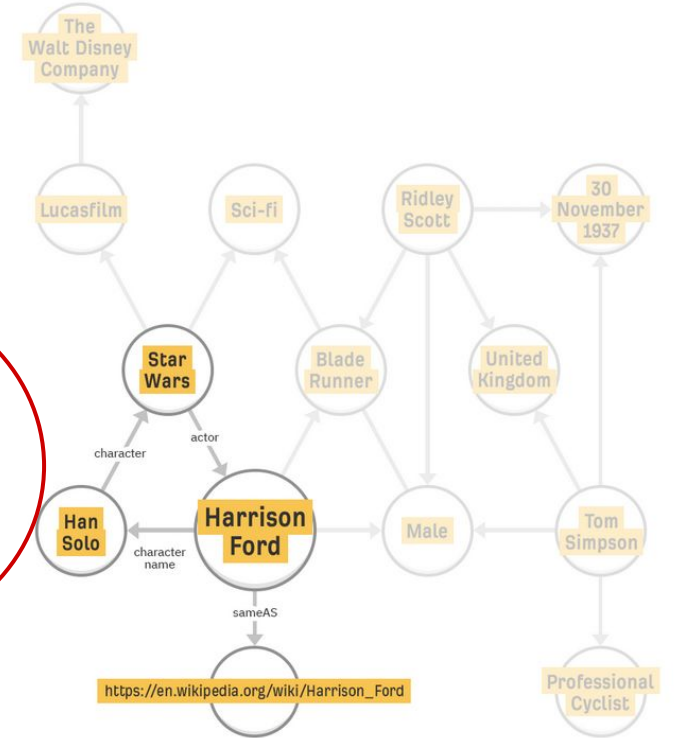
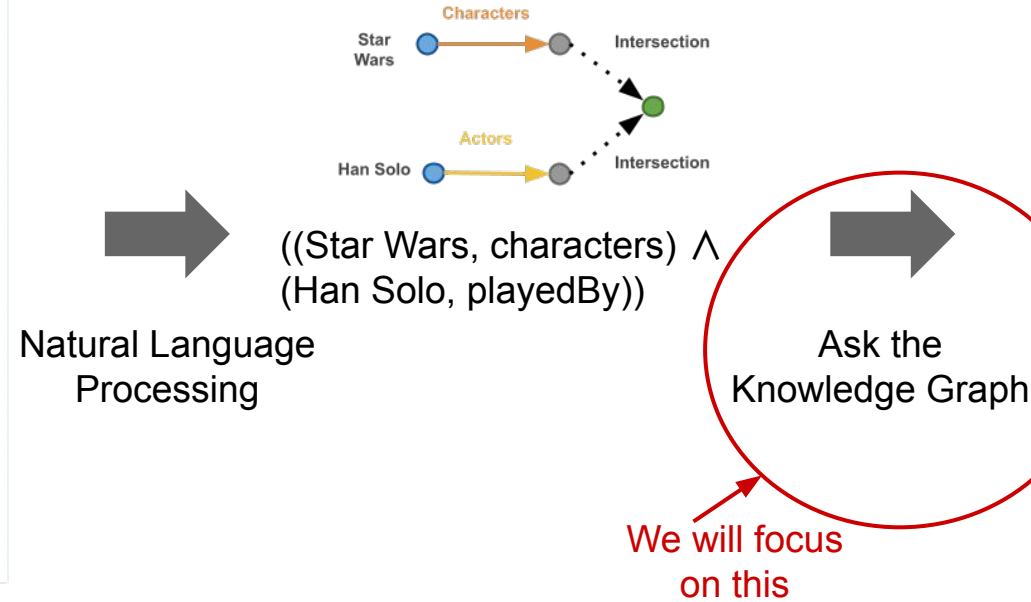
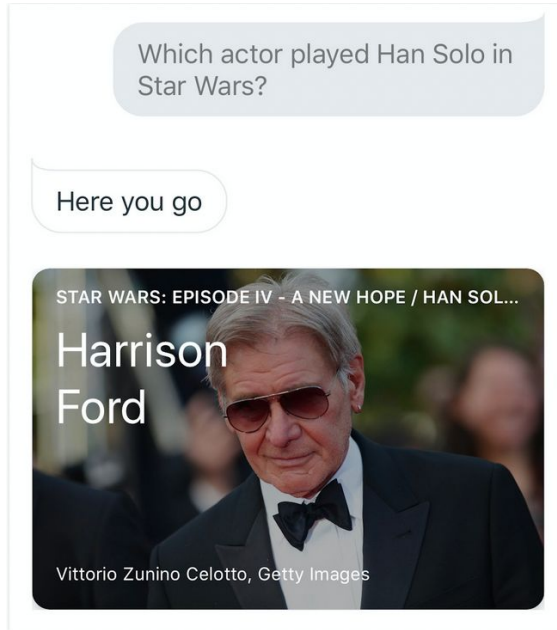


Neural Methods for Logical Reasoning over Knowledge Graphs

Alfonso Amayuelas
Shuai Zhang
Susie Xi Rao
Ce Zhang



But users want to ask more complex queries



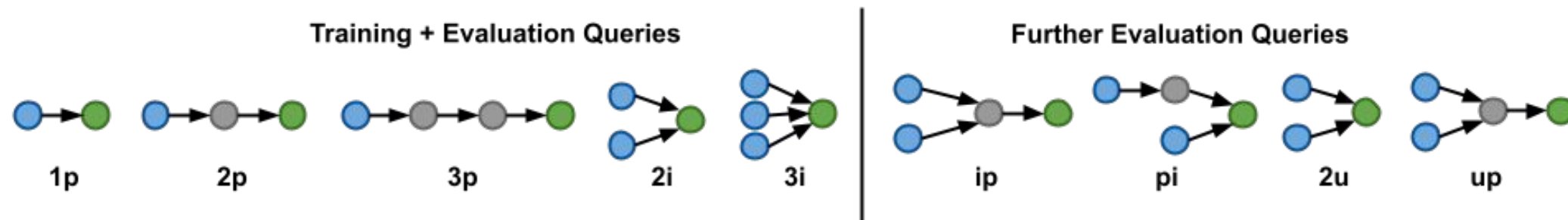
Here is where the problem starts...



Motivation: Logical Reasoning over Knowledge Graphs

Can we do multi-hop reasoning i.e. answer complex queries on an incomplete massive KG?

Our goal: Apply full First-order logic: *Existential, Negation, Conjunction, Disjunction*



Why is it complicated?

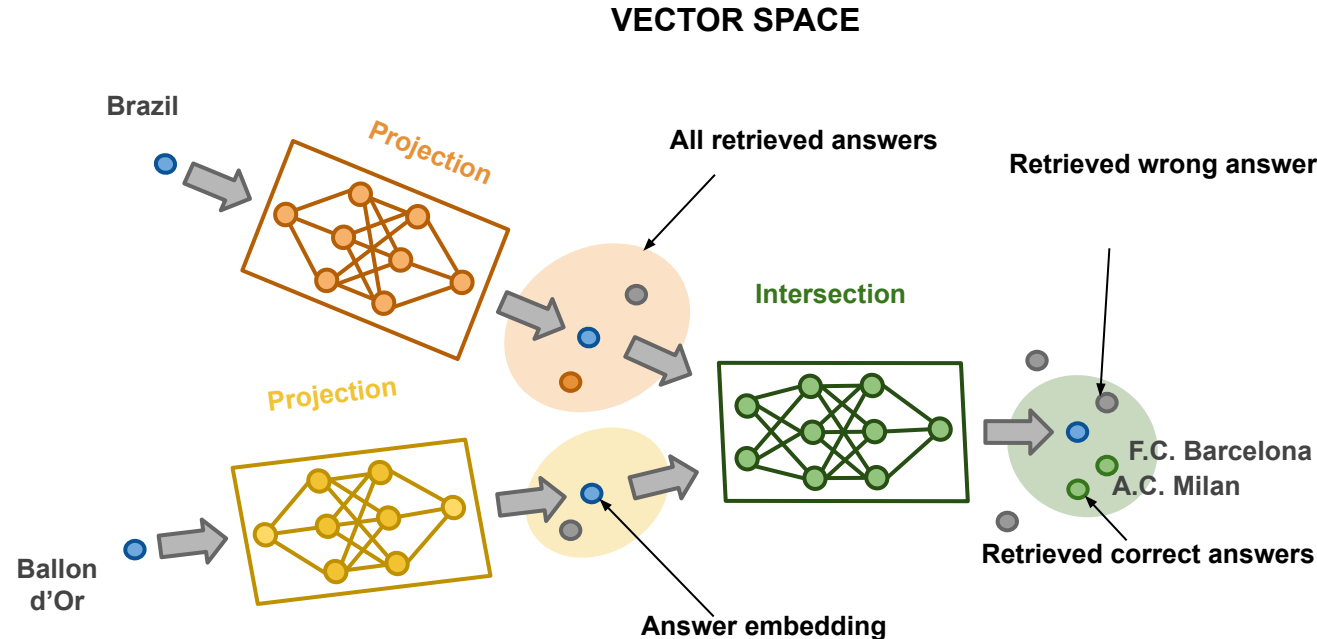
1. Increase in query-hops => Increase in complexity of traditional methods
2. Knowledge graphs are incomplete and very large in real cases

How the system works

Query: "List the teams where Brazilian football players who were awarded a Ballon d'Or played"

Input: Query in logical statements: $(((\text{Brazil}, \text{CitizenOf}), (\text{Ballon d'Or}, \text{Winner})), \text{Team})$

Output: Rank of all entities, according to the value of the negative random sampling. Done by near-neighbor search via *Locality Sensitivity Hashing*



The model uses low-dimensional one-point vector embeddings to represent the entities.

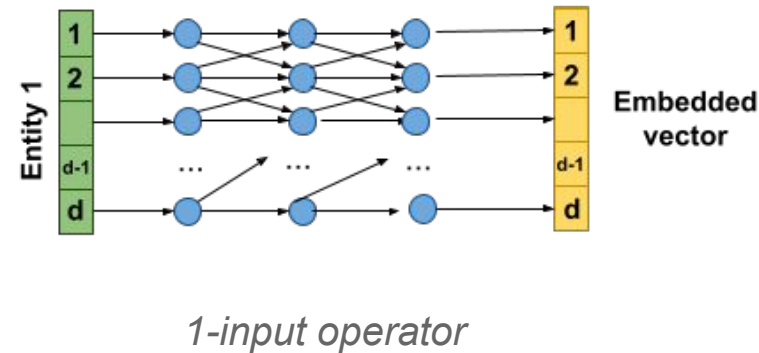
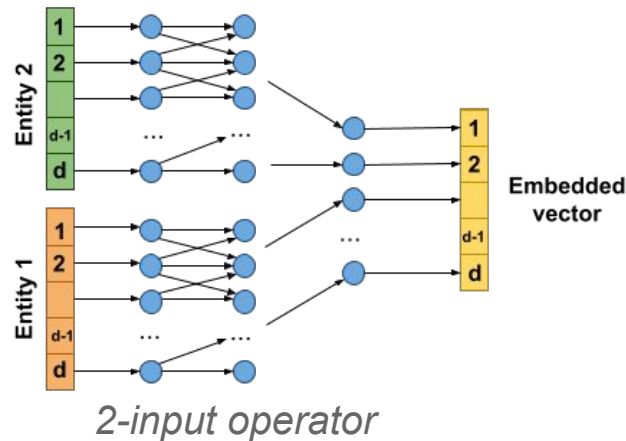
The logical operations are defined by Neural Networks

Multi-Layer Perceptron (MLP)

MLP: Operators are defined by a simple Multi-Layer Perceptron Neural Network

Why Neural Networks? Good results in basic KG tasks [5]

- (+) Flexibility to “learn” any operator
- (-) Hard to understand what they really learn



Operators:

- Projection $P(s_i, r_j) = NN_k(s_i, r_j), \forall i \in S, \forall j \in |R|$
- Intersection $I(s_i, s_j) = NN_k(s_i, s_j), \forall i, j \in S$
- Negation $N(s_i) = NN_k(s_i), \forall s_i \in S$

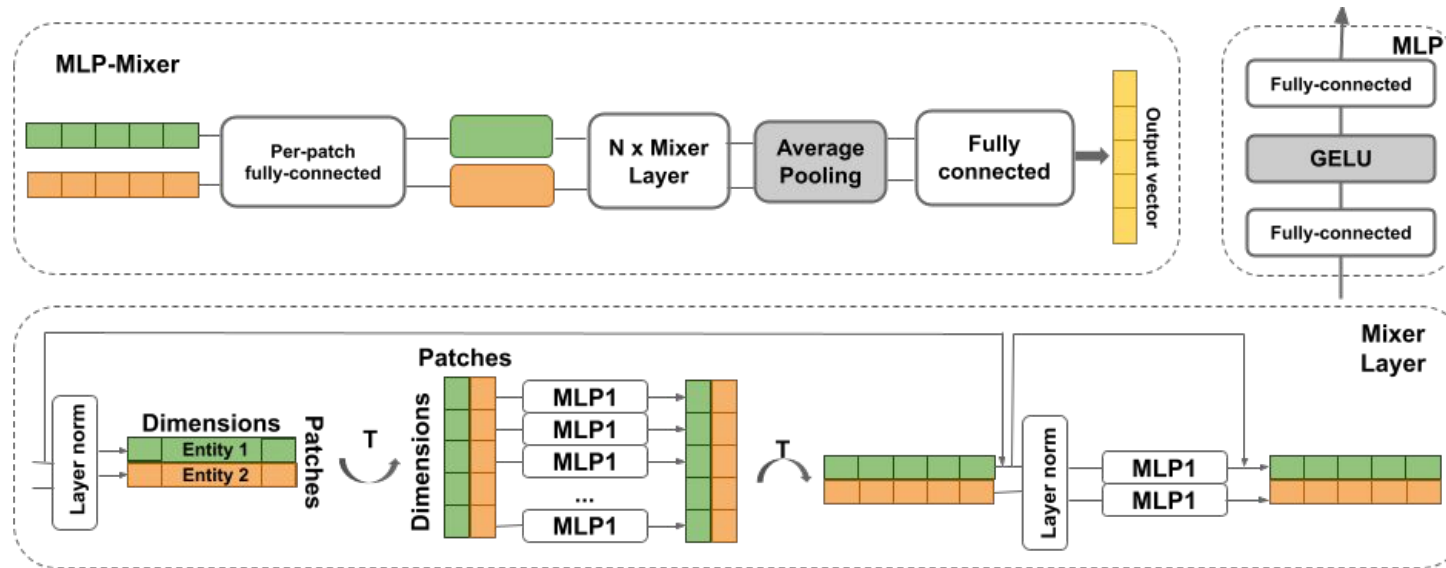
where s_i represents an entity variable and r_j a relation

!Notice we do not have a Union operator because we represent queries in DNF

Multi-Layer Perceptron Mixer (MLP-Mixer)

MLP-Mixer [6] is a Neural Network Architecture built for Image Processing with the purpose of removing convolutions.

MLP-Mixer
Modules



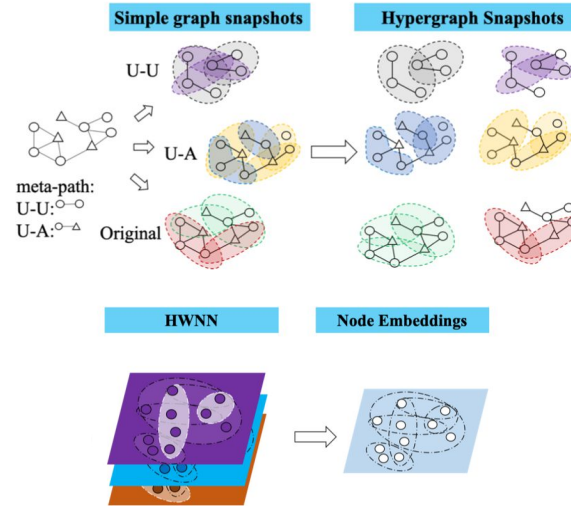
2-input Operators:

- Projection $P(s_i, r_j) = MLP_{mix}(s_i, r_j) \forall i \in S, \forall j \in |R|$
- Intersection $I(s_i, s_j) = MLP_{mix}(s_i, s_j), \forall i, j \in S$

Insight: Convolutional layers are not performing great -> Intuitively, nearby entities are not initially related

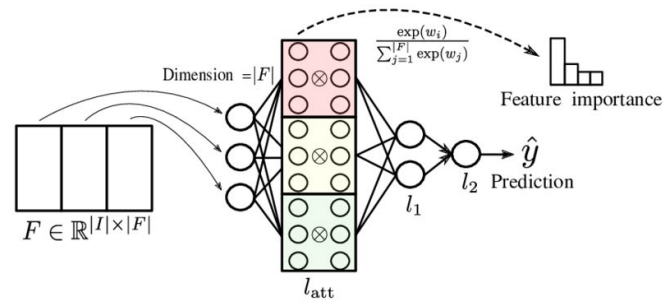
Model variants

Hyper-Graph Embeddings



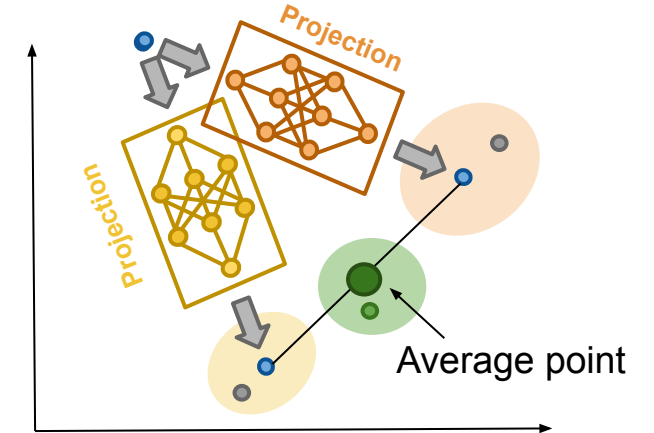
Graph embedding transformation into a series of snapshots to create new node embeddings

Attention mechanism



Include the attention layers in the operators to focus on the “important” parts of the embedding

2-vector Average



NNs may learn different “close” results
We compute the operators twice and average the result

Results: Models vs Baselines

Insights:

1. We see a considerable improvement in all cases
2. Neural Networks seem to be capturing the essence of the logical operations
3. A combination of model variants can potentially lead to a better improvement

	Best model so far (BetaE)			1-point vector encoding (GQE)		
Dataset	MLP	MLP-Mixer	2-vector avg	MLP	MLP-Mixer	2-vector avg
FB15k	5%	4%	9%	36%	35.5%	39%
FB15k-237	7%	9%	11%	28%	29%	31%
NELL995	7%	9%	8%	30%	32%	31%

Table of relative improvements (%)

Results: Negative Queries

Pros: Achieve better results than baseline model

Cons: (1) Hard to understand the representation of a negative entity
(2) Unable to measure query uncertainty

Dataset	Model	2in	3in	inp	pin	pni	avg
FB15K	MLP	17.2	17.8	13.5	9.1	15.2	14.5
	BetaE	14.3	14.7	11.5	6.5	12.4	11.8
FB15-237	MLP	6.6	10.7	8.1	4.7	4.4	6.9
	BetaE	5.1	7.9	7.4	3.6	3.4	5.4
NELL995	MLP	5.1	8.0	10.0	3.6	3.6	6.1
	BetaE	5.1	7.8	10.0	3.1	3.5	5.9

19%
improvement

22%
improvement

4%
improvement

(Measure) **MRR: Mean Reciprocal Rank**

Future work

Some points to cover in future work:

- **Logical Disjunction (\vee):** Now we use DNF transformation to handle this query. Look into other methods that create an OR operator.
- **Logic Regularizers:** Logic Neural Networks can be a good fit for this problem. Our initial results seemed discouraging. Further research needed.
- **Query/answer generation:** The structures we use for training and testing may have a great influence on the system performance. Better query generation techniques could have a performance boost.
- **Other embeddings:** There are other types of embeddings unexplored for this problem. Look into other promising graph embeddings (i.e. quantum embeddings)

References

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*Thank
you*

Alfonso Amayuelas Fernández
alfonso.amayuelas.alumni@epfl.ch

ETH zürich

**DS3Lab: Data Science, Data
Systems, Data Services**

Supervisors:
Shuai Zhang
Susie Rao

Lab Director:
Ce Zhang

<https://ds3lab.inf.ethz.ch>

EPFL

**Distributed Information
Systems Laboratory**

Lab Director:
Karl Aberer

<https://www.epfl.ch/labs/lisir/>