



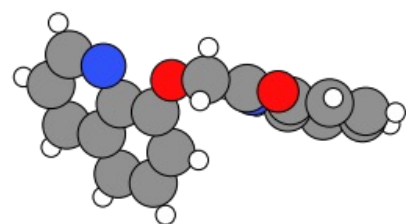
# Gradual Optimization Learning for Conformational Energy Minimization

Artem Tsypin et al.

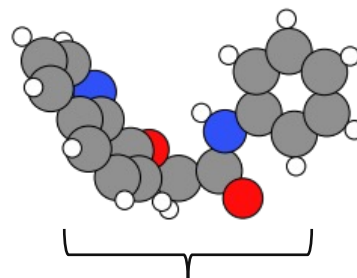
# Low-energy conformations

- Finding low-energy conformations is crucial in computer-aided drug design
- Important molecular properties that define a molecule's medicinal potential are estimated in low-energy conformations

- The transition of a molecule from any given conformation to a low-energy conformation is known as relaxation or geometry optimization



geometry optimization



Low-energy conformation

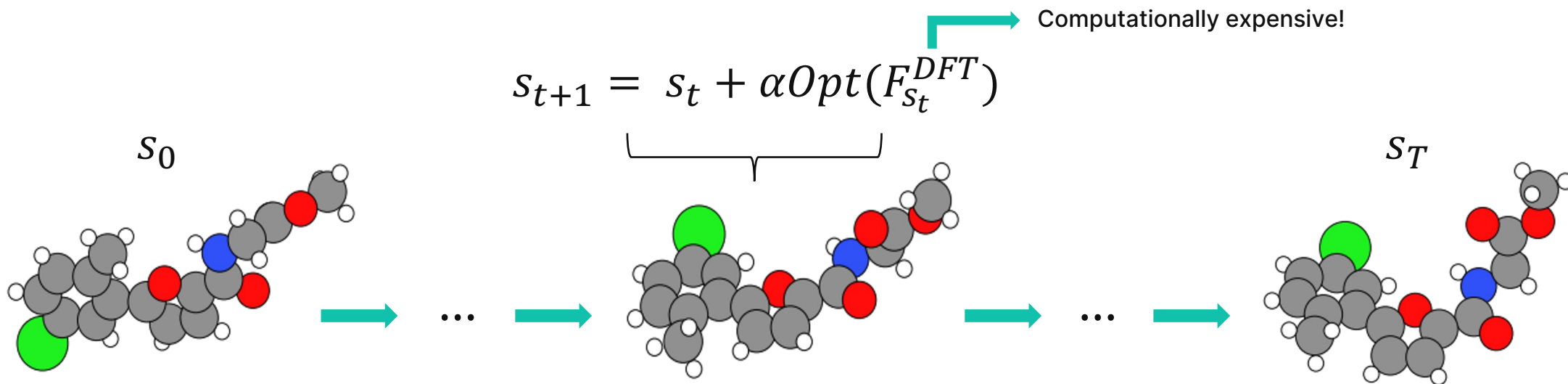
physical simulator,  
neural network, ...



Energy of HOMO  
Energy of LUMO  
Gap  
Dipole moment  
Internal energy  
Heat capacity  
...

# Traditional methods for geometry optimization

- We denote the  $t$ -th conformation in the optimization trajectory as  $s_t = \{X_t, z\}$ , where  $X_t$  is the matrix of atoms' coordinates, and  $z$  is the vector of atomic numbers
- Traditional methods iteratively optimize the geometry using interatomic forces  $F_{s_t}$  as anti-gradients
- To obtain reasonably accurate interatomic forces, we employ DFT-based physical simulators<sup>[1]</sup>
- Can scale as  $O(N^4)$ , where  $N$  is the number of electrons in the system



[1] Smith, Daniel GA, et al. "PSI4 1.4: Open-source software for high-throughput quantum chemistry." The Journal of chemical physics 152.18 (2020).

# Neural network potentials for geometry optimization

- A Neural Network Potential (**NNP**) is trained to predict energy based on conformation:

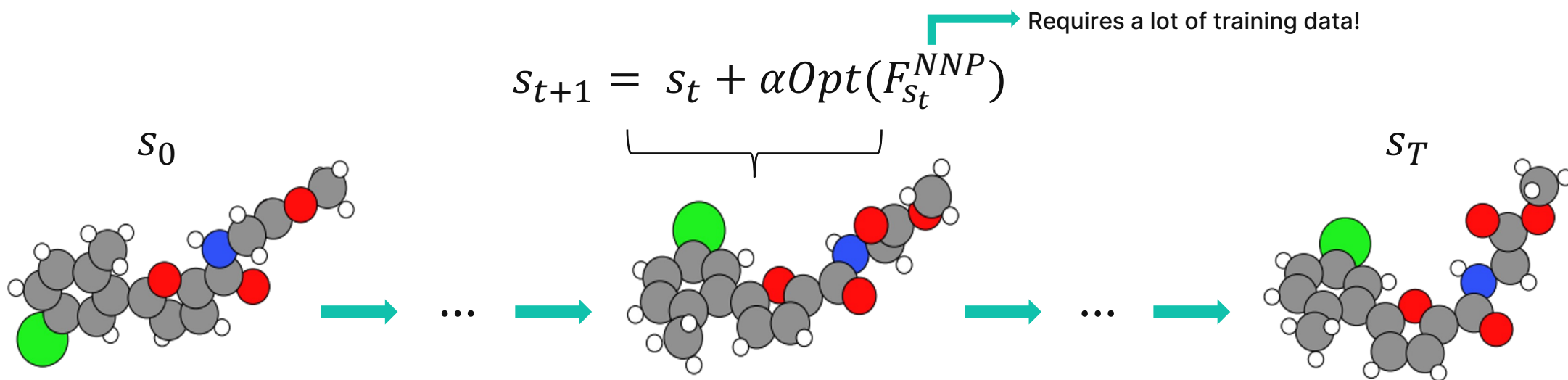
$$E_{s_t}^{NNP} = f(s_t; \theta)$$

- To predict the forces we take the gradient of the energy w.r.t. atoms' coordinates<sup>[1, 2]</sup>:

$$F_{s_t}^{NNP} = - \frac{\partial f(s_t; \theta)}{\partial X_t}$$

- Iterative optimization with NNP is ~2000 times faster in terms of wall-time

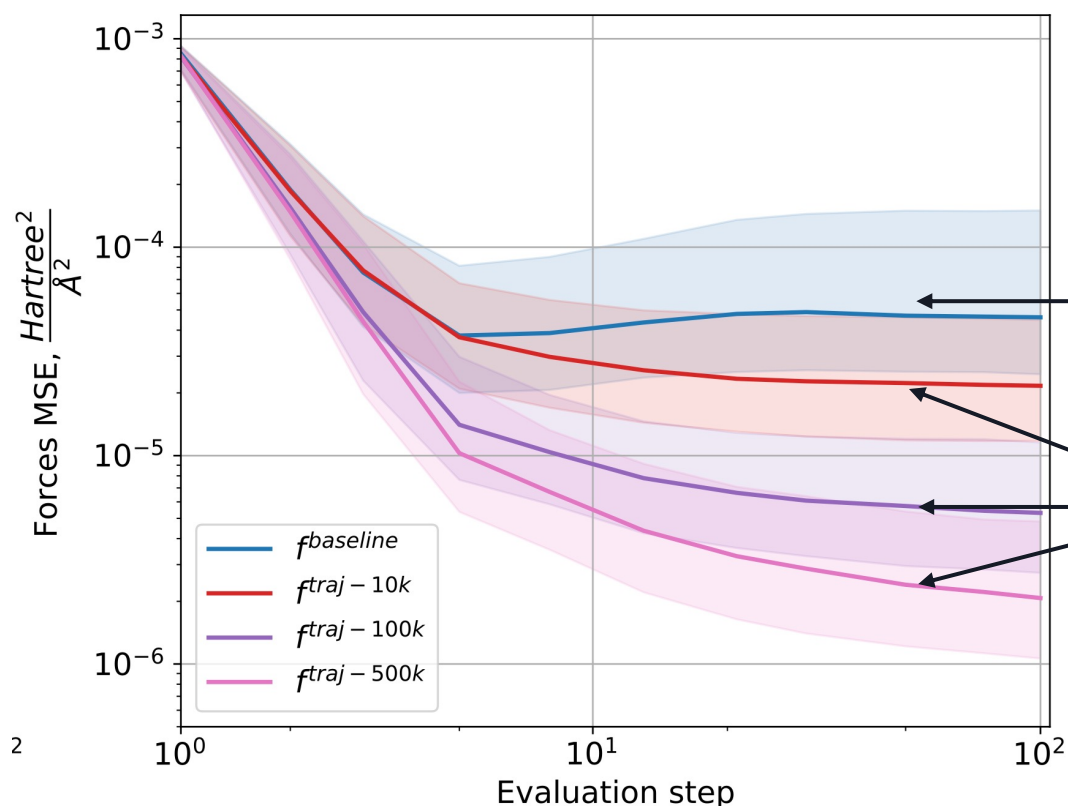
- Requires a lot of data!



[1] Schütt, Kristof T., et al. "SchNet—a deep learning architecture for molecules and materials." The Journal of Chemical Physics 148.24 (2018).

[2] Schütt, Kristof, Oliver Unke, and Michael Gastegger. "Equivariant message passing for the prediction of tensorial properties and molecular spectra." International Conference on Machine Learning. PMLR, 2021.

# Training NNPs for the task of geometry optimization



→ NNPs trained on publicly available datasets<sup>[1, 2]</sup> suffer from a distribution shift when used in the optimization task

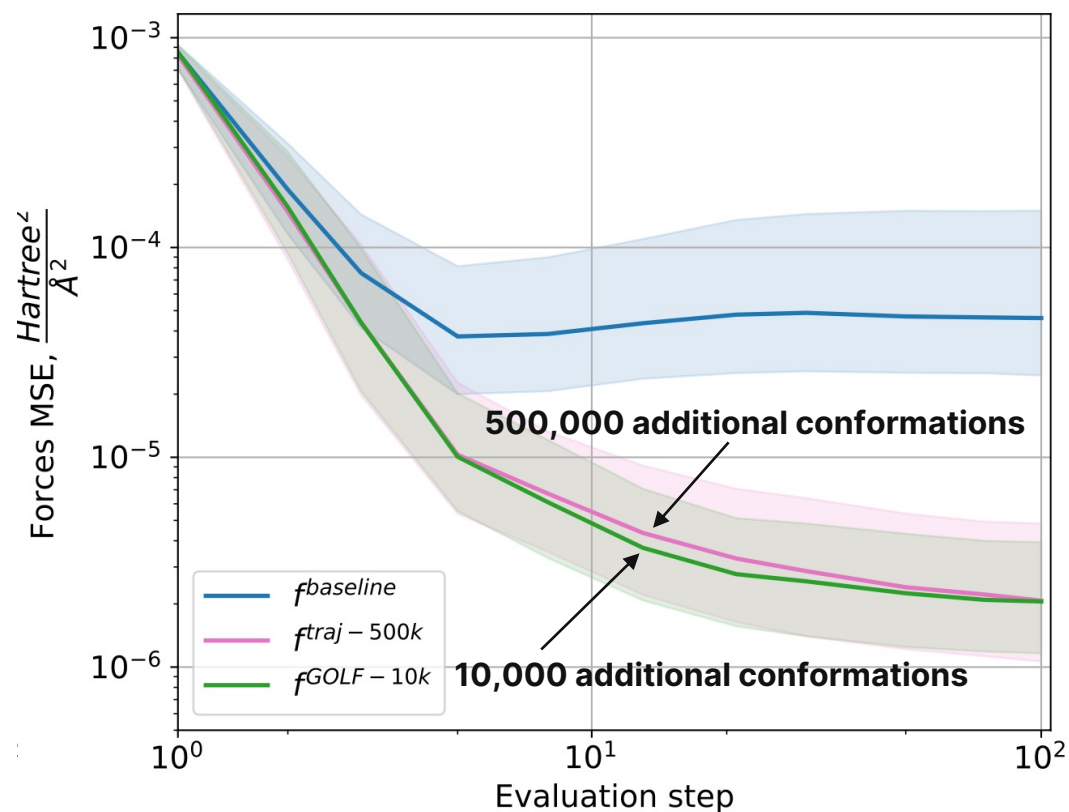
→ To show this, we run iterative optimization with NNP and evaluate forces predicted at each step with DFT-based oracle. The prediction error increases throughout the relaxation

→ To alleviate the distribution shift, we extend the training dataset with ground-truth optimization trajectories obtained with DFT-based oracle. The prediction error gradually decreases with the amount of additional training data

[1] Khrabrov, Kuzma, et al. "nabladft: Large-scale conformational energy and hamiltonian prediction benchmark and dataset." Physical Chemistry Chemical Physics 24.42 (2022): 25853-25863.

[2] Eastman, Peter, et al. "Spice, a dataset of drug-like molecules and peptides for training machine learning potentials." Scientific Data 10.1 (2023): 11.

# Motivation and the goal



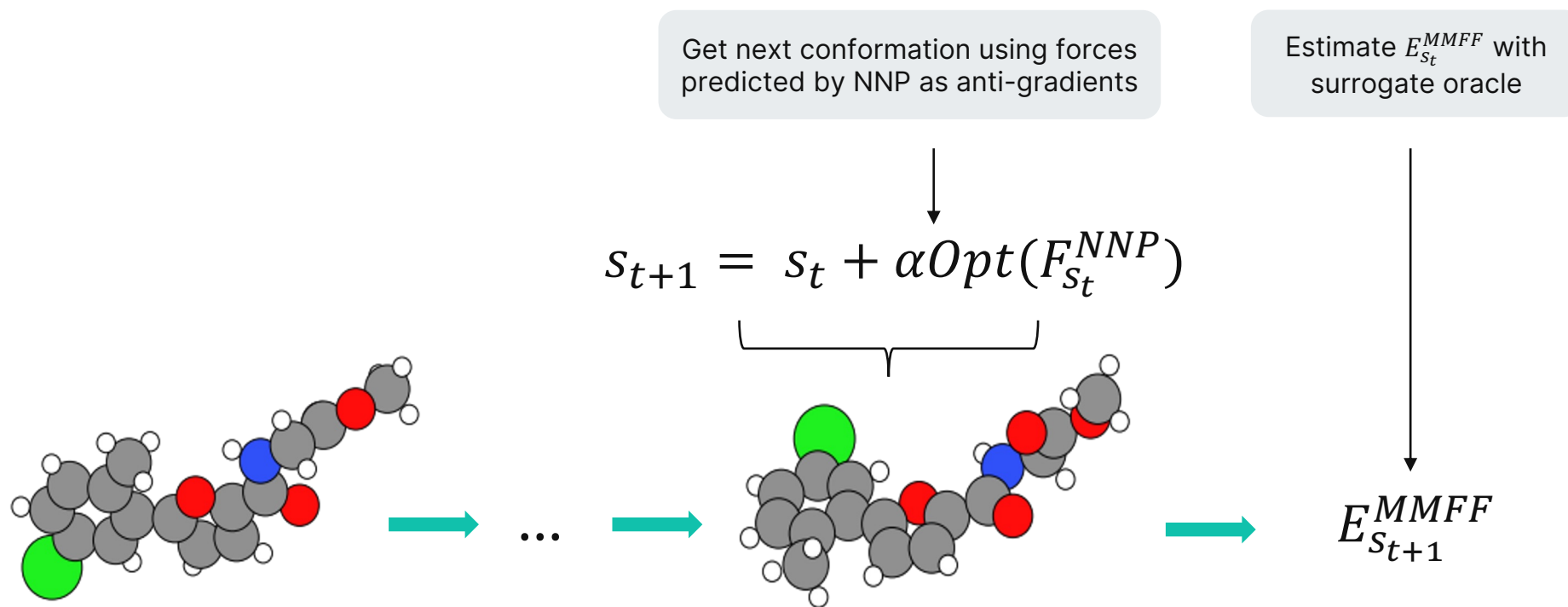
- We show that it requires approximately 500,000 additional conformations to reach optimization quality comparable with the DFT-based oracle
- For the molecules from the nablaDFT dataset and our selected physical simulator, this amounts to about **9 CPU-years of compute**



Our primary goal is to reduce the amount of additional data while maintaining optimization quality comparable to the DFT-based physical simulator.

# GOLF

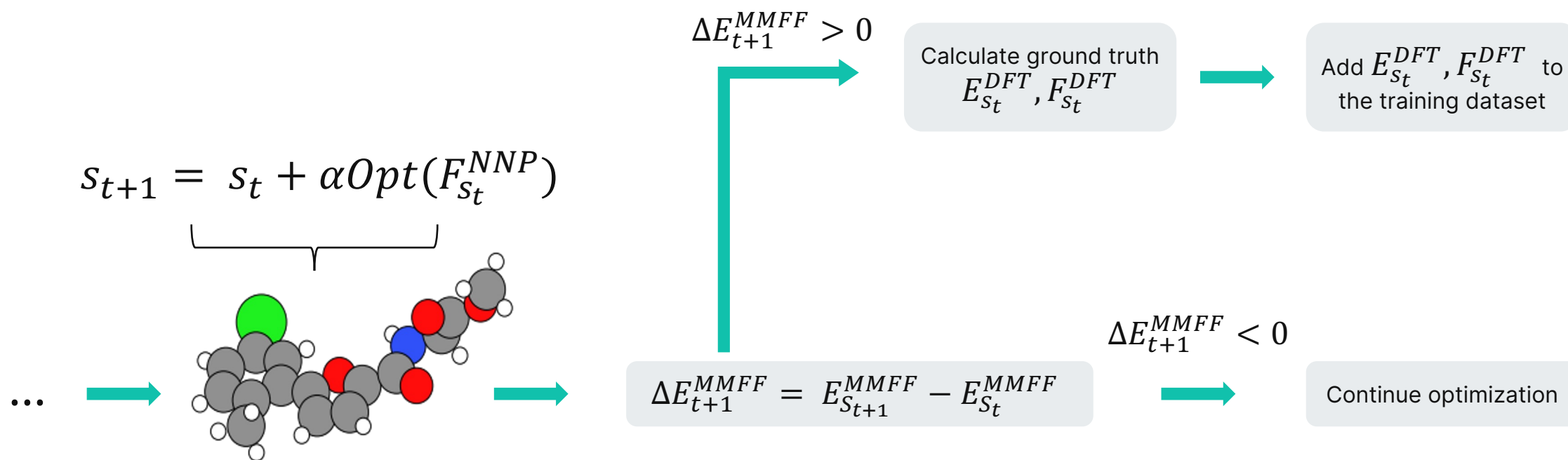
We use the NNP to perform iterative optimization.  
After every step, we estimate the energy in  $s_{t+1}$  with the **surrogate oracle** (RDKit's<sup>[1]</sup> MMFF in our work).



[1] RDKit: Open-source cheminformatics. <https://www.rdkit.org>

# GOLF

Then we estimate whether the energy has decreased. If the energy decreased, we continue the optimization; otherwise, we consider the NNP's prediction of interatomic forces incorrect and add the conformation from the previous step to the training dataset.





# Results

→ We test the algorithm on a subset of nabraDFT<sup>[1]</sup> dataset  $\mathcal{D}^{test}$  (~20000 conformations for ~10000 molecules)

→ We use the following metrics:

$$E^{residual} = \frac{1}{|\mathcal{D}^{test}|} \sum_{s \in \mathcal{D}^{test}} E_{S_T}^{DFT} - E_{optimal}^{DFT}$$

Chemical  
precision,  
kcal/mol

$$pct_{success} = \frac{1}{|\mathcal{D}^{test}|} \sum_{s \in \mathcal{D}^{test}} I[(E_{S_T}^{DFT} - E_{optimal}^{DFT}) < 1]$$

→ Training NNPs with GOLF reduces the amount of additional conformations required to match the optimization quality of DFT from 500,000 to 10,000

	$\overline{E}^{res}_T$ (kcal/mol) ↓	$\overline{pct}_T$ (%) ↑
$f^{baseline}$	8.6	8.2
$f^{traj-500k}$	0.5	73.4
$f^{GOLF-10k}$	0.5	77.3



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