Estimating Conditional Mutual Information for Dynamic Feature Selection

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Introduction

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- Dynamic Feature Selection: paradigm where we **sequentially query features** to make predictions with a minimal budget
- Important in settings like **emergency medicine** where not all features are available, are costly to acquire, and best selections differ between predictions
- We propose **an information-theoretic** approach which selects features based on their **conditional mutual information (CMI)** with the target variable

Contribution

- We develop a learning approach (DIME) to estimate the CMI in a discriminative fashion and prove that our objective recovers the exact CMI at optimality
- Most works assume uniform feature costs; we adapt DIME to scenarios with non-uniform feature costs
- We analyze the role of variable feature budgets between samples and how they enable an improved cost-accuracy tradeoff through multiple stopping criteria
- DIME provides consistent gains across all the datasets tested compared to many recent methods

Proposed Method

- CMI, denoted as $I(y; x_i | x_s)$, shows how much information an unknown feature x_i provides about the target y given the current set of selected features x_s
- Given a value network that accurately predicts CMI, we can use it greedily select the next feature
- This is identical to performing greedy uncertainty minimization

Training Approach



- Two networks: the value network v and predictor network f
- At each selection step *n* the value network $v(x_s; \phi)$ predicts the CMI $I(y; x_i | x_s)$ for each candidate feature
- The feature x_i which maximizes the CMI is used for the next prediction $f(x_{S\cup i}; \theta)$

Training Approach

• Predictor loss: cross entropy

 $\min_{\theta} \mathbb{E}_{xy} \mathbb{E}_{s}[\ell(f(x_{s};\theta), y)]$

• Value network loss: MSE

$$\min_{\phi} \mathbb{E}_{xy} \mathbb{E}_{s} \mathbb{E}_{i} \left[\left(v_{i}(x_{s}; \phi) - \Delta(x_{s}, x_{i}, y) \right)^{2} \right]$$

where $\Delta(x_s, x_i, y) = \ell(f(x_s), y) - \ell(f(x_s, x_i), y)$

• Models are trained jointly, with selections being made using the ϵ -greedy approach

Datasets

- Tabular Datasets
 - MNIST (flattened, d = 784)
 - ROSMAP dataset for dementia onset prediction (d = 43)
 - Intubation dataset for predicting the need of respiratory support (d = 35)
- Image Datasets
 - Imagenette, an Imagenet subset with 10 classes
 - Imagenet-100, an Imagenet subset with 100 classes
 - MHIST, a histopathology dataset to predict benign or pre-cancerous lesions

Results: Tabular Datasets



- Used multilayer perceptrons (MLPs) with two hidden layers and ReLU non-linearity
- DIME achieves the best results among all methods for both medical diagnosis tasks
- Performs the best on MNIST, achieving over 90% accuracy with an average of ~ 10/784 features (1.27%)

Results: Image Datasets



- Used Vision Transformers (ViT-small-patch-16) with a shared backbone
- Images are 256x256 with each feature being a 16x16 patch
- DIME with the penalized stopping criteria outperforms the baselines for all feature budgets
- Achieves nearly 97% accuracy on Imagenette with only \sim 15/196 patches (7.7%).

Results: Non-Uniform Costs



- For Intubation, relative costs are considered
- For ROSMAP, costs are expressed as the time required to obtain each feature
- DIME provides the best cost-accuracy tradeoff, reflecting the improved CMI estimation

Conclusion

- This work presents DIME, a new DFS approach enabled by estimating the CMI in a **discriminative fashion**
- Our approach involves learning value and predictor networks, trained in an endto-end fashion with a straightforward regression objective
- We prove that our training approach recovers the exact CMI at optimality
- Empirically, DIME accurately estimates the CMI and enables an improved costaccuracy tradeoff
- DIME beats prior methods, is robust to higher image resolutions, scales to more classes, and benefits from modern architectures