

Entropy is not Enough for Test-Time Adaptation: From the Perspective of Disentangled Factors

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Test-Time Adaptation

- Requirements
 - The pre-trained model \mathcal{M}_s trained on the source (training) data \mathcal{D}_s
 - Target (test) data $\mathcal{D}_t = \{x_t\}$
- Goal
 - Using \mathcal{M}_s and the **stream** of \mathcal{D}_t , obtain the best performance on target domain
- Constraints
 - No source (train) data \mathcal{D}_s
 - Efficiency (memory, runtime)

Test-Time Adaptation (cont'd)

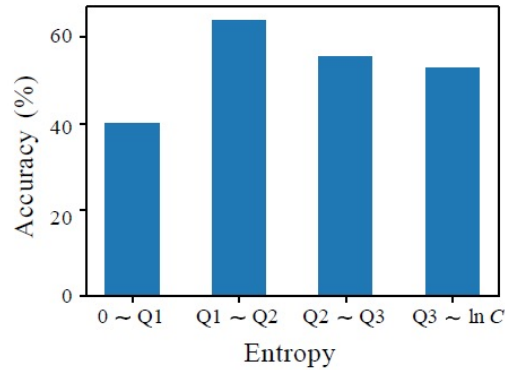
- TTA cannot access whole target data \mathcal{D}_t before adaptation.
 - Impossible to estimate the target distribution
 - Prone to inaccurate prediction in the early stage
 - Error accumulation!
 - Need to adapt using samples that have a lower likelihood of causing error
 - Sample filtering and reweighting with confidence metric!

Previous work

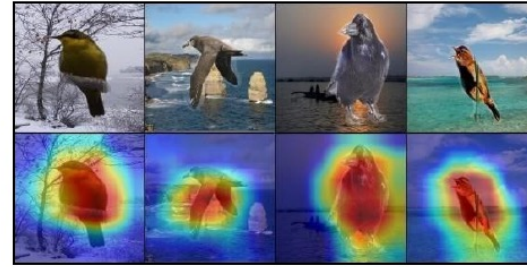
- TENT (ICLR 2021 spotlight)
 - Entropy minimization loss
 - **No filtering**
- EATA (ICML 2022)
 - TENT + filtering + regularization
 - Reliable (**entropy**) filtering + redundant filtering
 - Fisher regularization
- SAR (ICLR 2023 oral)
 - Reliable (**entropy**) filtering + sharpness-aware entropy minimization loss

Previous work (cont'd)

- Observations

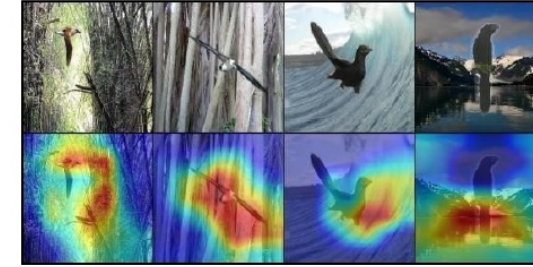


(a) Entropy level vs accuracy



Waterbirds (100%) Landbirds (100%) Waterbirds (100%) Landbirds (100%)

(b) Grad-CAM of correct samples



Waterbirds (100%) Waterbirds (100%) Landbirds (100%) Landbirds (100%)

(c) Grad-CAM of wrong samples

- The lowest entropy interval shows the lowest accuracy
 - **Unreliable!**
- Samples in 0~Q1
 - Correct samples: focus on bird (target) well
 - Wrong samples: relatively bad

Entropy is not enough for TTA!

- Entropy cannot reflect 'which part' of the image assigns low entropy.
 - If birds (object)? → good!
 - If spurious features (background)? → bad...
- Let's take 'disentangled factors' notation!

Entropy is not enough for TTA! (cont'd)

- Disentangled factors

- Disentangled latent vector $\mathbf{v}(\mathbf{x}) = (v_0(\mathbf{x}), v_1(\mathbf{x}), \dots, v_{d_v}(\mathbf{x})) \in \mathbb{R}^{d_v}$

- Each element is independent
- $\mathbf{v}(\mathbf{x})$ can perfectly reconstruct an input image \mathbf{x}
- $v_i(\mathbf{x}) \in [0,1]$: the i -th factor of \mathbf{x}

- In binary classification ($y \in \{-1, +1\}$)

- Each factor $v_i(\mathbf{x})$ has a correlation with a true label y
- Under distribution shift, the correlation can be changed!
- Define two correlations

$$- \text{corr}_i^{\text{train}} = \text{corr}(y^{\text{train}}, v_i^{\text{train}}), \text{corr}_i^{\text{test}} = \text{corr}(y^{\text{test}}, v_i^{\text{test}})$$

- Then we could divide $\mathbf{v}(\mathbf{x})$ into four partitions

$$\mathbf{v}_{pp} = \{v_i | \text{corr}_i^{\text{train}} > 0, \text{corr}_i^{\text{test}} > 0\}, \quad \mathbf{v}_{pn} = \{v_i | \text{corr}_i^{\text{train}} > 0, \text{corr}_i^{\text{test}} \leq 0\},$$

$$\mathbf{v}_{np} = \{v_i | \text{corr}_i^{\text{train}} \leq 0, \text{corr}_i^{\text{test}} > 0\}, \quad \mathbf{v}_{nn} = \{v_i | \text{corr}_i^{\text{train}} \leq 0, \text{corr}_i^{\text{test}} \leq 0\}.$$

Entropy is not enough for TTA! (cont'd)

- Assume the pretrained model \mathcal{M}_θ as a linear classifier.

Proposition 1. *Let us consider a pre-trained linear classifier \mathcal{M}_θ that uses the latent disentangled factors $\mathbf{v}(\mathbf{x})$ of sample \mathbf{x} as input. We define a **harmful** sample as one that reduces the difference in the mean logits between classes when used for adaptation. A sample $\mathbf{x} \in \mathcal{X}^{\text{test}}$ is a **harmful** sample for adaptation using entropy minimization loss if it satisfies the following condition:*

$$\hat{y}\mathbf{v}(\mathbf{x}) \cdot (\mathbb{E}_{\mathbf{x}^{\text{test}} \sim \mathcal{X}_{+1}^{\text{test}}}[\mathbf{v}(\mathbf{x}^{\text{test}})] - \mathbb{E}_{\mathbf{x}^{\text{test}} \sim \mathcal{X}_{-1}^{\text{test}}}[\mathbf{v}(\mathbf{x}^{\text{test}})]) < 0, \quad (5)$$

where $\mathcal{X}_y^{\text{test}} = \{\mathbf{x} | (\mathbf{x}, y) \in \mathcal{D}^{\text{test}}, y = y\}$, and $y \in \{1, -1\}$.

- With Proposition 1, we can explain why the samples with low entropy can be **harmful**.

Entropy is not enough for TTA! (cont'd)

- The partitions of optimal parameters θ^* for the training data

$$\begin{aligned} \mathbf{v}_{pp} &= \{v_i | \text{corr}_i^{\text{train}} > 0, \text{corr}_i^{\text{test}} > 0\}, & \mathbf{v}_{pn} &= \{v_i | \text{corr}_i^{\text{train}} > 0, \text{corr}_i^{\text{test}} \leq 0\}, & \theta_{pp}^*, \theta_{pn}^* &> 0 \\ \mathbf{v}_{np} &= \{v_i | \text{corr}_i^{\text{train}} \leq 0, \text{corr}_i^{\text{test}} > 0\}, & \mathbf{v}_{nn} &= \{v_i | \text{corr}_i^{\text{train}} \leq 0, \text{corr}_i^{\text{test}} \leq 0\}. & \theta_{np}^*, \theta_{nn}^* &\leq 0 \end{aligned}$$

- In the early stages of adaptation, \mathbf{x} with a high-confidence pseudo-label of $\hat{y} = +1$ satisfies

$$\begin{aligned} a_{\theta}(\mathbf{x}) &= \theta_{pp} \cdot \mathbf{v}_{pp} + \theta_{pn} \cdot \mathbf{v}_{pn} + \theta_{np} \cdot \mathbf{v}_{np} + \theta_{nn} \cdot \mathbf{v}_{nn} \gg 0, \\ |\theta_{pp} \cdot \mathbf{v}_{pp} + \theta_{pn} \cdot \mathbf{v}_{pn}| &\gg |\theta_{np} \cdot \mathbf{v}_{np} + \theta_{nn} \cdot \mathbf{v}_{nn}|. \end{aligned}$$

- Two dominant factors
 - \mathbf{v}_{pp} : Commonly Positively-coRrelated with label (CPR) factors
 - \mathbf{v}_{pn} : TRAIIn-time only Positively-correlated with label (TRAP) factors

Entropy is not enough for TTA! (cont'd)

- By definition, the expectations of CPR factors and TRAP factors are as follows:

$$\begin{aligned}\mathbb{E}_{\mathbf{x}^{\text{test}} \sim \mathcal{X}_{+1}^{\text{test}}}[\mathbf{v}_{pp}(\mathbf{x}^{\text{test}})] &> \mathbb{E}_{\mathbf{x}^{\text{test}} \sim \mathcal{X}_{-1}^{\text{test}}}[\mathbf{v}_{pp}(\mathbf{x}^{\text{test}})], \\ \mathbb{E}_{\mathbf{x}^{\text{test}} \sim \mathcal{X}_{+1}^{\text{test}}}[\mathbf{v}_{pn}(\mathbf{x}^{\text{test}})] &\leq \mathbb{E}_{\mathbf{x}^{\text{test}} \sim \mathcal{X}_{-1}^{\text{test}}}[\mathbf{v}_{pn}(\mathbf{x}^{\text{test}})].\end{aligned}$$

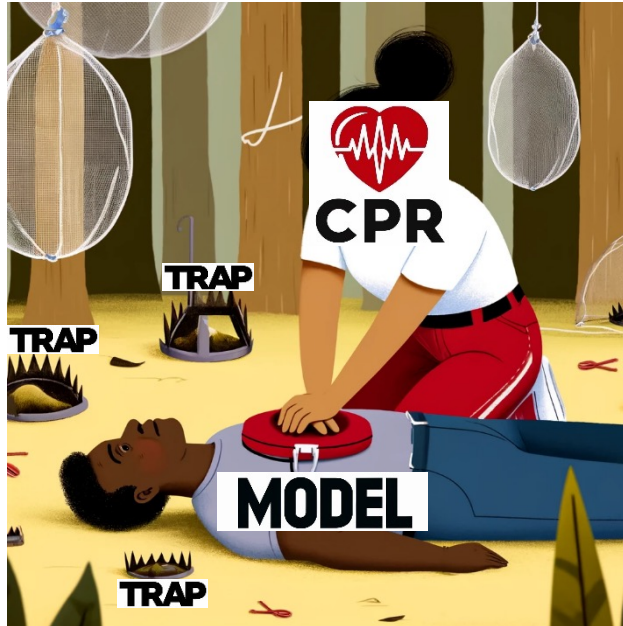
- Reformulation of Eq. (5) of Proposition 1.

$$\begin{aligned}\hat{y}\mathbf{v}(\mathbf{x}) \cdot (\mathbb{E}_{\mathbf{x}^{\text{test}} \sim \mathcal{X}_{+1}^{\text{test}}}[\mathbf{v}(\mathbf{x}^{\text{test}})] - \mathbb{E}_{\mathbf{x}^{\text{test}} \sim \mathcal{X}_{-1}^{\text{test}}}[\mathbf{v}(\mathbf{x}^{\text{test}})]) \\ \approx \underbrace{\mathbf{v}_{pp}(\mathbf{x}) \cdot (\mathbb{E}_{\mathbf{x}^{\text{test}} \sim \mathcal{X}_{+1}^{\text{test}}}[\mathbf{v}_{pp}(\mathbf{x}^{\text{test}})] - \mathbb{E}_{\mathbf{x}^{\text{test}} \sim \mathcal{X}_{-1}^{\text{test}}}[\mathbf{v}_{pp}(\mathbf{x}^{\text{test}})])}_{(7.a)} \\ + \underbrace{\mathbf{v}_{pn}(\mathbf{x}) \cdot (\mathbb{E}_{\mathbf{x}^{\text{test}} \sim \mathcal{X}_{+1}^{\text{test}}}[\mathbf{v}_{pn}(\mathbf{x}^{\text{test}})] - \mathbb{E}_{\mathbf{x}^{\text{test}} \sim \mathcal{X}_{-1}^{\text{test}}}[\mathbf{v}_{pn}(\mathbf{x}^{\text{test}})])}_{(7.b)} < 0\end{aligned}$$

- Eq. (7.a) (related to CPR factors) becomes positive, and Eq. (7.b) (related to TRAP factors) becomes negative
 - $| (7.a) | \ll | (7.b) | \rightarrow$ a *harmful* sample
 - When TRAP factors affect more than CPR factors, the sample becomes *harmful*

Entropy is not enough for TTA! (cont'd)

- If $|(\text{7.a})| \ll |(\text{7.b})|$ and $|\boldsymbol{\theta}_{pp} \cdot \mathbf{v}_{pp} + \boldsymbol{\theta}_{pn} \cdot \mathbf{v}_{pn}| \gg |\boldsymbol{\theta}_{np} \cdot \mathbf{v}_{np} + \boldsymbol{\theta}_{nn} \cdot \mathbf{v}_{nn}|$
→ \mathbf{x} becomes a *harmful* sample with low entropy (high confidence)
 - Low entropy filtering cannot discern **good** & **bad** samples
- Then how to adapt?
 - Utilize the **CPR** factors and avoid the **TRAP** factors!



All sources are created by DALL-E

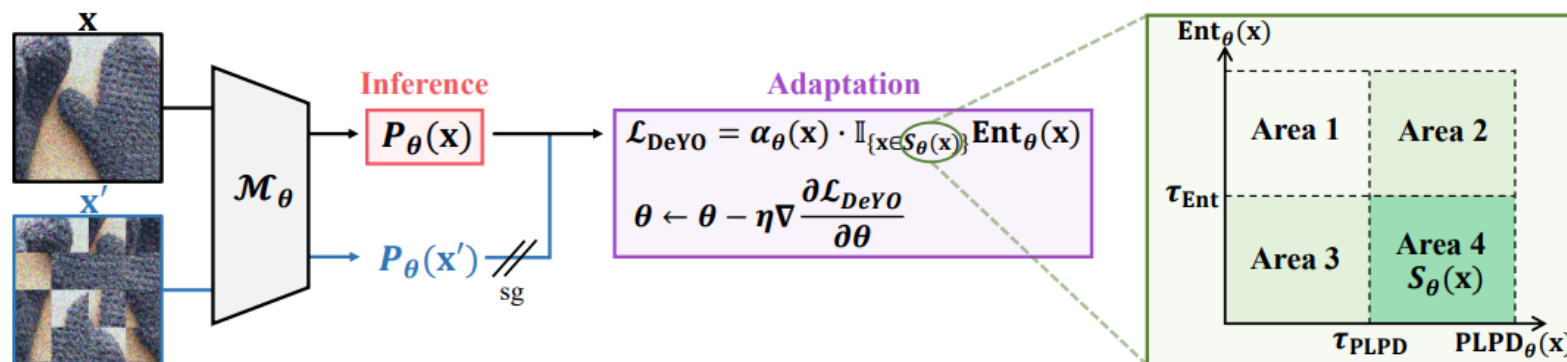
- Destroy Your Object (DeYO)
 - Utilize the factor that aligns with g.t. class (CPR factor: \mathbf{v}_{pp}) under **any** test distribution
 - Classification task: [the shape of object!](#)
 - We can simply apply patch shuffling to destroy the shape information, preserving the patch-level local features.
 - If a prediction becomes uncertain when the shape of object is destroyed,
→ The model considers the shape of the object as the dominant factor when classifying the sample.
 - Pseudo-Label Probability Difference (PLPD)
 - Measures the extent to which the probability of pseudo-label decreases after applying the patch shuffling
 - Utilize samples with low entropy & high PLPD!

$$S_{\theta}(\mathbf{x}) = \{\mathbf{x} | \text{Ent}_{\theta}(\mathbf{x}) < \tau_{\text{Ent}}, \text{PLPD}_{\theta}(\mathbf{x}, \mathbf{x}') > \tau_{\text{PLPD}}\}, \text{ where}$$

$$\text{PLPD}_{\theta}(\mathbf{x}, \mathbf{x}') = (\mathbf{p}_{\theta}(\mathbf{x}) - \mathbf{p}_{\theta}(\mathbf{x}'))_{\hat{y}},$$

Methodology (cont'd)

- Overall procedure of DeYO



$$S_\theta(\mathbf{x}) = \{\mathbf{x} | \text{Ent}_\theta(\mathbf{x}) < \tau_{\text{Ent}}, \text{PLPD}_\theta(\mathbf{x}, \mathbf{x}') > \tau_{\text{PLPD}}\}, \text{ where}$$

$$\text{PLPD}_\theta(\mathbf{x}, \mathbf{x}') = (\mathbf{p}_\theta(\mathbf{x}) - \mathbf{p}_\theta(\mathbf{x}'))_{\hat{y}},$$

$$\alpha_\theta(\mathbf{x}) = \frac{1}{\exp\{(\text{Ent}_\theta(\mathbf{x}) - \text{Ent}_0)\}} + \frac{1}{\exp\{-\text{PLPD}_\theta(\mathbf{x}, \mathbf{x}')\}},$$

$$\mathcal{L}_{\text{DeYO}}(\mathbf{x}; \theta) = \alpha_\theta(\mathbf{x}) \cdot \mathbb{I}_{\{\mathbf{x} \in S_\theta(\mathbf{x})\}} \text{Ent}_\theta(\mathbf{x}),$$

Experiments

- TTA on an i.i.d. sampling (mild) scenario (ResNet-50-BN)

Table 1: Comparisons with baselines on ImageNet-C at severity level 5 under a mild scenario regarding accuracy (%). The **bold** value signifies the top-performing result.

Mild	Noise			Defoc.	Blur			Snow	Weather			Contr.	Digital			Avg.
	Gauss.	Shot	Impul.		Glass	Motion	Zoom		Frost	Fog	Brit.		Elastic	Pixel	JPEG	
ResNet-50-BN	2.2	2.9	1.8	17.9	9.8	14.8	22.5	16.9	23.3	24.4	58.9	5.4	16.9	20.7	31.7	18.0
• MEMO	7.5	8.8	8.9	19.8	13.0	20.7	27.7	25.3	28.7	32.2	61.0	11.0	23.8	33.0	37.6	23.9
• Tent	29.2	31.2	30.1	28.1	27.7	41.4	49.4	47.2	41.5	57.7	67.4	29.2	54.8	58.5	52.4	43.1
• EATA	34.9	37.1	35.8	33.4	33.0	47.1	52.7	51.6	45.7	60.0	68.1	44.4	57.9	60.6	55.1	47.8
• SAR	30.6	30.6	31.3	28.5	28.5	41.9	49.4	47.1	42.2	57.5	67.3	37.8	54.6	58.4	52.1	43.9
• DeYO (ours)	35.6\pm0.2	37.9\pm0.1	37.1\pm0.1	33.8\pm0.2	34.1\pm0.2	48.5\pm0.1	52.8\pm0.1	52.7\pm0.0	46.4\pm0.1	60.6\pm0.0	68.0\pm0.1	46.1\pm0.1	58.4\pm0.1	61.5\pm0.1	55.7\pm0.1	48.6\pm0.0

- TTA on a spurious correlations shift (biased) scenario (ResNet-18/50-BN)

Table 2: Comparisons with baselines on ColoredMNIST regarding accuracy (%).

Biased	Avg Acc	Worst-Group Acc
ResNet-18-BN	63.40	20.05
• Tent	57.06	9.80
• MEMO	63.77	6.23
• SENTRY	63.23	15.78
• EATA	60.81	17.98
• SAR	58.37	12.36
• DeYO (ours)	78.24	67.39

Table 3: Comparisons with baselines on Water-Birds regarding accuracy (%).

Biased	Avg Acc	Worst-Group Acc
ResNet-50-BN	83.16	64.90
• Tent	82.95	54.14
• MEMO	82.34	50.47
• SENTRY	85.77	60.90
• EATA	82.38	52.38
• SAR	82.60	53.41
• DeYO (ours)	87.42	73.92

Experiments (cont'd)

- TTA on wild scenarios (ResNet-50-GN, ViT-16/B)
 - Temporally-correlated label shifts
 - Batch size 1

Table 5: Comparisons with baselines on ImageNet-C at severity level 5 under online imbalanced label shifts (imbalance ratio = ∞) or under batch size 1 regarding accuracy (%).

Label Shifts	Noise			Blur				Weather				Digital				Avg.
	Gauss.	Shot	Impul.	Defoc.	Glass	Motion	Zoom	Snow	Frost	Fog	Brit.	Contr.	Elastic	Pixel	JPEG	
ResNet-50-GN	17.9	19.9	17.9	19.7	11.3	21.3	24.9	40.4	47.4	33.6	69.3	36.3	18.7	28.4	52.2	30.6
• MEMO	18.4	20.6	18.4	17.1	12.7	21.8	26.9	40.7	46.9	34.8	69.6	36.4	19.2	32.2	53.4	31.3
• Tent	3.6	4.2	4.4	16.5	5.9	26.9	28.4	17.9	26.2	2.3	72.2	46.1	7.3	52.3	56.2	24.7
• EATA	25.7	28.6	24.8	18.5	19.6	24.1	28.4	35.3	33.0	41.2	65.2	33.3	28.0	42.4	43.1	32.7
• SAR	33.7	36.9	35.3	19.3	20.3	33.8	29.8	21.9	44.7	34.9	71.9	46.7	6.6	52.3	56.2	36.3
• DeYO (ours)	42.5 _{±0.5}	44.9 _{±0.2}	43.8 _{±0.3}	22.2 _{±0.0}	16.3 _{±10.2}	41.0 _{±0.2}	13.2 _{±9.8}	52.2 _{±0.4}	51.5 _{±0.5}	39.7 _{±27.4}	73.4 _{±0.1}	52.6 _{±0.2}	46.9 _{±1.2}	59.3 _{±0.1}	59.3 _{±0.0}	43.9 _{±2.0}
VitBase-LN	9.4	6.7	8.3	29.1	23.4	34.0	27.1	15.8	26.4	47.4	54.7	44.0	30.5	44.5	47.6	29.9
• MEMO	21.6	17.4	20.6	37.1	29.6	40.6	34.4	25.0	34.8	55.2	65.0	54.9	37.4	55.5	57.7	39.1
• Tent	33.9	1.8	27.2	54.8	52.9	58.6	54.3	12.4	11.7	69.7	76.3	66.3	59.6	69.7	66.6	47.7
• EATA	36.2	34.7	35.5	43.4	44.3	49.3	48.5	53.2	53.5	62.3	72.7	18.8	58.0	64.7	62.8	49.2
• SAR	42.3	34.9	44.1	50.0	50.5	55.6	53.1	59.7	47.2	66.2	75.2	50.3	60.1	67.3	65.0	54.8
• DeYO (ours)	53.5 _{±0.5}	36.0 _{±25.2}	54.6 _{±0.8}	57.6 _{±0.1}	58.7 _{±0.2}	63.7 _{±0.1}	46.2 _{±18.7}	67.6 _{±0.1}	66.0 _{±0.1}	73.2 _{±0.2}	77.9 _{±0.1}	66.7 _{±0.1}	69.0 _{±0.1}	73.5 _{±0.1}	70.3 _{±0.2}	62.3 _{±1.7}
Batch Size 1	Noise			Blur				Weather				Digital				Avg.
	Gauss.	Shot	Impul.	Defoc.	Glass	Motion	Zoom	Snow	Frost	Fog	Brit.	Contr.	Elastic	Pixel	JPEG	
ResNet-50-GN	18.0	19.8	17.9	19.8	11.4	21.4	24.9	40.4	47.3	33.6	69.3	36.3	18.6	28.4	52.3	30.6
• MEMO	18.5	20.5	18.4	17.1	12.6	21.8	26.9	40.4	47.0	34.4	69.5	36.5	19.2	32.1	53.3	31.2
• Tent	3.1	4.2	4.0	16.5	5.3	27.4	30.3	17.7	24.9	2.0	72.1	46.2	7.8	52.6	56.3	24.7
• EATA	24.8	27.9	25.8	17.9	17.3	28.7	29.3	44.7	44.4	40.2	71.0	44.5	27.0	46.8	55.6	36.4
• SAR	23.3	26.6	23.9	18.5	15.2	28.6	30.3	44.0	44.7	29.0	72.3	44.6	13.1	46.8	56.1	34.5
• DeYO (ours)	41.8 _{±0.7}	44.7 _{±0.4}	43.0 _{±0.7}	22.5 _{±0.1}	24.7 _{±0.3}	41.8 _{±0.1}	24.4 _{±9.8}	54.5 _{±0.2}	52.2 _{±0.2}	20.7 _{±26.8}	73.5 _{±0.0}	53.5 _{±0.2}	48.5 _{±0.3}	60.2 _{±0.0}	59.8 _{±0.1}	44.4 _{±1.2}
VitBase-LN	9.5	6.8	8.2	29.0	23.5	33.9	27.1	15.9	26.5	47.2	54.7	44.1	30.5	44.5	47.8	29.9
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• Tent	43.0	1.6	43.9	52.8	48.8	55.9	51.3	22.9	21.1	66.9	75.1	65.0	54.0	67.0	64.3	48.9
• EATA	32.2	26.7	30.3	43.8	40.1	47.7	42.6	35.7	43.4	60.8	65.6	61.1	46.5	60.5	58.2	46.3
• SAR	40.6	36.9	41.9	53.7	50.5	57.4	52.8	58.9	52.7	68.9	76.0	65.8	57.9	68.9	65.8	56.6
• DeYO (ours)	54.0 _{±0.7}	52.1 _{±3.6}	55.1 _{±0.8}	58.8 _{±0.1}	59.5 _{±0.1}	64.2 _{±0.1}	53.5 _{±5.5}	68.2 _{±0.1}	66.4 _{±0.0}	73.7 _{±0.1}	78.3 _{±0.0}	68.2 _{±0.1}	68.9 _{±0.1}	73.8 _{±0.1}	70.8 _{±0.3}	64.4 _{±0.7}

Thank you!

- **TL;DR**
 - Address the limitations of relying solely on entropy as a confidence metric for TTA.
- **Summary**
 - Theoretically prove why entropy is not enough for TTA.
 - Entropy cannot discern the CPR and TRAP factors.
 - Introduce an effective TTA method based on the proposed novel confidence metric.
 - Achieve state-of-the-art performances in various TTA scenarios.
- More details can be found:
 - Paper: <https://openreview.net/forum?id=gw3iw8wDuE>
 - Project page: <https://whitesnowdrop.github.io/DeYO/>
 - Code: <https://github.com/Jhyun17/DeYO>
 - Poster Session: Tue 7 May 10:45 am - 12:45 pm at Halle B