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ITRANSFORMER: INVERTED TRANSFORMERS ARE EFFECTIVE FOR TIME SERIES FORECASTING

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Time Series Forecasting



Wide Applications



Energy Consumption



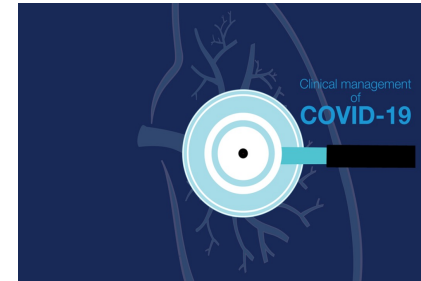
Traffic Flow



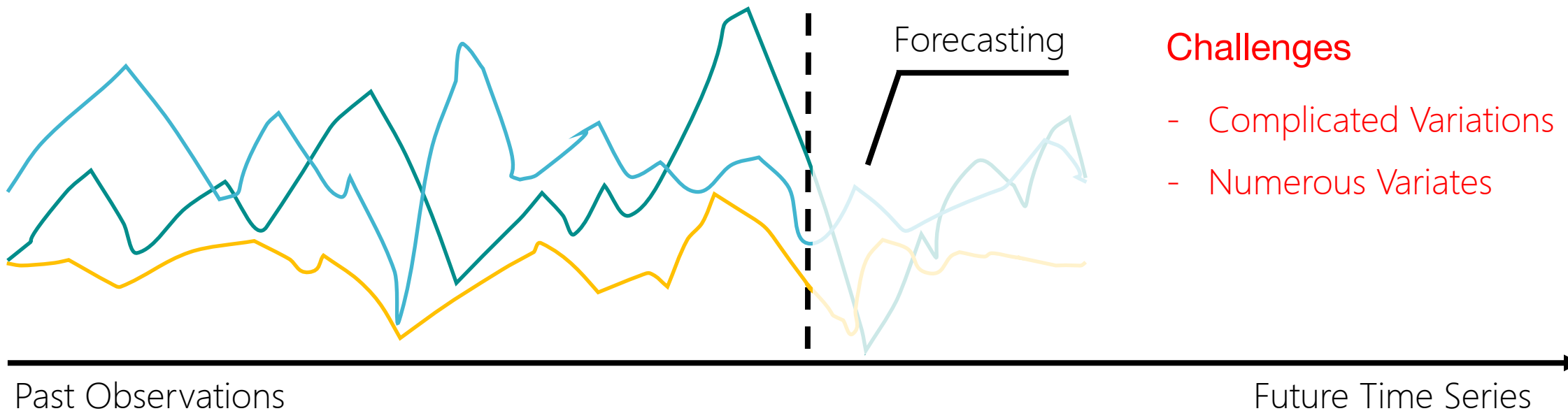
Economic Changes



Weather Variations



Disease Estimations



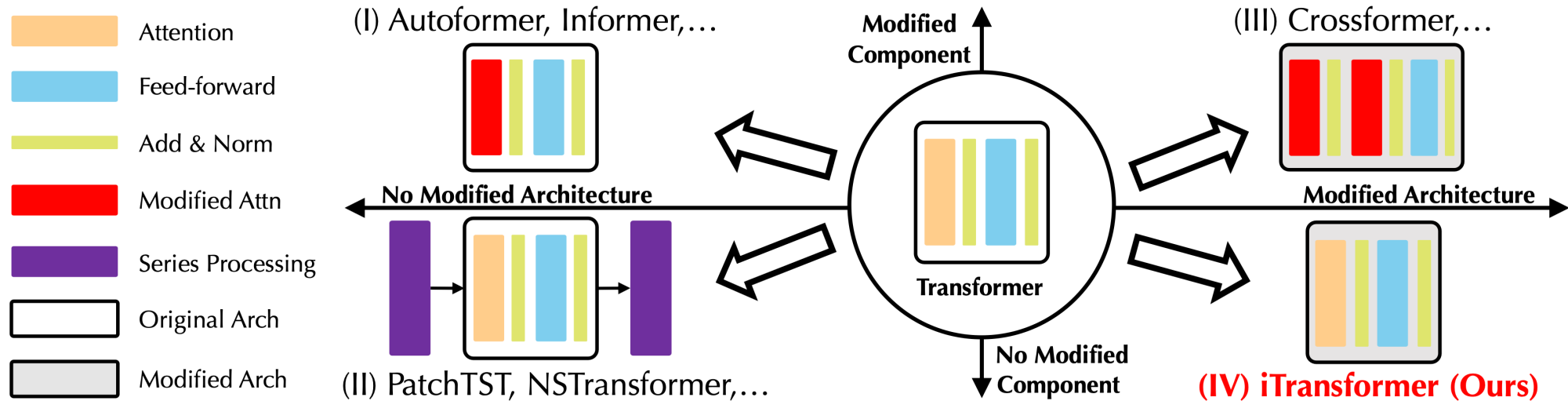
Challenges

- Complicated Variations
- Numerous Variates



Transformer-based Forecaster

- Emergence of Transformers in TSF

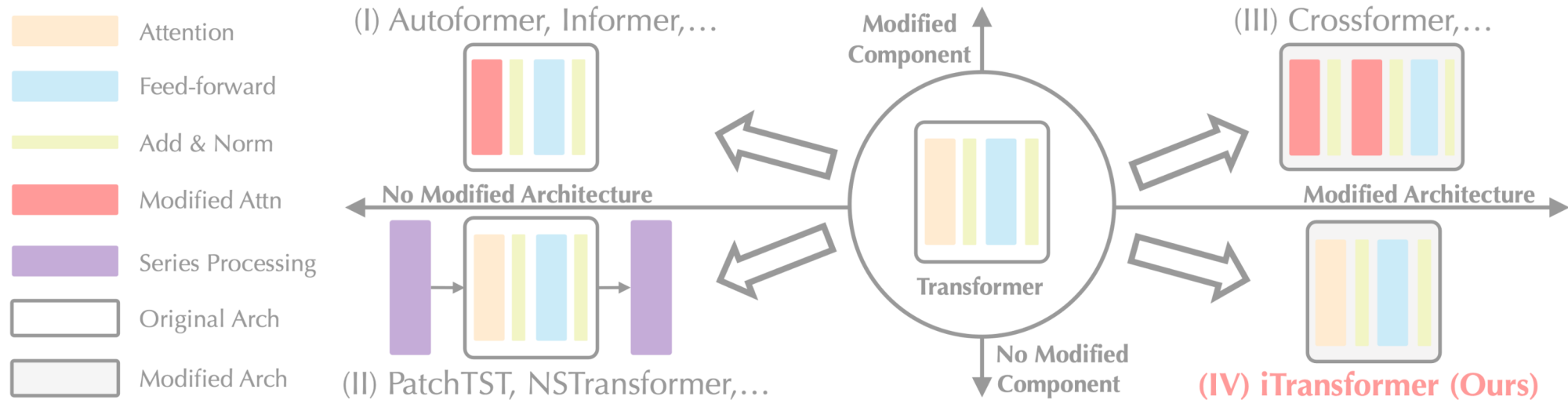


- Passionate modifications!

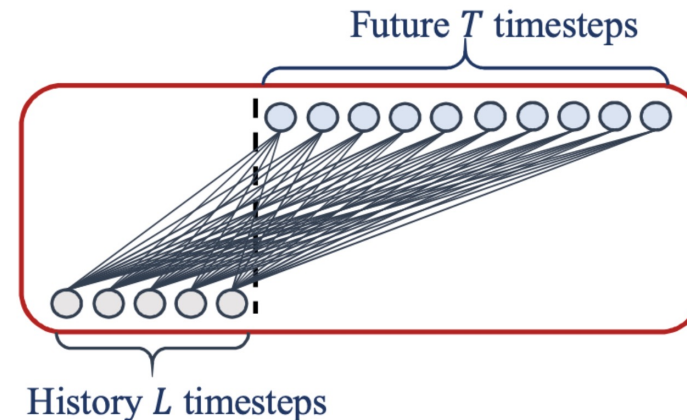


Transformer-based Forecaster

- Emergence of Transformers in TSF

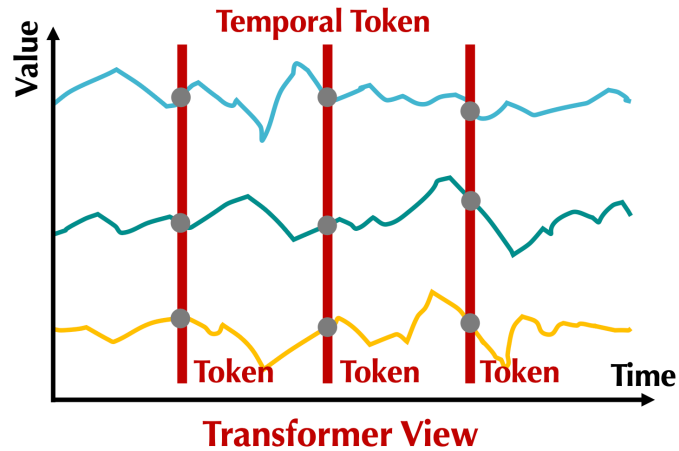


- Passionate modifications!
- Linear models beat Transformers?
 - ARIMA, Holt-Winter ...
 - DLinear, RLinear ...



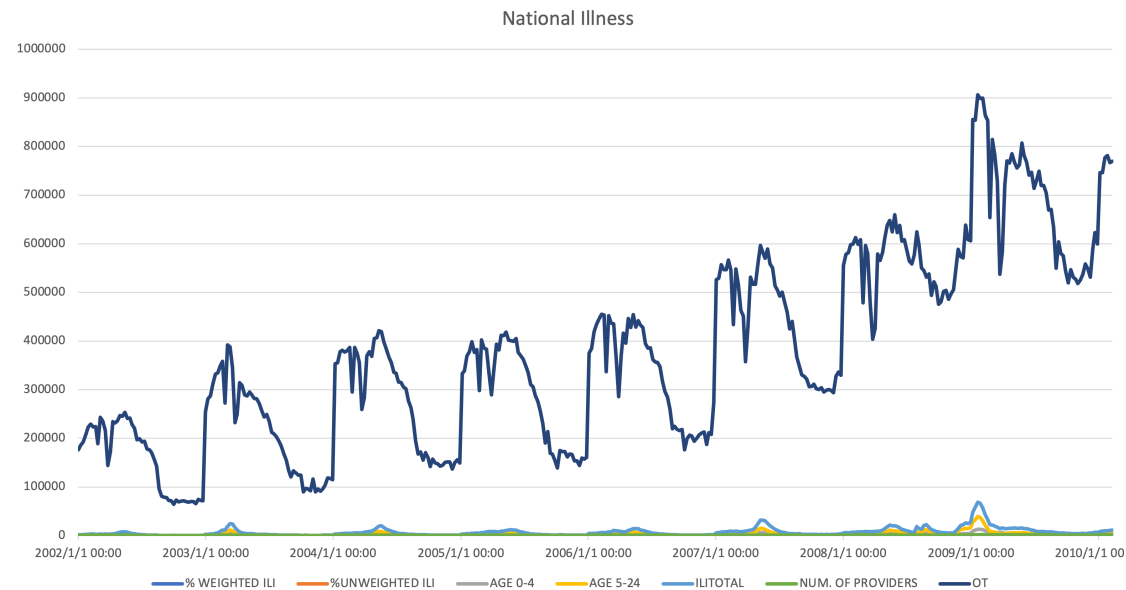


Time Series Tokens in Transformer



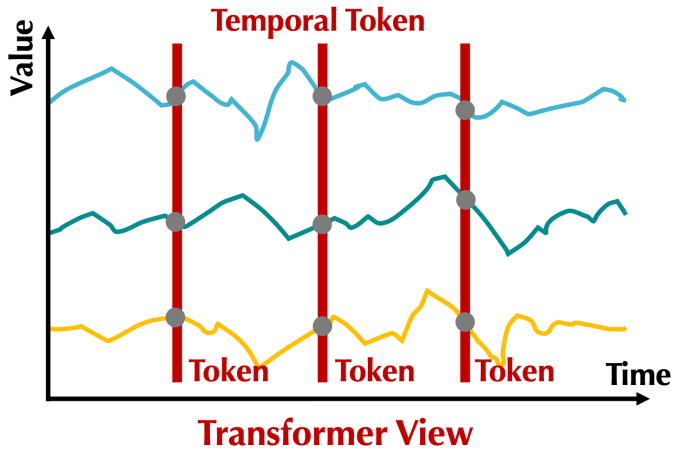
Underlying Risks of Tokenization

- Excessively receptive field
- Inconsistent scale and distribution



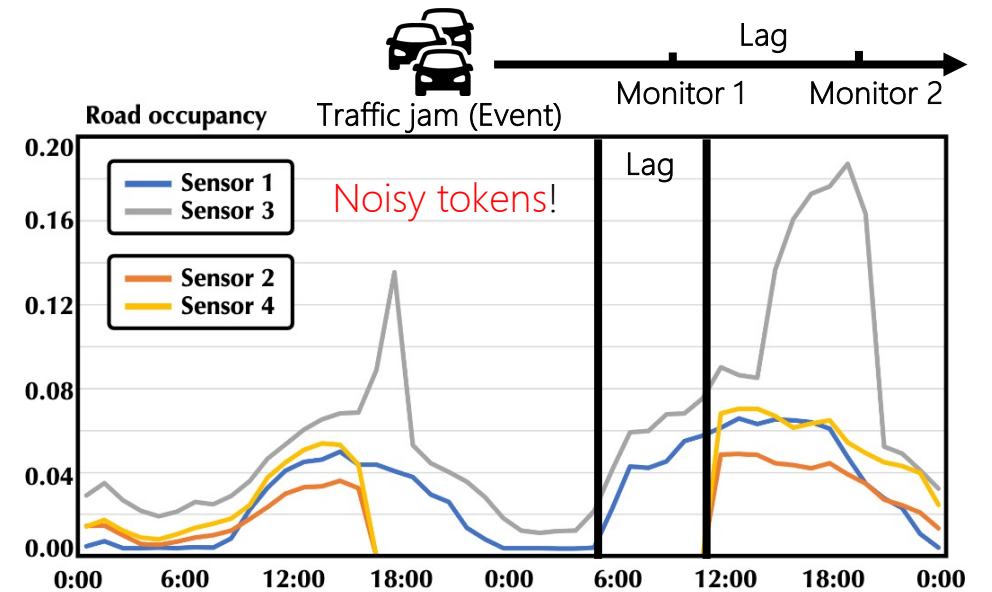
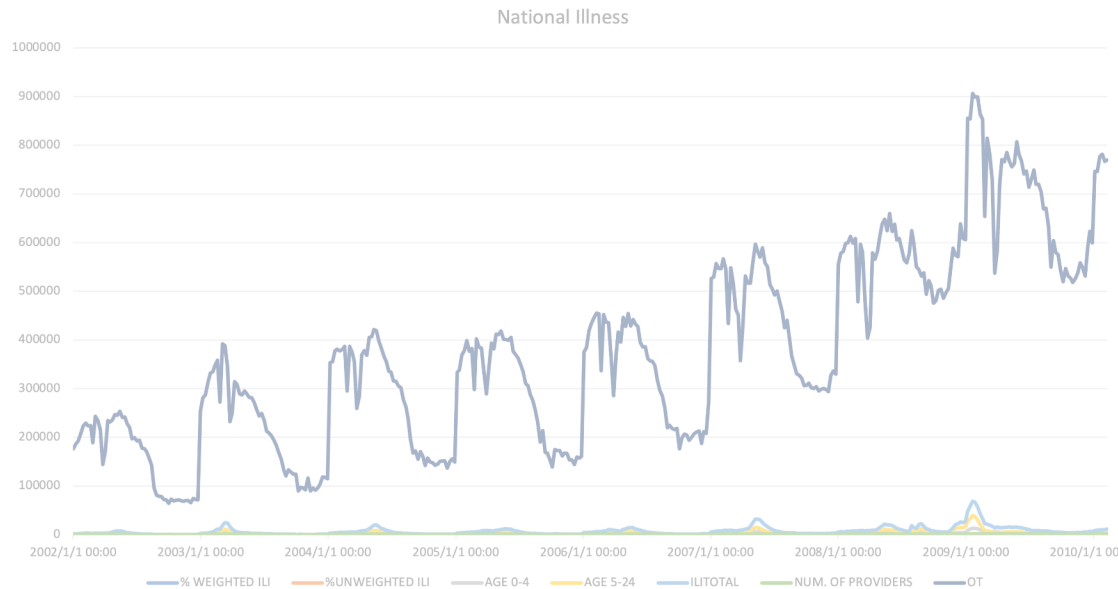
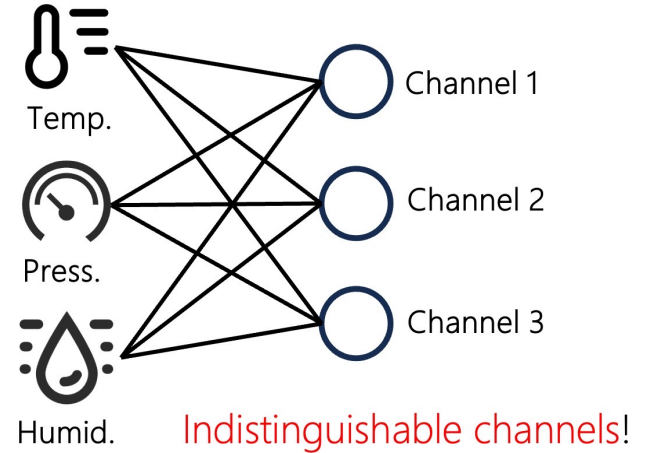


Time Series Tokens in Transformer

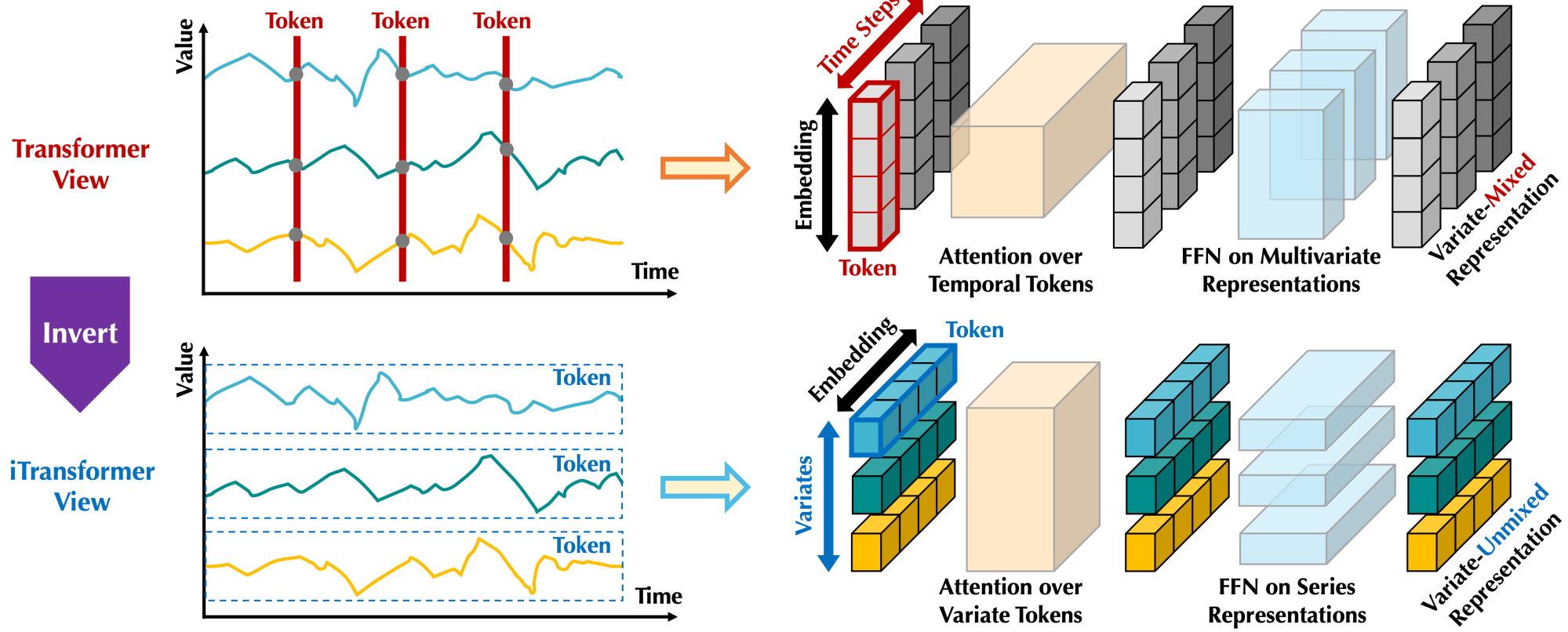


Underlying Risks of Tokenization

- Excessively local receptive field
- Inconsistent scale and distribution
- Variate-mixed representations
- Inherent lags between variates...



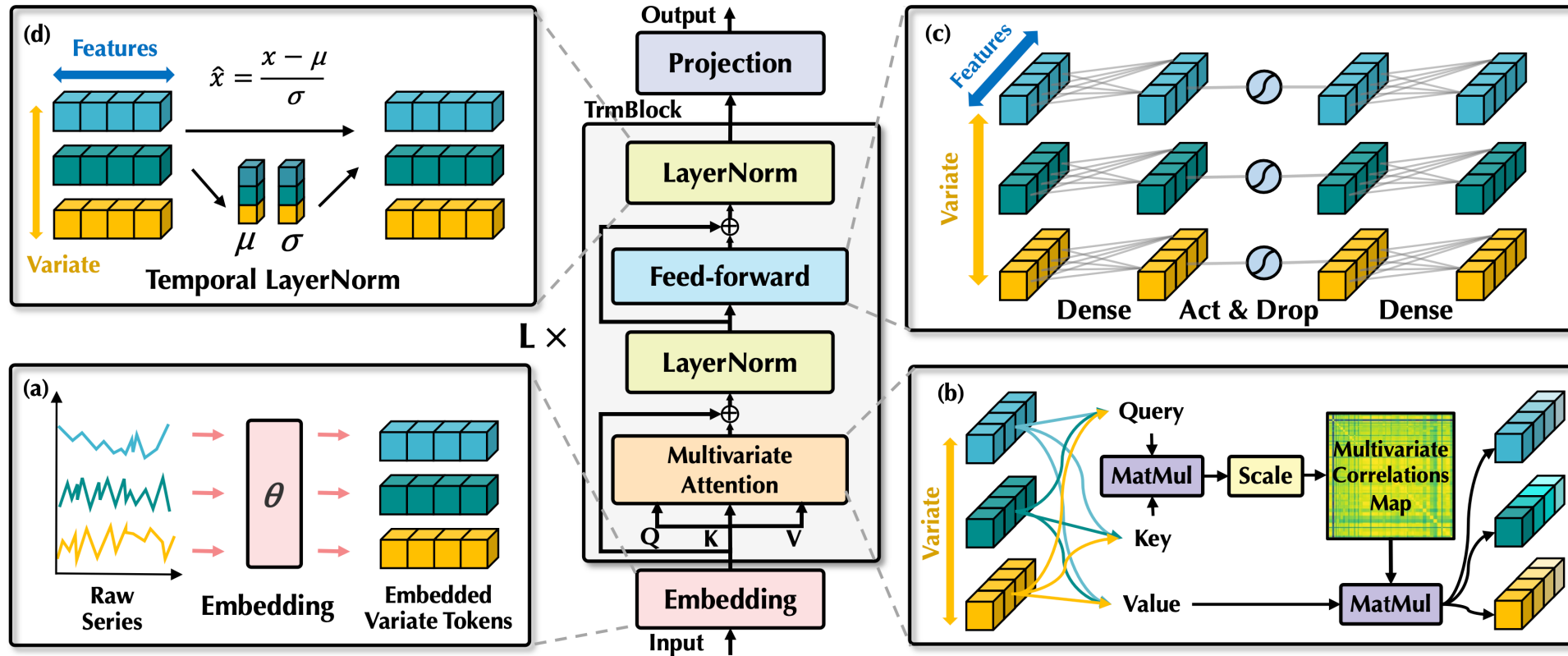
Motivation



iTransformer regards multivariate series **invertedly** without any modular modification



iTransformer

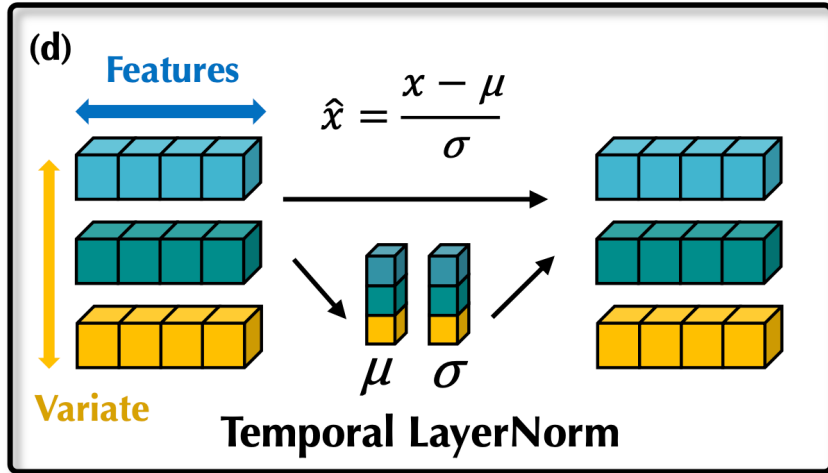


Encoder-only Arch.

$$\mathbf{h}_n^0 = \text{Embedding}(\mathbf{X}_{:,n}),$$
$$\mathbf{H}^{l+1} = \text{TrmBlock}(\mathbf{H}^l),$$
$$\hat{\mathbf{Y}}_{:,n} = \text{Projection}(\mathbf{h}_n^L).$$

- Time series of individual variate as the Variate Token
- LayerNorm and FFN for Variate-centric Representations
- Multivariate Correlations are captured by self-attention

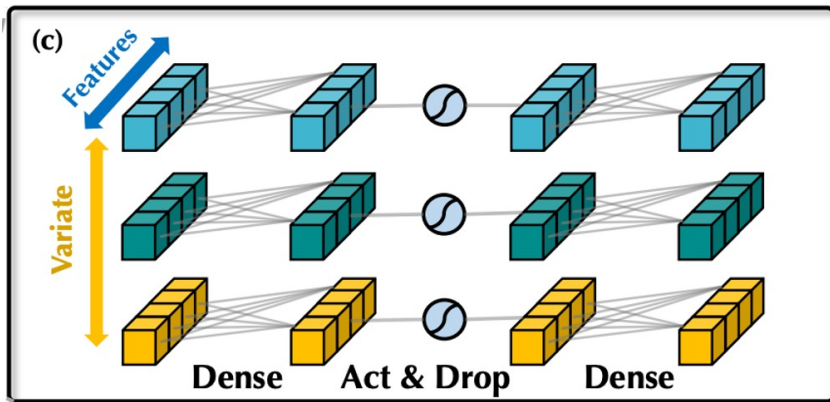
Transformer Modules



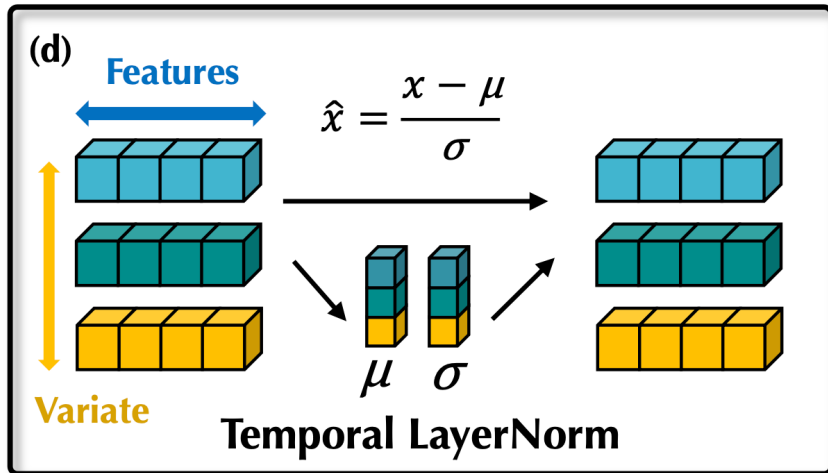
Layer normalization (**within Variate Tokens**)

$$\text{LayerNorm}(\mathbf{H}) = \left\{ \frac{\mathbf{h}_n - \text{Mean}(\mathbf{h}_n)}{\sqrt{\text{Var}(\mathbf{h}_n)}} \mid n = 1, \dots, N \right\}$$

Mitigate variate discrepancies in scaling and distribution
 Instead, time-unaligned events are merged and the obtained Temporal Tokens can be over-smoothed



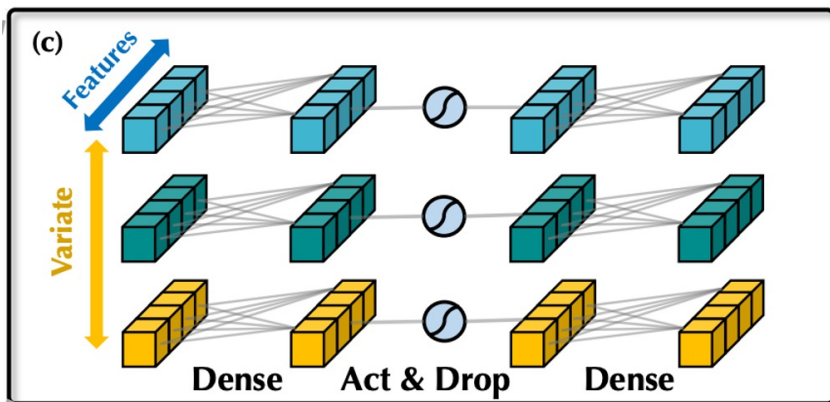
Transformer Modules



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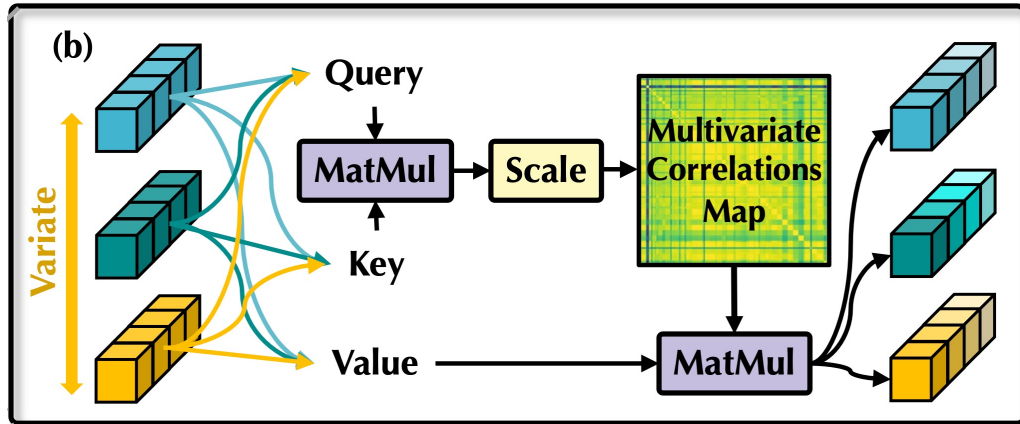


Feed-forward network (**within Variate Tokens**)

- Learns temporal representation
- Describe intrinsic properties of time series
- Transferable representation across variates

Naturally captured: Nonlinear temporal representation under Channel Independence

Module Reflections

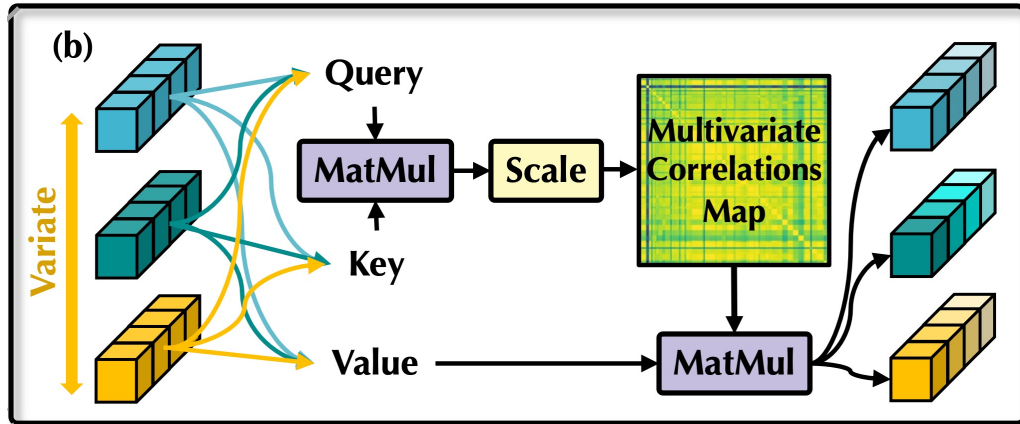


Self-attention (among Variate Tokens)

$$\mathbf{H} = \{\mathbf{h}_0, \dots, \mathbf{h}_N\} \quad N - \text{Variate number}$$

$\mathbf{q}_i, \mathbf{k}_j$ - Query and key of Variate Tokens

Module Reflections



Self-attention (among Variate Tokens)

$$\mathbf{H} = \{\mathbf{h}_0, \dots, \mathbf{h}_N\} \quad N - \text{Variate number}$$

$\mathbf{q}_i, \mathbf{k}_j$ - Query and key of Variate Tokens

Pearson Correlation coefficients:

$$\rho_{xy} = \frac{\sum_i (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_i (x_i - \bar{x})^2} \sqrt{\sum_i (y_i - \bar{y})^2}}$$



Elements of Attention:

$$\mathbf{A}_{i,j} = (\mathbf{Q}\mathbf{K}^\top / \sqrt{d_k})_{i,j} \propto \mathbf{q}_i^\top \mathbf{k}_j$$



$\mathbf{A} \in \mathbb{R}^{N \times N}$ - Multivariate Correlations

Highly correlated tokens will be more weighted with the Value

$$\text{Softmax} \left(\frac{\mathbf{Q}\mathbf{K}^\top}{\sqrt{d_k}} \right) \mathbf{V}$$



Time Series Forecasting

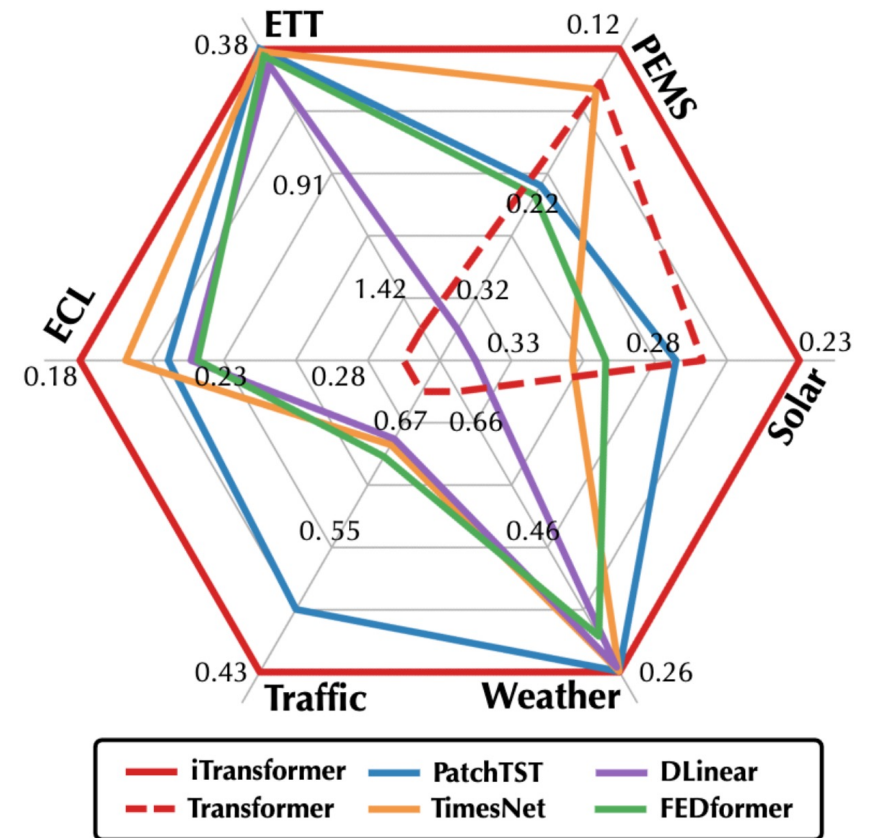
7 Benchmark (13 Datasets, 52 Prediction Settings)

Models	iTransformer (Ours)		RLinear (2023)		PatchTST (2023)		Crossformer (2023)		TiDE (2023)		TimesNet (2023)		DLinear (2023)	
	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE
ECL	0.178	0.270	0.219	0.298	0.205	<u>0.290</u>	0.244	0.334	0.251	0.344	<u>0.192</u>	0.295	0.212	0.300
ETT (Avg)	0.383	0.399	0.380	0.392	<u>0.381</u>	<u>0.397</u>	0.685	0.578	0.482	0.470	0.391	0.404	0.442	0.444
Exchange	<u>0.360</u>	0.403	0.378	0.417	0.367	<u>0.404</u>	0.940	0.707	0.370	0.413	0.416	0.443	0.354	0.414
Traffic	0.428	0.282	0.626	0.378	<u>0.481</u>	<u>0.304</u>	0.550	<u>0.304</u>	0.760	0.473	0.620	0.336	0.625	0.383
Weather	0.258	0.278	0.272	0.291	<u>0.259</u>	<u>0.281</u>	0.259	0.315	0.271	0.320	0.259	0.287	0.265	0.317
Solar-Energy	0.233	0.262	0.369	0.356	<u>0.270</u>	<u>0.307</u>	0.641	0.639	0.347	0.417	0.301	0.319	0.330	0.401
PEMS (Avg)	0.119	0.218	0.514	0.482	0.217	0.305	0.220	0.304	0.375	0.440	0.148	0.246	0.320	0.394

Market Datasets (Server Load Prediction of Ant Group)

Models	iTransformer (Ours)		RLinear (2023)		PatchTST (2023)		Crossformer (2023)		TiDE (2023)		TimesNet (2023)		DLinear (2023)	
	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE
Merchant	0.072	0.147	0.152	0.247	<u>0.084</u>	<u>0.171</u>	0.117	0.181	0.187	0.289	0.093	0.184	0.110	0.206
Wealth	0.345	<u>0.289</u>	0.585	0.461	0.394	0.326	0.429	0.288	0.595	0.481	<u>0.360</u>	0.318	0.501	0.412
Finance	0.184	0.216	0.395	0.336	<u>0.231</u>	<u>0.248</u>	5.333	0.618	0.987	0.442	0.516	0.308	0.765	0.372
Terminal	0.065	0.150	0.180	0.286	0.077	0.179	<u>0.071</u>	<u>0.162</u>	0.216	0.311	0.080	0.179	0.106	0.210
Payment	0.072	0.144	0.143	0.245	<u>0.084</u>	<u>0.174</u>	0.207	0.179	0.208	0.278	0.105	0.182	0.116	0.200
Customer	0.094	0.150	0.214	0.261	<u>0.118</u>	<u>0.180</u>	0.309	0.194	0.308	0.307	0.142	0.191	0.184	0.219

Averaged MSE (4 prediction lengths)



Achieve **state-of-the-art** on MTSF

Excel at high-dimensional series: ECL, Traffic, Solar...

Framework Generality



Models		Transformer (2017)		Reformer (2020)		Informer (2021)		Flowformer (2022)		Flashformer (2022)	
Metric		MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE
ECL	Original	0.277	0.372	0.338	0.422	0.311	0.397	0.267	0.359	0.285	0.377
	+Inverted	0.178	0.270	0.208	0.301	0.216	0.311	0.210	0.293	0.206	0.291
Promotion		35.6%	27.4%	38.4%	28.7%	30.5%	21.6%	21.3%	18.6%	27.8%	22.9%
Traffic	Original	0.665	0.363	0.741	0.422	0.764	0.416	0.750	0.421	0.658	0.356
	+Inverted	0.428	0.282	0.647	0.370	0.662	0.380	0.524	0.355	0.492	0.333
Promotion		35.6%	22.3%	12.7%	12.3%	13.3%	8.6%	30.1%	15.6%	25.2%	6.4%
Weather	Original	0.657	0.572	0.803	0.656	0.634	0.548	0.286	0.308	0.659	0.574
	+Inverted	0.258	0.279	0.248	0.292	0.271	0.330	0.266	0.285	0.262	0.282
Promotion		60.2%	50.8%	69.2%	55.5%	57.3%	39.8%	7.2%	7.7%	60.2%	50.8%

Prediction Accuracy

Transformer
↑ 38.9%

Reformer
↑ 36.1%

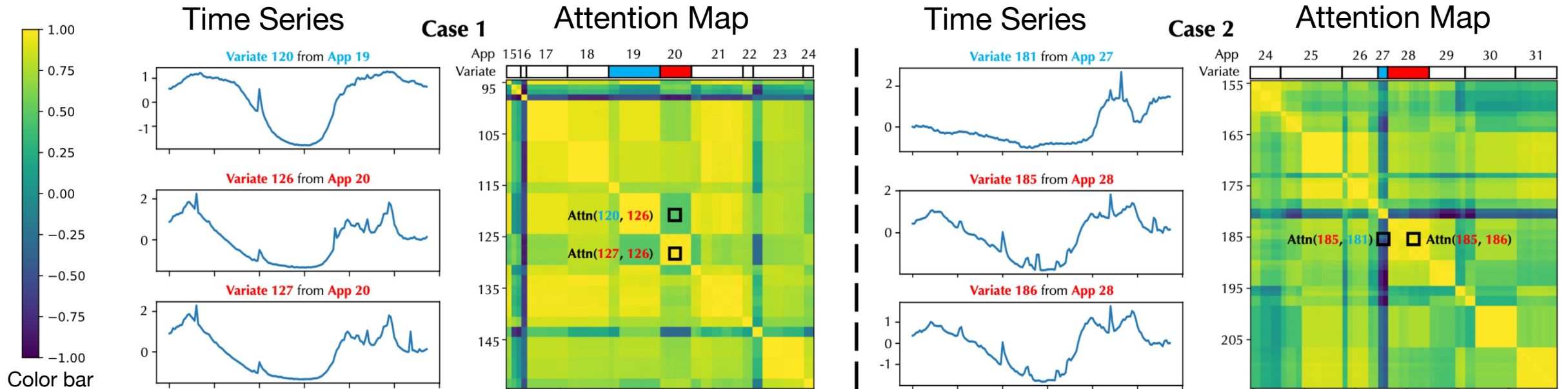
Informer
↑ 28.5%

Flowformer
↑ 16.8%

Flashformer
↑ 32.2%

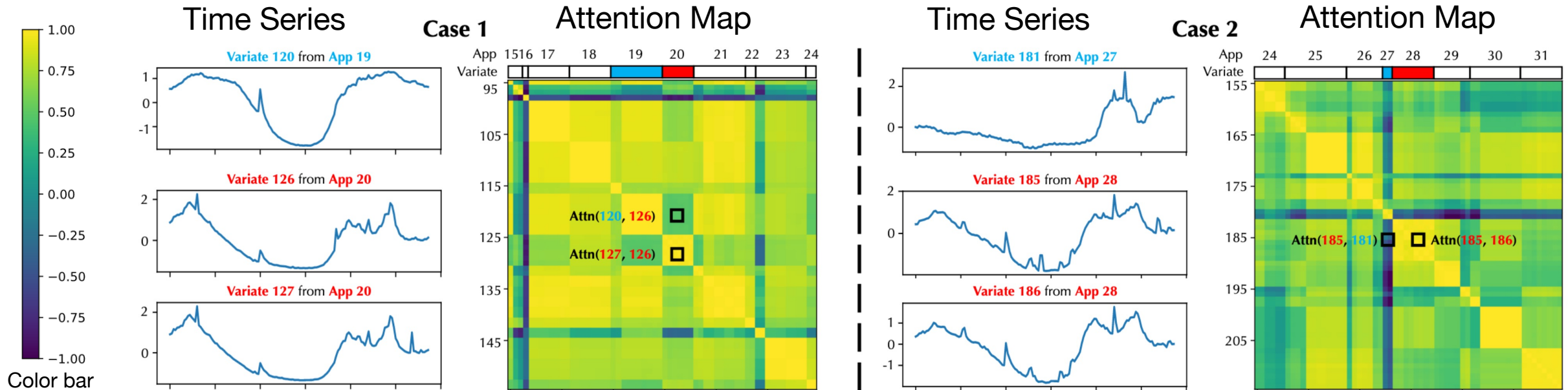
- Inverting can consistently improve various Transformers
- Take advantage of booming efficient attention mechanisms

Multivariate Correlations



Market Dataset: each variate represents the monitored series of a service interface of a kind

Multivariate Correlations



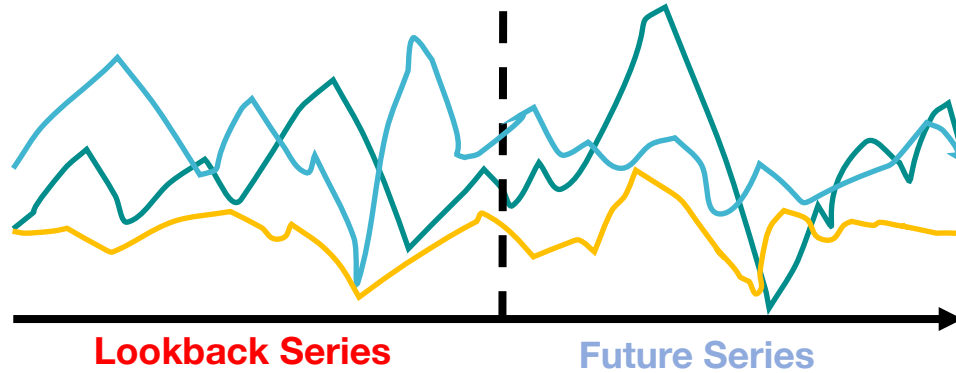
Market Dataset: each variate represents the monitored series of a service interface of a kind

- Partitions in the learned attention map, indicating the grouping of variates
- The learned attention map reveals the correlations between the variates

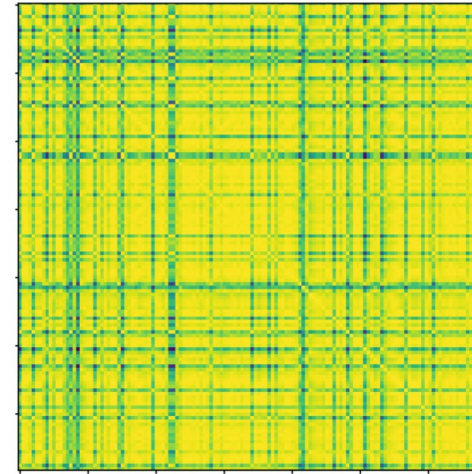


Multivariate Correlations

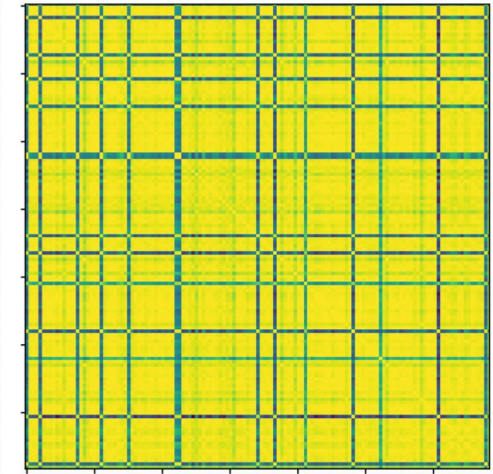
Solar-Energy Dataset: distinct multivariate correlations in the lookback and future series



Lookback Correlations



Future Correlations



Calculated from raw series

$$\rho_{xy} = \frac{\sum_i (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_i (x_i - \bar{x})^2} \sqrt{\sum_i (y_i - \bar{y})^2}}$$



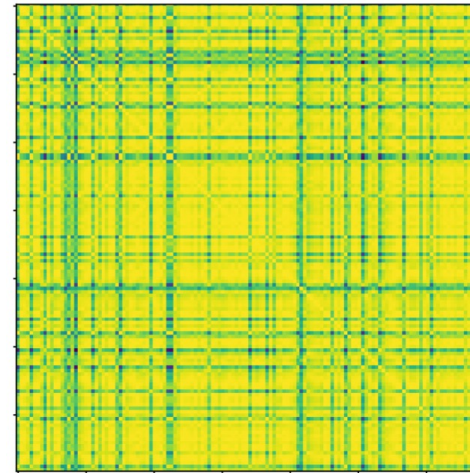
Multivariate Correlations

Solar-Energy Dataset: distinct variate correlations in the lookback and future series

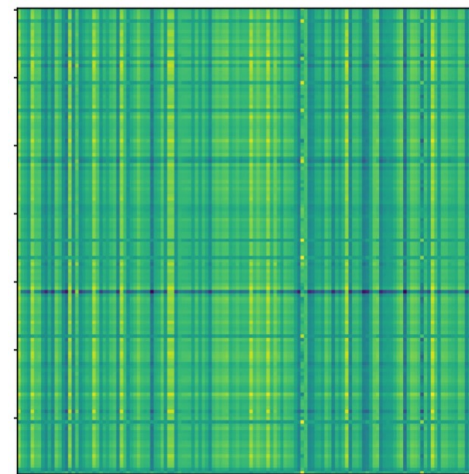
Attention map can reflect the correlation between the variates

In the shallow layer, the map share similarities to the correlations of lookback series

Lookback Correlations



$$\rho_{xy} = \frac{\sum_i (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_i (x_i - \bar{x})^2} \sqrt{\sum_i (y_i - \bar{y})^2}}$$



Score Map of Layer 1

Learned by iTransformer

$$\mathbf{A}_{i,j} = (\mathbf{QK}^\top / \sqrt{d_k})_{i,j} \propto \mathbf{q}_i^\top \mathbf{k}_j$$

Multivariate Correlations



Solar-Energy Dataset: distinct variate correlations in the lookback and future series

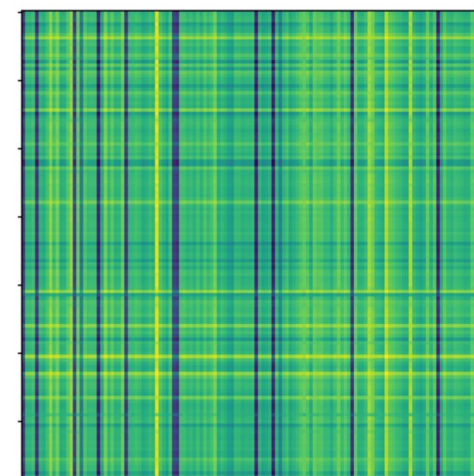
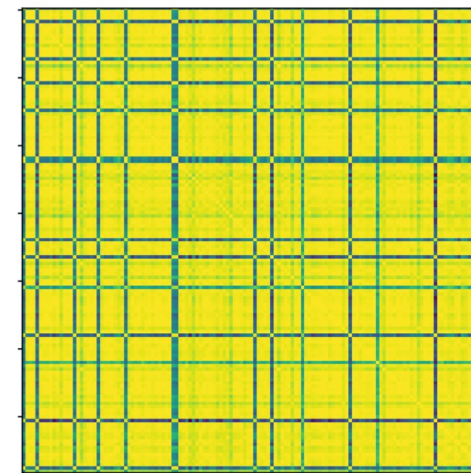
Attention map reflect the correlation between the variates

In the deep layer, the map share similarities to the correlations of future series

$$\rho_{xy} = \frac{\sum_i (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_i (x_i - \bar{x})^2} \sqrt{\sum_i (y_i - \bar{y})^2}}$$

$$\mathbf{A}_{i,j} = (\mathbf{Q}\mathbf{K}^\top / \sqrt{d_k})_{i,j} \propto \mathbf{q}_i^\top \mathbf{k}_j$$

Future Correlations



Score Map of Layer L

Learned by iTransformer



Multivariate Correlations

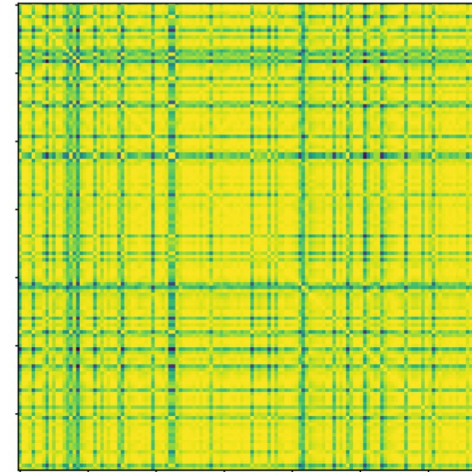
Solar-Energy Dataset: distinct variate correlations in the lookback and future series

Attention scores reflect the correlation between the variates

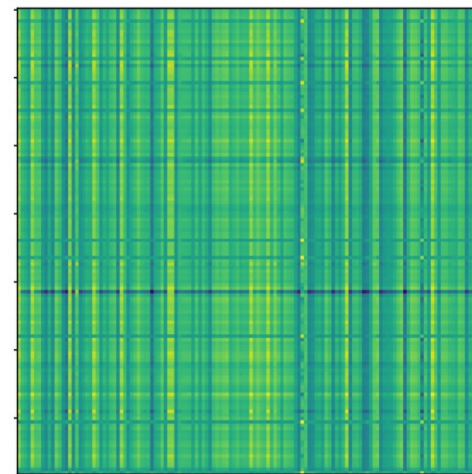
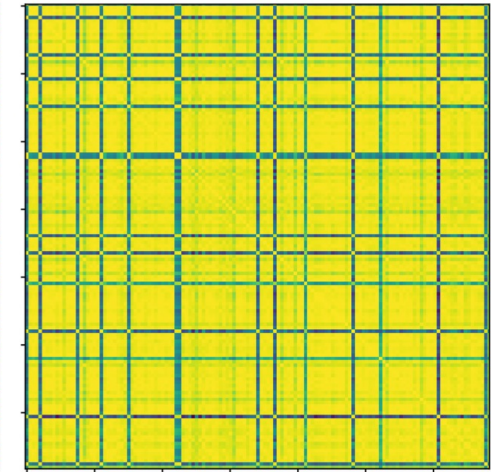
Inverting empowers

- Attention: Interpretable variate correlating
- FFN & LN: Encoding Variate Tokens and decoding them for the prediction

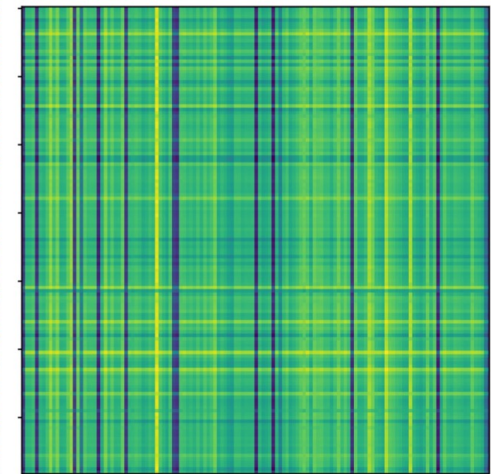
Lookback Correlations



Future Correlations



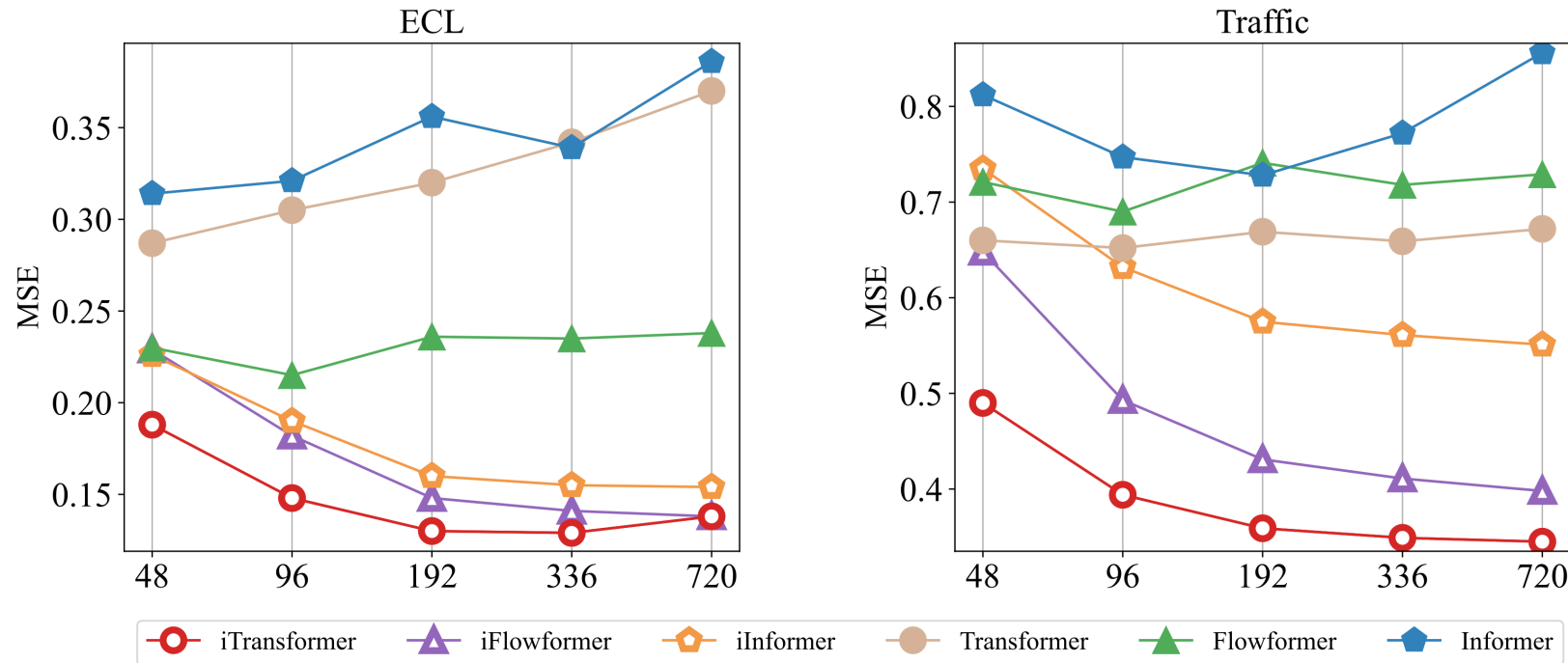
Score Map of Layer 1



Score Map of Layer L



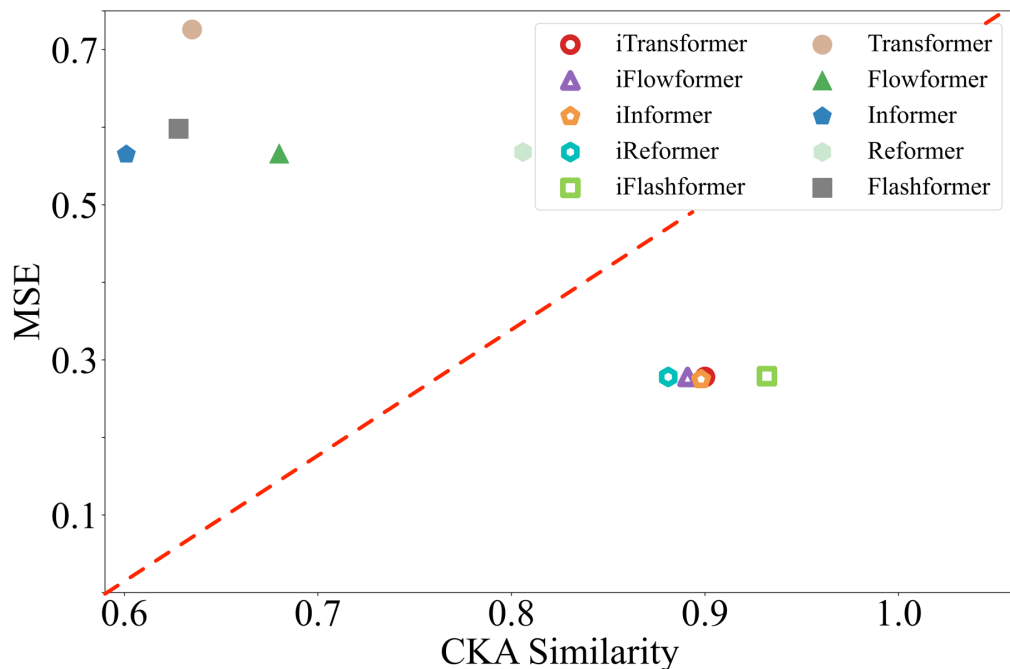
Prolonged Lookback Length



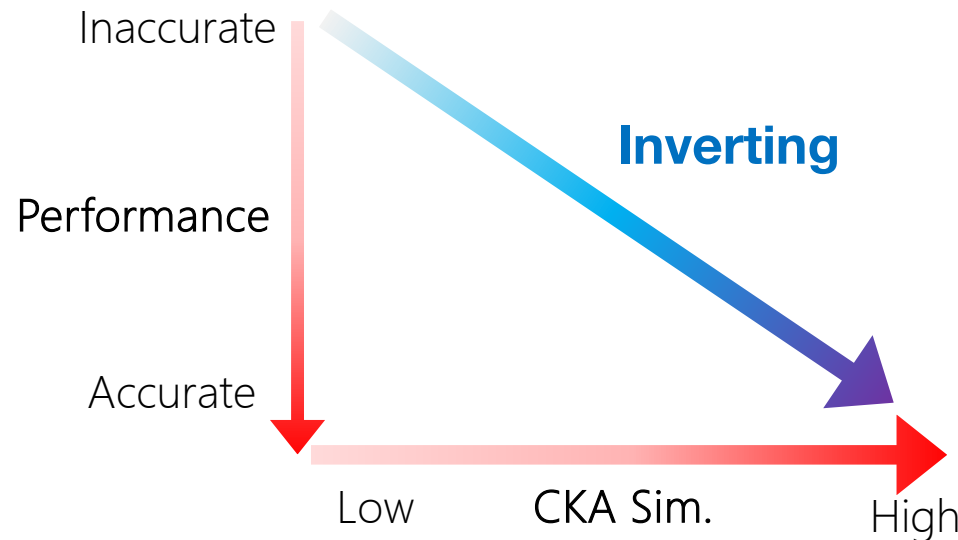
Previous work found that Transformer-based forecasters does not necessarily improve with enlarged lookback window

Performance of iTransformer is generally improving with more lookback observations

Representation Analysis



Forecasting Performance V.S Centered Kernel Alignment



Previous work demonstrated that time series forecasting, as a low-level generative task, prefers the higher CKA similarity

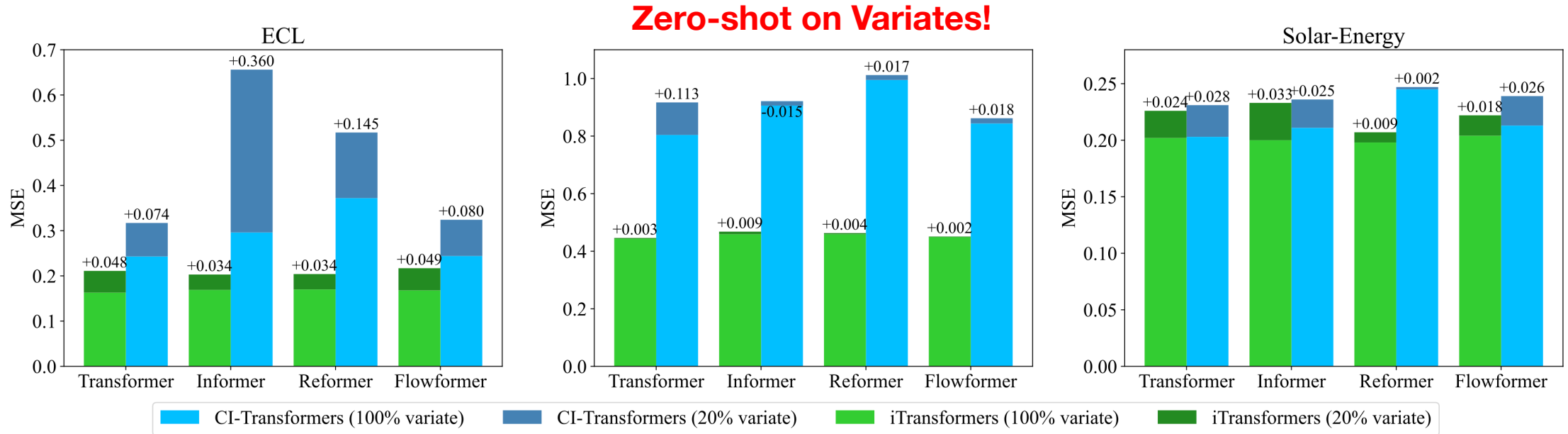
Inverting learns favored series representations and thus achieves more accurate predictions.



Variate Generalization

Based on the **independent embedding** of Variate Tokens

iTransformer can forecast with arbitrary numbers of variates during inference



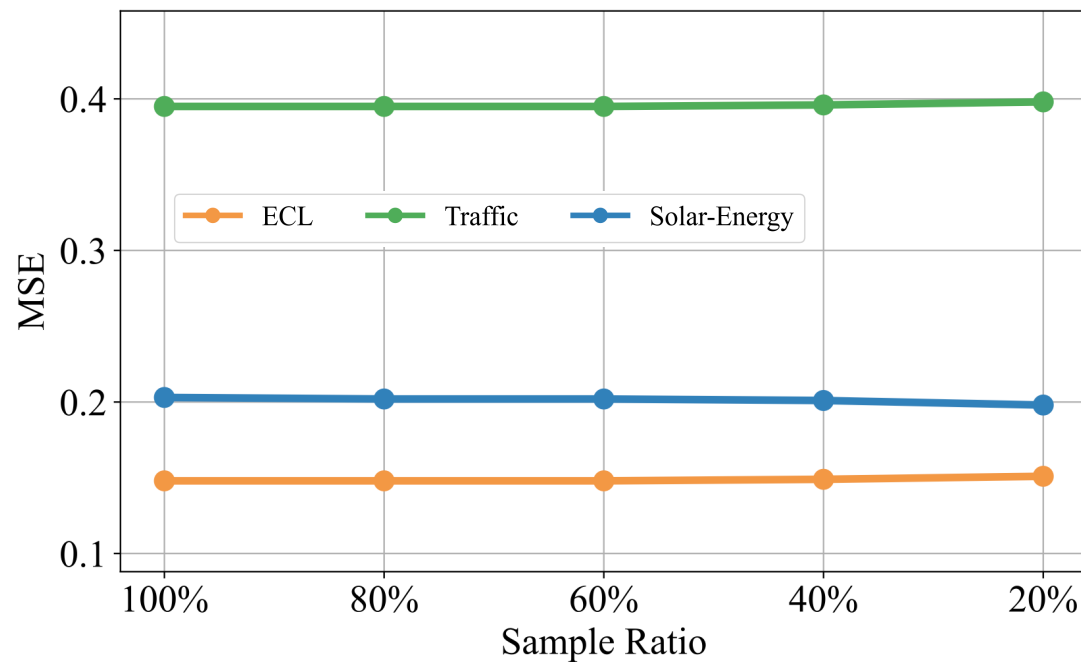
Similar to Channel Independence

iTransformers can be trained on partial variables and generalize well on unseen variates

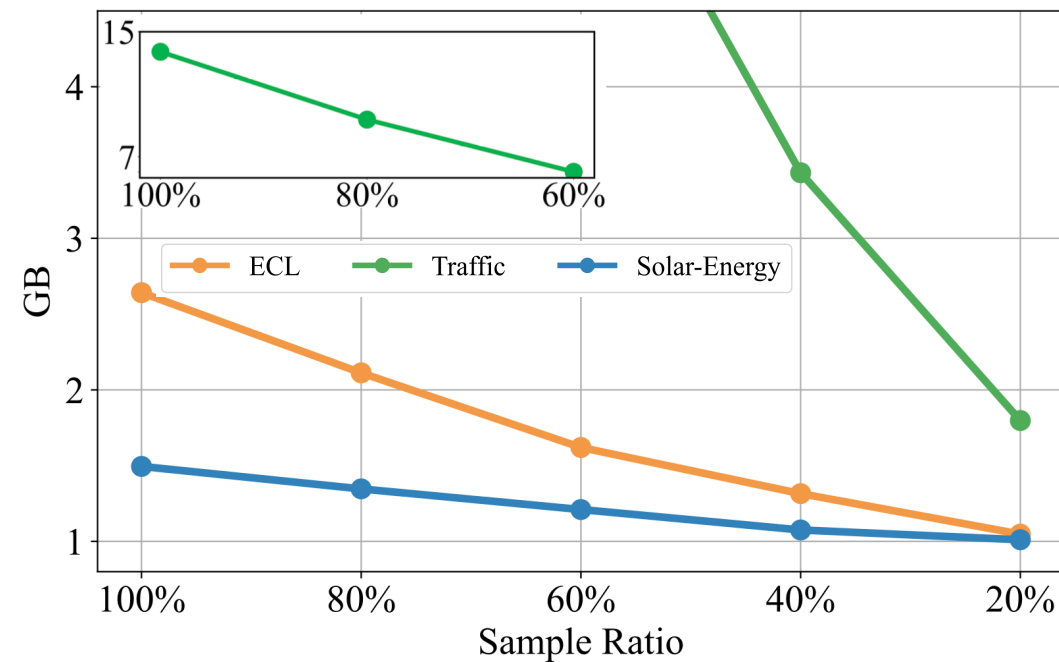
Efficient Training



Performance



Memory Footprint

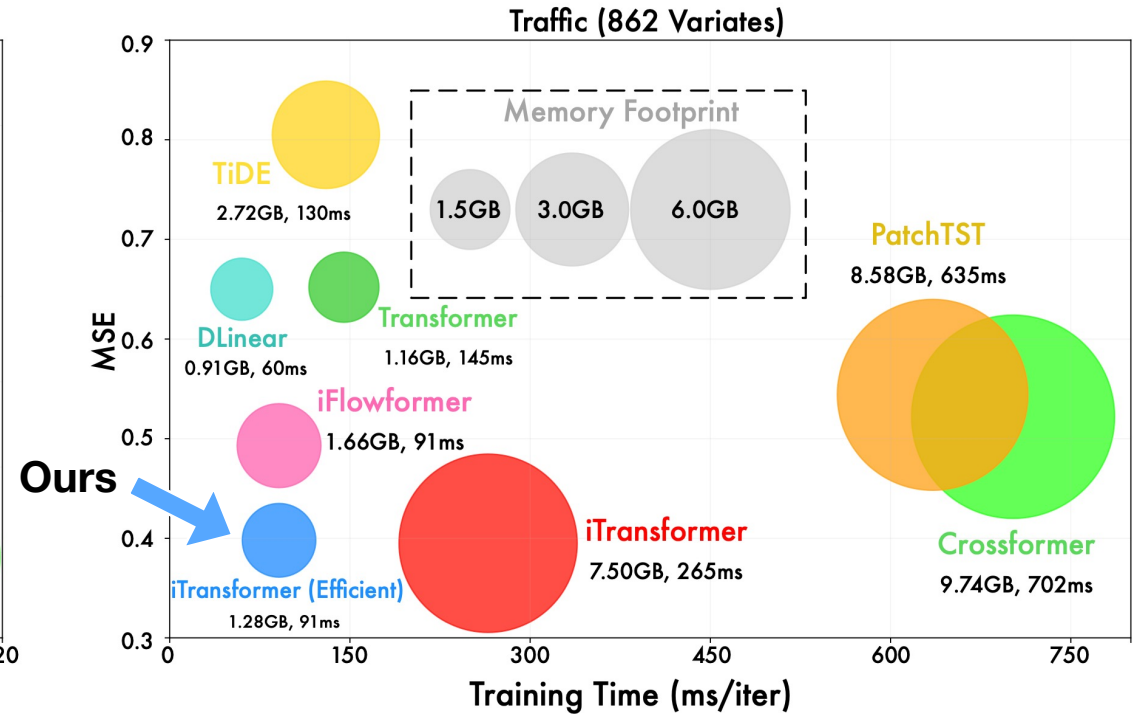
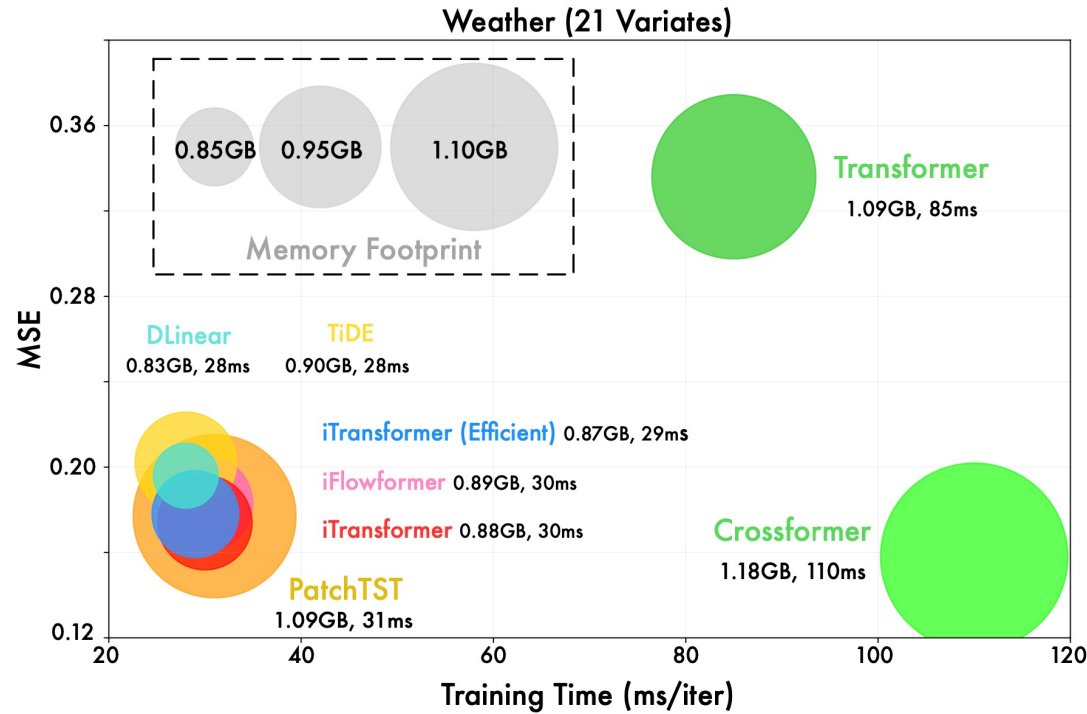


Based on the Variate Generalization Capability

We proposed an Efficient Training Strategy that trains sampled variates in each batch

Performance remains stable while memory footprints can be cut off significantly

Efficiency



- iTransformer exceeds other Transformers in datasets with a small number of variates
- Via Efficient Training, iTransformer shows strength in both Performance/Efficiency



Thank You!

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Code and datasets are available at <https://github.com/thuml/iTransformer>