Pink Noise Is All You Need

Colored Noise Exploration in Deep Reinforcement Learning

Onno Eberhard¹ · Jakob Hollenstein^{2,1} · Cristina Pinneri^{1,3} · Georg Martius¹

¹Max Planck Institute for Intelligent Systems

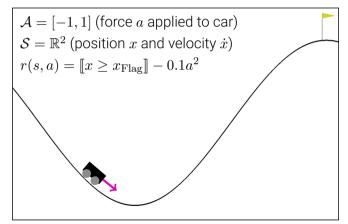
²Universität Innsbruck ³ETH Zürich



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Introduction

- ► Setting: Reinforcement learning for continuous control
- ► Mountain-car problem: Why is exploration necessary?

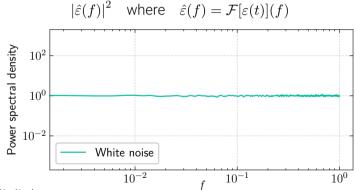


White Noise Exploration

- ▶ Usual method for exploration: add some noise ε_t to actions
- ▶ If $\varepsilon_t \sim \mathcal{N}(0, I)$ independently at every time step, then $\varepsilon_{1:T}$ is called **white noise**
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 - ▶ Used as default by many algorithms: TD3, SAC, MPO, ...
- ▶ The **power spectral density** (PSD) is defined for any signal $\varepsilon(t)$ as



Temporal Correlation

- ▶ White noise has no temporal correlation ($cov[\varepsilon_t, \varepsilon_{t'}] = 0$)
- ► This makes exploration very slow, simple tasks like Mountain-car challenging

Temporal Correlation

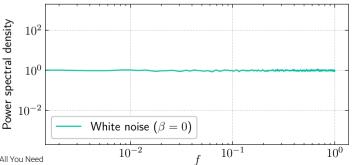
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- ► Popular choice: Ornstein-Uhlenbeck (OU) noise

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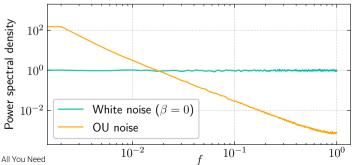
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- ▶ Simple fix: Use a temporally correlated noise process $(cov[\varepsilon_t, \varepsilon_{t'}] > 0)$
- ► Popular choice: Ornstein-Uhlenbeck (OU) noise
- lacktriangle Problem: Very strong temporal correlation ightarrow poor performance if not needed
- ▶ Idea: Use intermediate temporal correlation to get best of both worlds

- ▶ Noise with a PSD proportional to $f^{-\beta}$ is called **colored noise** with color β
- lacktriangle Color parameter eta controls strength of temporal correlation

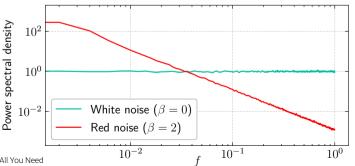
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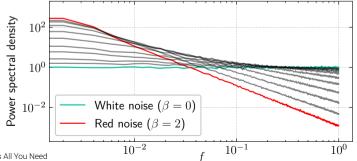
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- ▶ OU noise is related to red noise (CN with $\beta = 2$)



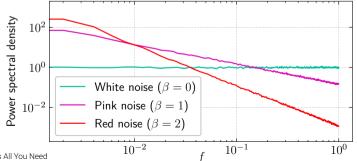
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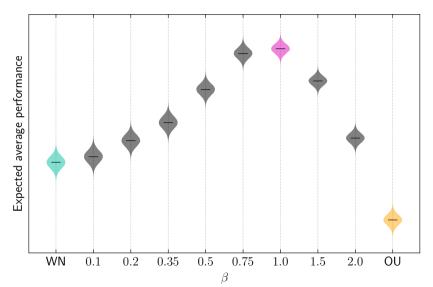
Experiments

▶ We perform experiments on a number of benchmark tasks using MPO and SAC

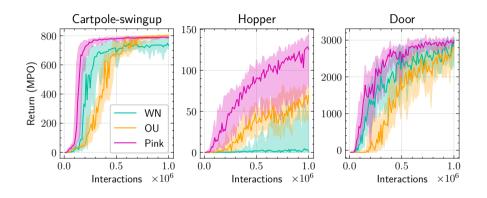


- ► Measure **average performance** (mean normalized performance across all tasks)
 - ► Default action noise should work well everywhere

Results



Results



- ▶ Pink noise works well on **all** environments we tested
- ► Not true for white noise or OU noise!

Pink Noise

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- ► Pink noise performed better than all these methods

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Why does pink noise work so well as a default?

- ► Works very well on some environments
- ► Works well on all environments

► Simple 2-dimensional "bounded integrator" environment:

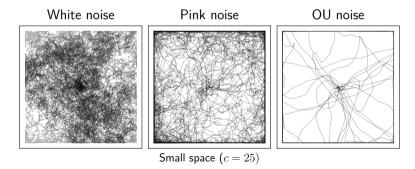
$$s_{t+1} = \operatorname{clip}(s_t + a_t, -c\mathbf{1}, +c\mathbf{1})$$

▶ Parameterized by its size (area = $4c^2$)

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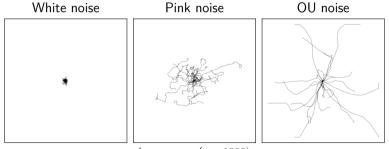
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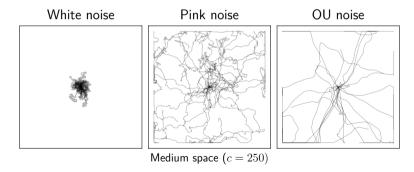


Large space (c=1000)

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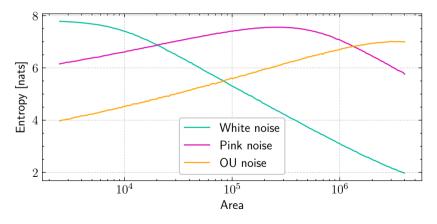
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- ► Measure exploration by estimating state-visitation entropy
- ► Repeat for a large range of environment sizes

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The Power of Pink

- ► Very similar results on a second simplified environment
- ▶ Pink noise is **general**: less sensitive to the environment parameterization
- ► Explains average performance results (benchmark experiments)
 - lacktriangledown Many different tasks with different preferences ightarrow general noise preferable

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Takeaway

► Try pink noise as the default action noise pip install pink-noise-rl

Thank you!

https://bit.ly/pink-noise-rl

More Info: