Loss Landscape and Generalization

Huanran Chen



Flatness strongly correlated with generalization



- Measured by F-norm/Spectral norm of Hessian matrix
- Intuition: Assume that the testing loss is shifted from the training loss.
 Sharp minima will have a larger testing error.

[Li, Hao, et al. "Visualizing the loss landscape of neural nets." Nips, 2018.]

From observation to methodology

• ALRS scheduler

Using large learning rate. Decrease as slow as possible.

- Backbone
- e.g., use residual connection/wider toeplitz matrix.

Regularization

Perturbing the gradient to prevent convergence into local optima.



[Chen, Huanran, et al. "Bootstrap Generalization Ability from Loss Landscape Perspective." ECCVW, 2022.]

Inspiration to my research

- Observing the phenomenon
- e.g. decreasing the loss slowly results in better generalization.
- Make some conjectures
- e.g. flatness result in better generalization
- More rigorous theoretical explanations
- e.g. assuming the testing loss is shifted from training loss...
- Validating the explanations
- e.g. measuring the spectral norm of Hessian of different optima
- Proposing new methods
- e.g. new backbone, new scheduler.

Rethinking Model Ensemble in Transfer-based Adversarial Attacks

ICLR 2024

Adversarial examples raise security concerns





Dong et al. How Robust is Google's Bard Against Adversarial Image Attack. NeurIps Workshop, 2023 Huang et al. T-sea: Transfer-based self-ensemble attack on object detection. CVPR, 2023

One definition of adversarial examples



Goodfellow et al. Explaining and Harnessing Adversarial Examples. ICLR, 2015

Transfer attacks



Sitawarin et al. Defending Against Transfer Attacks From Public Models. arxiv, 2023.

We formulate the transfer attack as generalization problem

• Target: attacking all the deployed models

 $\min_{\boldsymbol{x}} \mathbb{E}_{f \in \mathcal{F}}[L(f(\boldsymbol{x}), y)], \text{ s.t. } \|\boldsymbol{x} - \boldsymbol{x}_{nat}\|_{\infty} \leq \epsilon,$

where F is the set of all models.

- However, we can only access to surrogate models F_t: $\frac{1}{n}\sum_{i=1}^{n}L(f_i(x),y)$
- Similar to ERM, a generalization bound given by Hoeffding inequality:

$$\forall f \in \mathcal{F}, \ R_{\mathcal{D}}(f) \leq \widehat{R}_{S}(f) + \sqrt{\frac{\log c + \log \frac{1}{\sigma}}{N}},$$

Inspiration by generalization bound

• Increasing number of models and number of images



Huang et al. T-SEA: Transfer-based Self-Ensemble Attack on Object Detection. CVPR, 2023 Xie et al. Mitigating Adversarial Effects Through Randomization. CVPR, 2019

This work, a new conjecture from loss landscape

Closeness of landscape result in better generalization



(a) Not flat and not close

(b) Flat and not close

(c) Not flat and close

(d) Flat and close

Closeness and generalization

 Conjecture: closeness and flatness are both 2-order information.A way to connect them with generalization: Tayler expansion of testing loss at the optimum of each surrogate models:

$$\mathbb{E}_{f_i \in \mathcal{F}}\left[L(f_i(\boldsymbol{p}_i), y) + \frac{1}{2}(\boldsymbol{x} - \boldsymbol{p}_i)^\top \boldsymbol{H}_i(\boldsymbol{x} - \boldsymbol{p}_i)\right].$$

• Decompose them by assuming the indenpendence:

Proof.

$$\begin{split} \mathbb{E}[(\boldsymbol{x} - \boldsymbol{p}_{i})^{\top} \boldsymbol{H}_{i}(\boldsymbol{x} - \boldsymbol{p}_{i})] \\ = \mathbb{E}[\|(\boldsymbol{x} - \boldsymbol{p}_{i})\|_{p} \|\boldsymbol{H}_{i}(\boldsymbol{x} - \boldsymbol{p}_{i})\|_{q}] \quad (\text{where } \frac{1}{p} + \frac{1}{q} = 1) \\ \leq \mathbb{E}[\|(\boldsymbol{x} - \boldsymbol{p}_{i})\|_{p} \|\boldsymbol{H}_{i}\|_{r,q} \|(\boldsymbol{x} - \boldsymbol{p}_{i})\|_{r}] \\ = \mathbb{E}[\|\boldsymbol{H}_{i}\|_{r,q}] \mathbb{E}[\|(\boldsymbol{x} - \boldsymbol{p}_{i})\|_{p} \|(\boldsymbol{x} - \boldsymbol{p}_{i})\|_{r}], \end{split}$$

where $\|\cdot\|_{r,q}$ is an induced matrix norm.

Special case: When p = q = r = 2, we have

 $\mathbb{E}[(\boldsymbol{x} - \boldsymbol{p}_i)^\top \boldsymbol{H}_i(\boldsymbol{x} - \boldsymbol{p}_i)] \leq \mathbb{E}[\|\boldsymbol{H}_i\|_2]\mathbb{E}[\|(\boldsymbol{x} - \boldsymbol{p}_i)\|_2^2],$ where $\|\boldsymbol{H}_i\|_2$ is the spectral norm of \boldsymbol{H}_i . As we also have $\|\boldsymbol{H}_i\|_2 \leq \|\boldsymbol{H}_i\|_F$, we obtain $\mathbb{E}[(\boldsymbol{x} - \boldsymbol{p}_i)^\top \boldsymbol{H}_i(\boldsymbol{x} - \boldsymbol{p}_i)] \leq \mathbb{E}[\|\boldsymbol{H}_i\|_F]\mathbb{E}[\|(\boldsymbol{x} - \boldsymbol{p}_i)\|_2^2],$ where $\|\boldsymbol{H}_i\|_F$ is the Frobenius norm of \boldsymbol{H}_i .

Better generalization with closeness

- Now: closeness of testing landscape strongly correlated with testing loss.
- We need prove: better training closeness, better testing closeness.
- i.e. closeness generalize better than directly training by loss function.
- Intuition: closeness is measured by the distance of optimum. If optimum is some distribution with variance, then the probability of generalizing better can be bound by this variance.

Theorem A.2. Denote F(m,n) as *F*-distribution with parameter *m* and *n*, $F_{\alpha}(m,n)$ as $P(F(m,n) > \alpha)$, For any two different optimum of ensemble model c^1 and c^2 and corresponding $\hat{\sigma}_1 = \frac{1}{n} \sum_{\boldsymbol{p}_i \in O_{c_t^1}} (\boldsymbol{p}_i - c_t^1)^2$, $\hat{\sigma}_2 = \frac{1}{n} \sum_{\boldsymbol{p}_i \in O_{c_t^2}} (\boldsymbol{p}_i - c_t^2)^2$, there is $F_{\frac{\hat{\sigma}_1}{\hat{\sigma}_2}}(n-1,n-1)$ probability that:

$$\mathbb{E}_{\boldsymbol{p}_{i} \in O_{\boldsymbol{c}^{1}}}[\|(\boldsymbol{c}_{1} - \boldsymbol{p}_{i})\|^{2}] \leq \mathbb{E}_{\boldsymbol{p}_{i} \in O_{\boldsymbol{c}^{2}}}[\|(\boldsymbol{c}_{2} - \boldsymbol{p}_{i})\|^{2}].$$
(A.1)

Encouraging flatness

$$\min[\max_{\|\boldsymbol{\delta}\|_{\inf} < \epsilon} L(\boldsymbol{x} + \boldsymbol{\delta}) - L(\boldsymbol{x})].$$

$$\begin{split} \boldsymbol{\delta} &= \arg \max_{\|\boldsymbol{\delta}\|_{\inf} < \epsilon} L(\boldsymbol{x} + \boldsymbol{\delta}) \\ &\approx \arg \max_{\|\boldsymbol{\delta}\|_{\inf} < \epsilon} L(\boldsymbol{x}) + \boldsymbol{\delta}^{\top} \operatorname{sign}(\nabla_{\boldsymbol{x}} L(\boldsymbol{x})) \\ &= \arg \max_{\|\boldsymbol{\delta}\|_{\inf} < \epsilon} \boldsymbol{\delta}^{\top} \operatorname{sign}(\nabla_{\boldsymbol{x}} L(\boldsymbol{x})) \\ &= \epsilon \cdot \operatorname{sign}(\nabla_{\boldsymbol{x}} L(\boldsymbol{x})). \end{split}$$

Algorithm 2 MI-SAM

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Rec	puire: natural image x_{nat} , label y, perturbation budget ϵ ,
	$\mathcal{F}_t = \{f_i\}_{i=1}^n$, decay factor μ , step sizes r, β and α .
1:	Initialize: $\boldsymbol{m} = 0, \boldsymbol{x}_0 = \boldsymbol{x}_{nat};$
2:	for $t = 0$ to $T - 1$ do
3:	Calculate $g = \nabla_{\boldsymbol{x}} L(\frac{1}{n} \sum_{i=1}^{n} f_i(\boldsymbol{x}_t), y);$
4:	Update \boldsymbol{x}_t by $\boldsymbol{x}_t^r = \hat{\operatorname{clip}}_{\boldsymbol{x}_{nat},\epsilon}(\boldsymbol{x}_t + r \cdot \operatorname{sign}(\boldsymbol{g}));$
5:	Calculate $g = \nabla_{\boldsymbol{x}} L(\frac{1}{n} \sum_{i=1}^{n} f_i(\boldsymbol{x}_t^r), y);$
6:	Update \boldsymbol{x}_t^r by $\boldsymbol{x}_t^f = \operatorname{clip}_{\boldsymbol{x}_{nat},\epsilon}(\boldsymbol{x}_t^r - \beta \cdot \operatorname{sign}(\boldsymbol{g}));$
7:	Calculate the update $g = \boldsymbol{x}_t^f - \boldsymbol{x}_t$;
8:	Update momentum $\boldsymbol{m} = \boldsymbol{\mu} \cdot \boldsymbol{m} + \boldsymbol{g}$;
9:	update \boldsymbol{x}_{t+1} by $\boldsymbol{x}_{t+1} = \operatorname{clip}_{\boldsymbol{x}_{nat}, \boldsymbol{\epsilon}}(\boldsymbol{x}_t + \alpha \cdot (\boldsymbol{m}));$
10:	end for
11:	Return: x_T .

$$\nabla_{\boldsymbol{x}} L(\boldsymbol{x} + \boldsymbol{\delta}) = \nabla_{\boldsymbol{x} + \boldsymbol{\delta}} L(\boldsymbol{x} + \boldsymbol{\delta}) \cdot \nabla_{\boldsymbol{x}} (\boldsymbol{x} + \boldsymbol{\delta}) = \nabla_{\boldsymbol{x} + \boldsymbol{\delta}} L(\boldsymbol{x} + \boldsymbol{\delta}) + \nabla_{\boldsymbol{x} + \boldsymbol{\delta}} L(\boldsymbol{x} + \boldsymbol{\delta}) \cdot \nabla_{\boldsymbol{x}} \boldsymbol{\delta}.$$

$$\overset{\boldsymbol{x}_{t}^{r}}{\underset{\boldsymbol{x}_{t} \\ \nabla_{\boldsymbol{x}} L}} \overset{\boldsymbol{x}_{t}^{r}}{\underset{\boldsymbol{x}_{t+1}}{}} \overset{\boldsymbol{x}_{t}^{r}}{\underset{\boldsymbol{x}_{t+1}}{}} \overset{\boldsymbol{x}_{t}^{r}}{\underset{\boldsymbol{x}_{t+1}}{}} \overset{\boldsymbol{x}_{t}^{r}}{\underset{\boldsymbol{x}_{t+1}}{}} \overset{\boldsymbol{x}_{t}^{r}}{\underset{\boldsymbol{x}_{t} \\ \boldsymbol{x}_{t} \\ \boldsymbol{$$

Encouraging closeness

• How to optimize this: $\frac{1}{n}\sum_{\boldsymbol{p}_i\in O_{\boldsymbol{c}_t}} \|(\boldsymbol{c}_t-\boldsymbol{p}_i)\|_2^2$

Using Cauchy-Swartz theorem, we can get:

$$\sum_{i=1}^{n} \|(\boldsymbol{c} - \boldsymbol{p}_i)\|_2^2 = \sum_{i=1}^{n} (\boldsymbol{H}_i^{-1} \boldsymbol{g}_i)^\top (\boldsymbol{H}_i^{-1} \boldsymbol{g}_i) = \sum_{i=1}^{n} \|(\boldsymbol{H}_i^{-1} \boldsymbol{g}_i)\|_2^2 \le \sum_{i=1}^{n} \|\boldsymbol{H}_i^{-1}\|_F^2 \|\boldsymbol{g}_i\|_2^2.$$

The treatment of $\|\boldsymbol{H}_i\|_F$ has already been discussed in Appendix B.1. In this section, we set M as the maximum value of $\|\boldsymbol{H}_i^{-1}\|_F^2$, which allows us to obtain the following result:

$$\sum_{i=1}^{n} \|(\boldsymbol{c} - \boldsymbol{p}_{i})\|_{2}^{2} \leq M \sum_{i=1}^{n} \boldsymbol{g}_{i}^{\top} \boldsymbol{g}_{i} = M \left[(\sum_{i=1}^{n} \boldsymbol{g}_{i})^{2} - 2 \sum_{i=1}^{n} \sum_{j=1}^{i-1} \boldsymbol{g}_{i} \boldsymbol{g}_{j} \right].$$

Since c is the optimal solution for the ensemble model, we have $(\sum_{i=1}^{n} g_i)^2 = 0$. Consequently, our final training objective is:

$$\max \sum_{i=1}^{n} \sum_{j=1}^{i-1} \boldsymbol{g}_i \boldsymbol{g}_j, \qquad (A.2)$$

How to encourage cosine similarity

$$\begin{split} \frac{\partial}{\partial x} \frac{g_{i}g_{j}}{\|g_{i}\|_{2}\|g_{j}\|_{2}} &= \frac{H_{i}}{\|g_{i}\|_{2}} \left(I - \frac{g_{i}g_{i}^{\top}}{\|g_{i}\|_{2}}\right) \frac{g_{j}}{\|g_{j}\|_{2}} + \frac{H_{j}}{\|g_{j}\|_{2}} \left(I - \frac{g_{j}g_{j}^{\top}}{\|g_{j}\|_{2}}\right) \frac{g_{i}}{\|g_{i}\|_{2}}, \\ \frac{\partial}{\partial x} \frac{g_{i}g_{j}}{\|g_{i}\|_{2}\|g_{j}\|_{2}} &\approx \frac{H_{i}}{\|g_{i}\|_{2}} \frac{g_{j}}{\|g_{j}\|_{2}} + \frac{H_{j}}{\|g_{j}\|_{2}} \frac{g_{i}}{\|g_{i}\|_{2}}, \\ \mathbb{E}\left[\frac{\partial}{\partial x} \frac{g_{i}g_{j}}{\|g_{i}\|_{2}\|g_{j}\|_{2}}\right] &\approx 2\mathbb{E}\left[\frac{H_{i}}{\|g_{i}\|_{2}} \frac{g_{j}}{\|g_{j}\|_{2}}\right], \\ g_{i}' &= g_{i} + H_{i}(x^{i} - x^{1}) \\ &= g_{i} - \beta H_{i} \sum_{j=1}^{i-1} \frac{g_{j}'}{\|g_{j}'\|_{2}} \\ = g_{i} - \beta H_{i} \sum_{j=1}^{i-1} \frac{g_{j} + o(\beta)}{\|g_{j} + o(\beta)\|_{2}} \\ &= \mathbb{E}[\beta \sum_{i=1}^{n} \frac{g_{i}}{\|g_{i}\|_{2}} - \beta^{2} \sum_{i=1}^{n} \sum_{j=1}^{i-1} H_{i} \frac{g_{j}}{\|g_{i}\|_{2}} + \sum_{i=1}^{n} O(\beta^{3}) \\ &= \beta\mathbb{E}[\sum_{i=1}^{n} \frac{g_{i}}{\|g_{i}\|_{2}}] - \frac{\beta^{2}}{2}\mathbb{E}[\sum_{i,j}^{i$$

Combination of closeness and flatness

Algorithm 3 MI-CSE algorithm

Require: natural image x_{nat} , label y, perturbation budget ϵ , iteration $\mathcal{F}_t = \{f_i\}_{i=1}^n$, decay factor μ , step sizes β and α . 1: Initialize: m = 0, inner momentum $\hat{m} = 0$, $x_0 = x_{nat}$; 2: for t = 0 to T - 1 do for i = 1 to n do 3: Calculate $\boldsymbol{g} = \nabla_{\boldsymbol{x}} L(f_i(\boldsymbol{x}_t^{i-1}), y);$ 4: Update inner momentum by $\hat{\boldsymbol{m}} = \mu \cdot \hat{\boldsymbol{m}} + \frac{\boldsymbol{g}}{\|\boldsymbol{g}\|_2};$ 5: Update \boldsymbol{x}_{t}^{i} by $\boldsymbol{x}_{t}^{i} = \operatorname{clip}_{\boldsymbol{x}_{nat},\epsilon}(\boldsymbol{x}_{t}^{i-1} - \beta \cdot \hat{\boldsymbol{m}});$ 6: 7: end for Calculate the update $\boldsymbol{g} = \boldsymbol{x}_t^n - \boldsymbol{x}_t$; 8: Update momentum $m = \mu \cdot m + q$; 9: update \boldsymbol{x}_{t+1} by $\boldsymbol{x}_{t+1} = \operatorname{clip}_{\boldsymbol{x}_{nat}, \boldsymbol{\epsilon}}(\boldsymbol{x}_t + \alpha \cdot \operatorname{sign}(\boldsymbol{m}));$ 10: 11: end for 12: Return: x_T .

Algorithm 1 MI-CWA algorithm **Require:** natural image x_{nat} , label y, perturbation budget ϵ , ite $\mathcal{F}_t = \{f_i\}_{i=1}^n$, decay factor μ , step sizes r, β and α . 1: Initialize: m = 0, inner momentum $\hat{m} = 0$, $x_0 = x_{nat}$; 2: for t = 0 to T - 1 do Calculate $\boldsymbol{g} = \nabla_{\boldsymbol{x}} L(\frac{1}{n} \sum_{i=1}^{n} f_i(\boldsymbol{x}_t), y);$ 3: Update \boldsymbol{x}_t by $\boldsymbol{x}_t^0 = \operatorname{clip}_{\boldsymbol{x}_{nat},\epsilon}(\boldsymbol{x}_t + r \cdot \operatorname{sign}(\boldsymbol{g}));$ 4: 5: for i = 1 to n do Calculate $\boldsymbol{g} = \nabla_{\boldsymbol{x}} L(f_i(\boldsymbol{x}_t^{i-1}), y);$ 6: 7: Update inner momentum by $\hat{\boldsymbol{m}} = \mu \cdot \hat{\boldsymbol{m}} + \frac{\boldsymbol{g}}{\|\boldsymbol{g}\|_2}$; Update \boldsymbol{x}_{t}^{i} by $\boldsymbol{x}_{t}^{i} = \operatorname{clip}_{\boldsymbol{x}_{nat},\epsilon}(\boldsymbol{x}_{t}^{i-1} - \beta \cdot \hat{\boldsymbol{m}});$ 8: 9: end for 10: Calculate the update $\boldsymbol{g} = \boldsymbol{x}_t^n - \boldsymbol{x}_t$; 11: Update momentum $m = \mu \cdot m + q$; update \boldsymbol{x}_{t+1} by $\boldsymbol{x}_{t+1} = \operatorname{clip}_{\boldsymbol{x}_{nat},\epsilon}(\boldsymbol{x}_t + \alpha \cdot \operatorname{sign}(\boldsymbol{m}));$ 12: 13: end for 14: Return: \boldsymbol{x}_T .

Method	Backbone	FGSM	BIM	MI	DI	TI	VMI	SVRE	PI	SSA	RAP	MI-SAM	MI-CSE	MI-CWA	VMI-CWA	SSA-CWA
	AlexNet	76.4	54.9	73.2	78.9	78.0	83.3	82.5	78.2	89.0	82.9	81.0	93.6	94.6	95.9	96.9
	VGG-16	68.9	86.1	91.9	92.9	82.5	94.8	96.4	93.1	97.7	93.1	95.6	99.6	99.5	99.9	99.9
	GoogleNet	54.4	76.6	89.1	92.0	77.8	94.2	95.7	91.0	97.2	90.4	94.4	98.8	99.0	99.8	99.8
	Inception-V3	54.5	64.9	84.6	89.0	75.7	91.1	92.6	85.9	95.6	85.0	89.2	97.3	97.2	98.9	99.6
	ResNet-152	54.5	96.0	96.6	93.8	87.8	97.1	99.0	97.2	97.6	95.3	97.9	99.9	99.8	100.0	100.0
	DenseNet-121	57.4	93.0	95.8	93.8	88.0	96.6	99.1	96.9	98.2	94.1	98.0	99.9	99.8	99.9	100.0
	SqueezeNet	85.0	80.4	89.4	92.9	85.8	94.2	96.1	92.1	97.2	92.1	94.1	99.1	99.3	99.6	99.8
Normal	ShuffleNet-V2	81.2	65.3	79.9	85.7	78.2	89.9	90.3	85.8	93.9	89.3	87.9	97.2	97.3	98.7	98.8
Normai	MobileNet-V3	58.9	55.6	71.8	78.6	74.5	87.3	80.6	77.1	91.4	81.1	80.7	94.6	95.7	97.8	98.1
	EfficientNet-B0	50.8	80.2	90.1	91.5	76.8	94.6	96.7	93.3	96.9	91.4	95.2	98.8	98.9	99.7	99.9
	MNasNet	64.1	80.8	88.8	91.5	75.5	94.1	94.2	90.3	97.2	92.5	94.3	99.1	98.7	99.6	99.9
	RegNetX-400MF	57.1	81.1	89.3	91.2	82.4	95.3	95.4	91.0	97.4	90.8	93.9	98.9	99.4	99.8	99.9
	ConvNeXt-T	39.8	68.6	81.6	85.4	56.2	92.4	88.2	85.7	93.1	86.8	90.1	96.2	95.4	97.8	98.1
	ViT-B/16	33.8	35.0	59.2	66.8	56.9	81.8	65.8	64.5	83.0	66.7	68.9	89.6	89.6	92.3	90.0
	Swin-S	34.0	48.2	66.0	74.2	40.9	84.2	73.4	69.1	85.2	72.2	75.1	88.6	87.6	91.6	88.4
	MaxViT-T	31.3	49.7	66.1	73.2	32.7	83.5	71.1	70.1	85.2	69.7	75.6	85.8	85.9	88.1	86.1
FGSMAT	Inception-V3	53.9	43.4	55.9	61.8	66.1	72.3	66.8	61.1	84.3	69.6	64.5	89.6	89.6	91.5	92.7
EnsAT	IncRes-V2	32.5	28.5	42.5	52.9	58.5	66.4	46.8	45.3	76.1	48.6	47.9	78.2	79.1	83.2	84.1
FastAT	ResNet-50	45.6	41.6	45.7	47.1	49.3	51.4	51.0	33.1	34.7	56.5	50.6	75.0	74.6	73.5	70.4
PGDAT	ResNet-50	36.3	30.9	37.4	38.0	43.9	47.1	43.9	23.0	25.3	51.0	43.9	73.5	73.6	72.7	66.8
PGDAT	ResNet-18	46.8	41.0	45.7	47.7	50.7	48.9	48.5	39.0	41.1	55.5	48.0	68.4	69.5	69.2	65.9
	WRN-50-2	27.7	20.9	27.8	31.3	37.0	36.2	33.0	17.9	18.7	41.2	33.4	64.4	64.8	63.1	55.6
$PGDAT^{\dagger}$	XCiT-M12	23.0	16.4	22.8	25.4	29.4	33.4	30.2	11.9	13.1	44.7	31.8	77.5	77.8	75.1	66.3
	XCiT-L12	19.8	15.7	19.8	21.7	26.9	30.8	26.7	11.5	11.5	41.3	26.9	71.0	71.7	67.5	59.4
HGD	IncRes-V2	36.0	78.0	76.2	88.4	73.5	92.0	85.5	79.2	93.9	79.0	87.9	95.6	95.6	98.2	98.7
R&P	ResNet-50	67.9	95.8	96.3	96.2	91.5	98.7	99.9	98.2	98.9	95.3	98.8	99.7	99.8	99.8	100.0
Bit	ResNet-50	69.1	97.0	97.3	96.1	94.1	99.0	99.9	98.8	99.5	97.1	99.4	100.0	100.0	100.0	100.0
JPEG	ResNet-50	68.5	96.0	96.3	95.4	93.5	98.6	99.5	97.6	99.2	96.0	99.4	99.8	99.9	100.0	100.0
RS	ResNet-50	60.9	96.1	95.6	95.6	89.9	96.9	99.3	96.4	98.1	95.9	98.1	100.0	100.0	100.0	100.0
NRP	ResNet-50	36.6	88.7	72.4	63.1	71.7	89.0	91.2	81.3	92.8	33.3	87.3	88.1	86.8	33.1	85.4
DiffPure	ResNet-50	50.9	68.5	76.0	82.0	86.3	92.6	87.1	87.7	93.4	79.6	85.6	93.3	93.1	97.3	97.5

Amazing performance

Table 2: mAP (%, \downarrow) of black-box detectors under attacks on INRIA dataset. The universal adversarial patch trained on YOLOv3 and YOLOv5 by Adam-CWA achieves the lowest mAPs on multiple modern detectors (9.85 on average) with large margins.

Method	Surrogate	YOLOv2	YOLOv3	YOLOv3-T	YOLOv4	YOLOv4-T	YOLOv5	FasterRCNN	SSD	Avg.
Single	YOLOv3	54.63	12.35	53.99	58.20	53.38	69.21	50.81	58.13	51.34
Single	YOLOv5	30.45	34.17	33.26	53.55	54.54	7.98	37.87	37.00	36.10
Loss Ensemble	YOLOv3+YOLOv5	25.84	8.08	38.50	47.22	43.50	19.21	34.41	35.04	31.48
Adam-CWA	YOLOv3+YOLOv5	6.59	2.32	8.44	11.07	8.33	2.06	14.41	25.56	9.85



Validation of our algorithm

- Exactly same time complexity with SGD&Adam&MI
- But much higher performance



CWA is a universal optimizer

```
Algorithm 4 Generalized Common Weakness Algorithm (CWA)
Require: image x_0; label y; total iteration T; loss function L, model set
  \mu; inner optimizer \beta, reverse optimizer r, outer optimizer \alpha
  Calculate the number of models n
  for t = 1 to T do
     o = copy(x)
     # first step
      calculate the gradient \boldsymbol{g} = \nabla_{\boldsymbol{x}} L(\frac{1}{n} \sum_{i=1}^{n} f_i(\boldsymbol{x}), y)
     update x by r.step(-g)
     # second step
     for j = 1 to n do
         pick the jth model f_i
         calculate the gradient \boldsymbol{g} = \nabla_{\boldsymbol{x}} L(f_i(\boldsymbol{x}), y)
         update x by \beta.step(\frac{g}{\|g\|_2})
      end for
     calculate the update in this iteration q = o - x
     update \boldsymbol{x} by \alpha.step(\boldsymbol{q})
  end for
  return x
```

Interesting experiments



(a) YOLOv3



(b) YOLOv5



(c) Loss Avg



(d) Adam-CWA



(e) Strongest

• $1:\beta/2$ is the best tradeoff



How Robust is Google's Bard to Adversarial Image Attacks?

NeurIPSW 2023





$$\max_{\boldsymbol{x}} \sum_{i=1}^{N} \|f_i(\boldsymbol{x}) - f_i(\boldsymbol{x}_{nat})\|_2^2, \quad \text{s.t.} \ \|\boldsymbol{x} - \boldsymbol{x}_{nat}\|_{\infty} \leq \epsilon,$$

$$\max_{\boldsymbol{x}} \sum_{i=1}^{N} \sum_{t=1}^{L} \log p_{g_i}(y_t | \boldsymbol{x}, \boldsymbol{p}, y_{< t}), \quad \text{s.t. } \|\boldsymbol{x} - \boldsymbol{x}_{nat}\|_{\infty} \le \epsilon$$

Bard



View other drafts

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The image shows two men standing in front of a house. The men are both wearing casual clothes. The man on the left is wearing a blue t-shirt and jeans. The man on the right is wearing a gray shirt and shorts. Both men are smiling and looking at the camera.

The house in the background is a two-story house with a white exterior. The house has a black front door and a black roof. There are two windows on the first floor and three windows on the second floor. There is a tree in the front yard of the house.

The overall mood of the image is happy and relaxed. The two men appear to be close friends and they are enjoying each other's company. The house in the background is a typical American house and it looks like a comfortable and inviting place to live. Describe this image

1



View other drafts

The image is a close-up of a painting of a woman's face. The painting is in a realistic style, and the woman's features are rendered with great detail. Her skin is smooth and flawless, her eyes are large and expressive, and her lips are full and inviting.

V

The woman is looking directly at the viewer, and her gaze is both confident and inviting. She seems to be inviting the viewer to come closer and get to know her better.

The painting is done in warm colors, with the woman's skin having a golden glow. This gives the painting a sense of warmth and intimacy.

Overall, the image is a beautiful and evocative portrait of a woman. The painter has captured

GPT-4



Describe this image

\$

The image shows a pair of hands creating a heart shape. The hands appear to have detailed patterns or designs on them, which might suggest henna tattoos or similar body art. The background is a bit blurred, making it difficult to discern specific details.



Describe this image

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The image appears to be a highly stylized or abstract representation. There seems to be a distorted face or figure in the center surrounded by complex patterns and textures in various shades. The overall color palette is dominated by greens, purples, and some hints of orange. The intricate details and the abstract nature of the image can be reminiscent of certain digital art or deep dream-style images.

New Bing



- ✓ Analyzing the image: Privacy blur hides faces from Bing chat
- ✓ Searching for: cat face mosaic filter
- ✓ Searching for: cat face mosaic filter
- Generating answers for you...

The image you sent is a **low resolution image of a cat's face** with a **mosaic or tile effect filter** applied to it. The filter has different shades of brown and black. The cat's eyes are closed and its nose and mouth are visible. The background is dark and indistinguishable.

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- Analyzing the image: Privacy blur hides faces from Bing chat
- ✓ Searching for: cat dog bed painting
- Searching for: cat dog bed painting
- ✓ Generating answers for you...

This is a low resolution image of a **cat and a dog lying on a bed**. The cat is a tabby and is lying on top of the dog. The dog is a black and tan dachshund. The bed has a colorful quilt on it with a geometric pattern. The background is a wall with a window and a lamp. The image has a filter applied to it that makes it look like a painting.

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ERINE 文心一言

	Attack Success Rate
GPT-4	45%
Bing Chat	26%
ERNIE Bot	86%



Summary

Formulate the transfer attack as generalization problem

Identify closeness, introduce flatness

Proving that closeness is another good properties for generalization

Proposing CSE, CWA optimizer/attacker

♦ Successfully attack GPT-4 and Bard