

# Optimizing Neural Networks with Gradient Lexicase Selection

Li Ding<sup>1</sup> & Lee Spector<sup>2,1</sup>

<sup>1</sup> College of Information & Computer Sciences, University of Massachusetts Amherst

<sup>2</sup> Department of Computer Science, Amherst College

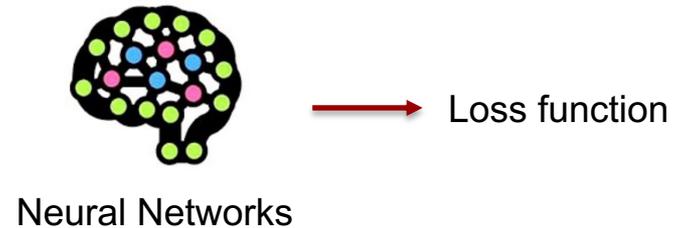
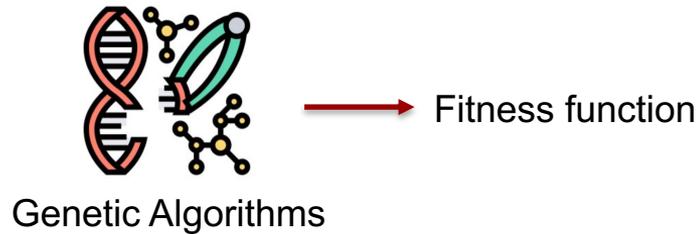
liding@umass.edu, lspector@amherst.edu



**ICLR**  
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Learning Representations

# Aggregated Performance Measure

- Modern data-driven learning algorithms are usually optimized by computing the aggregate performance on the training data.



# Seeking “Compromises”

- One potential drawback for aggregated performance measurement is that the model may learn to seek “compromises” and getting stuck at local optima.

✓ 0.9  
 ✗ 0.1  
 ✓ 0.9  
 ✓ 0.9  
 ✓ 0.9

loss: 2.724

some training steps →

✓ 0.99  
 ✗ 0.1  
 ✓ 0.99  
 ✓ 0.99  
 ✓ 0.99

loss: 2.343

what we prefer

✓ 0.6  
 ✓ 0.6  
 ✓ 0.6  
 ✓ 0.6  
 ✓ 0.6

loss: 2.554

# Lexicase Selection [1]

- Uncompromising problems have been recently explored in evolutionary computation for tasks such as program synthesis.
- Instead of using an aggregated fitness function, lexicase selection gradually eliminates candidates by evaluating on each individual training case.
- It has also been used in rule-based learning, symbolic regression, constraint satisfaction problems, machine learning, and evolutionary robotics to improve model generalization.

[1] Thomas Helmuth, Lee Spector, and James Matheson. Solving uncompromising problems with lexicase selection. IEEE Transactions on Evolutionary Computation, 19(5):630–643, 2014.

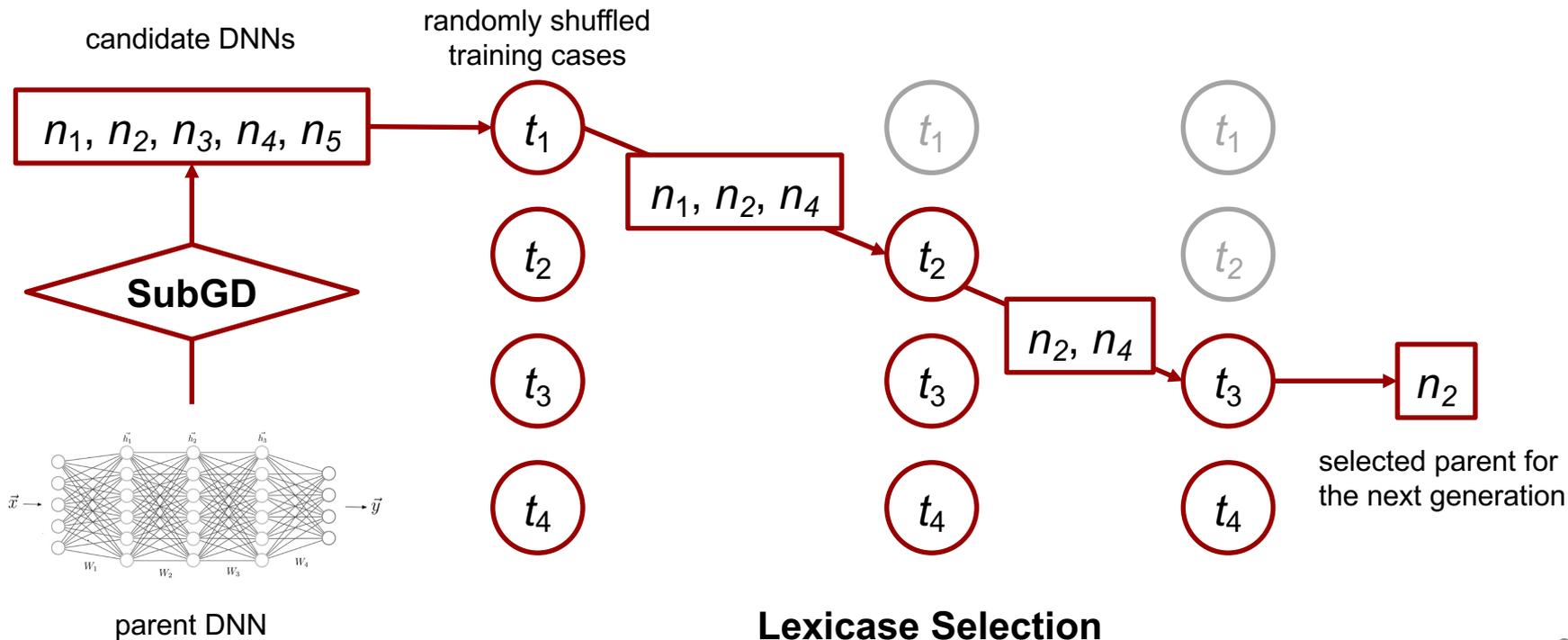
# This Work: Gradient Lexicase Selection

- Our goal is to integrate the idea of lexicase selection to improve the generalization of DNNs, while at the same time keep the efficiency of the popular gradient-based learning.
- Our method has two main components: subset gradient descent (SubGD) and lexicase selection.

# Mutation by Subset Gradient Descent

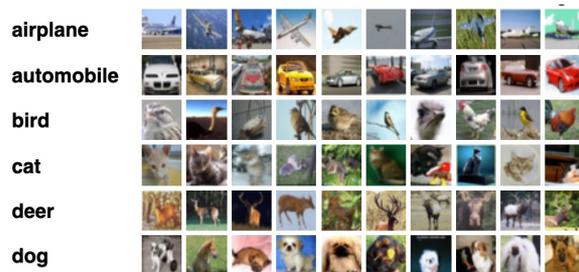
- We propose a gradient-based mutation method: the training set is randomly divided into subsets. Each model candidate is then trained on one of the subsets using stochastic gradient descent.
- There are several advantages:
  - All the candidates are trained with different non-overlapping training samples, so they are more likely to evolve diversely, especially when data augmentation is also included.
  - Each candidate is trained using gradient descent for efficiency.
  - Candidates can be trained in parallel to further reduce computation time.
- The goal is to find a balance between exploration and exploitation towards the whole evolution process.

# Gradient Lexicase Selection



# Experiments

- **Three image classification benchmarks** (CIFAR-10 (Krizhevsky et al., 2009), CIFAR-100 (Krizhevsky et al., 2009), and SVHN (Netzer et al., 2011)) **are used for evaluation.**
- **We implement the proposed algorithm on six popular DNN architectures** (VGG (Simonyan & Zisserman, 2015), ResNet (He et al., 2016), DenseNet (Huang et al., 2017), MobileNetV2 (Sandler et al., 2018), SENet (Hu et al., 2018), EfficientNet (Tan & Le, 2019)).
- **We also implement the original momentum-SGD training as baselines.**



# Results

Table 1: Image classification results. We report the mean percentage accuracy (*acc.*) with standard deviation (*std.*) obtained by running the same experiment with three different random seeds. The last column (*acc. ↑*) calculates the difference of accuracy by using our method compared to baseline, where positive numbers indicate improvement.

Dataset	Architecture	Baseline		Lexicase		<i>acc. ↑</i>
		<i>acc.</i>	<i>std.</i>	<i>acc.</i>	<i>std.</i>	
CIFAR-10	VGG16	92.85	0.10	93.40	0.13	<b>0.55</b>
	ResNet18	94.82	0.10	95.35	0.06	<b>0.53</b>
	ResNet50	94.63	0.46	94.98	0.18	<b>0.34</b>
	DenseNet121	95.06	0.31	95.38	0.04	<b>0.32</b>
	MobileNetV2	94.37	0.19	93.97	0.12	-0.39
	SENet18	94.69	0.14	95.37	0.23	<b>0.68</b>
	EfficientNetB0	92.60	0.18	93.00	0.22	<b>0.40</b>
CIFAR-100	VGG16	72.09	0.52	72.53	0.20	<b>0.44</b>
	ResNet18	76.33	0.29	76.68	0.40	<b>0.35</b>
	ResNet50	76.82	0.96	77.44	0.25	<b>0.63</b>
	DenseNet121	78.72	0.82	79.08	0.26	<b>0.36</b>
	MobileNetV2	75.87	0.28	75.57	0.30	-0.30
	SENet18	76.97	0.06	77.22	0.29	<b>0.25</b>
	EfficientNetB0	71.03	0.86	71.36	0.87	<b>0.33</b>
SVHN	VGG16	96.27	0.06	96.29	0.08	<b>0.02</b>
	ResNet18	96.43	0.14	96.62	0.08	<b>0.19</b>
	ResNet50	96.69	0.21	96.74	0.07	<b>0.04</b>
	DenseNet121	96.82	0.16	96.87	0.03	<b>0.05</b>
	MobileNetV2	96.23	0.13	96.26	0.07	<b>0.03</b>
	SENet18	96.62	0.19	96.59	0.11	-0.03
	EfficientNetB0	96.14	0.12	95.94	0.10	-0.20

# Results

- Comparing other selection methods.

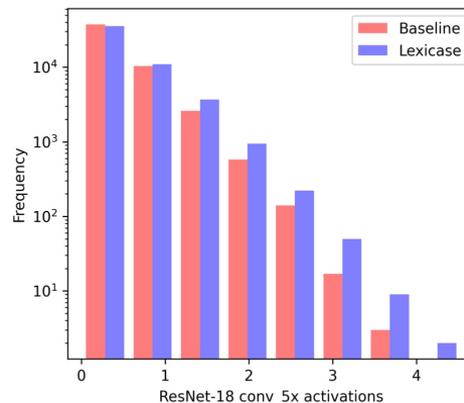
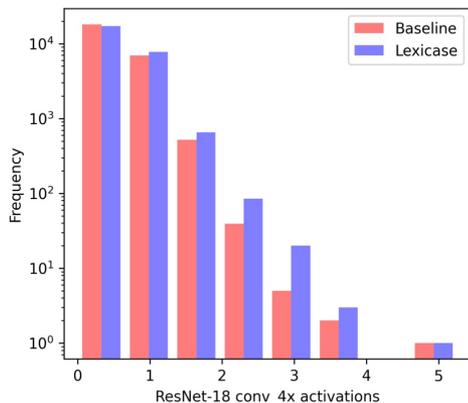
Table 2: Comparing gradient lexicase selection to other selection methods on CIFAR-10. We report the mean percentage accuracy (*acc.*) with standard deviation (*std.*) obtained by running the same experiment with three different random seeds.

Architecture	SGD		Random		Tournament		Lexicase	
	<i>acc.</i>	<i>std.</i>	<i>acc.</i>	<i>std.</i>	<i>acc.</i>	<i>std.</i>	<i>acc.</i>	<i>std.</i>
VGG16	92.85	0.10	92.97	0.15	93.12	0.12	<b>93.40</b>	0.13
ResNet18	94.82	0.10	94.99	0.12	94.90	0.14	<b>95.35</b>	0.06
ResNet50	94.63	0.46	94.75	0.13	94.77	0.04	<b>94.98</b>	0.18
DenseNet121	95.06	0.31	95.13	0.04	95.12	0.02	<b>95.38</b>	0.04
MobileNetV2	<b>94.37</b>	0.19	94.02	0.14	93.91	0.09	93.97	0.12
SENet18	94.69	0.14	95.04	0.15	95.01	0.23	<b>95.37</b>	0.23
EfficientNetB0	92.60	0.18	92.77	0.11	92.83	0.12	<b>93.00</b>	0.22

# Ablation Studies

- Representation Diversity

- Lexicase selection has been shown to improve population diversity in GP, it may as well help DNNs learn more diverse representations, which improves model generalization.
- We visualize the feature activations in ResNet-18 trained using normal SGD and gradient lexicase selection, which shows that our method produces more diverse representations.



# Conclusion

- We propose Gradient Lexicase Selection, an evolutionary algorithm that incorporates lexicase selection with gradient descent to help optimizing DNNs for better generalization.
- Experimental results show that the proposed method can improve the generalization of popular DNN architectures on the image classification benchmarks.
- Several ablation studies further validates our method. Qualitative analysis also shows that our method can produce better representation diversity.

UMassAmherst

College of Information  
& Computer Sciences

## COMPUTING FOR THE COMMON GOOD

Li Ding ([lding@umass.edu](mailto:lding@umass.edu)) &

Lee Spector ([lspector@amherst.edu](mailto:lspector@amherst.edu))