

Beating Price of Anarchy and Gradient Descent without Regret in Potential Games

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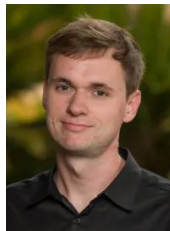
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Quality of Learning Outcomes in Potential Games

- Multi-agent learning occurs on **highly non-convex** landscapes.
- Even if learning dynamics equilibrate, their fixed points may be of **poor performance**.

How do we **measure** the performance of learning dynamics?

Are some learning dynamics **better than** others?

Limitations of Static Performance Metrics

$$\text{PoA} = \frac{\max_x \text{SW}(x)}{\min_{x^* \in \text{NE}} \text{SW}(x^*)}$$

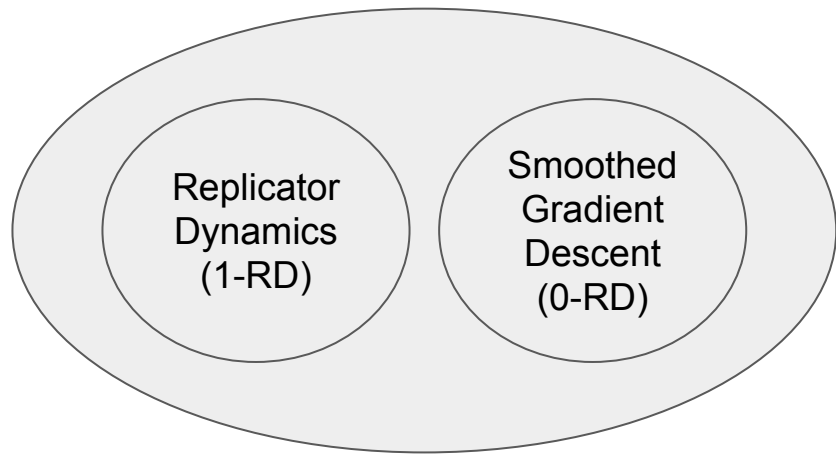
- The PoA **does not depend** on the learning process.
- The socially-worst equilibrium might be reachable by **only a few initializations**.
- The PoA can be **unbounded** even for simple classes of games.

Average Price of Anarchy (APoA)

$$\text{APoA} = \frac{\max_x \text{SW}(x)}{\mathbb{E}[\text{SW}(x^*)]}$$

- The APoA **depends on the learning process**.
- The APoA **requires equilibration** for almost all initial conditions.

Convergence of QRD in Potential Games (Theorem 3.2)



Q-Replicator Dynamics (QRD)

- QRD equilibrate in almost **all potential games**
- QRD equilibrate for almost **all initial conditions**

Average Price of Anarchy Analysis for QRD

In symmetric 2x2 potential games, where the **payoff-dominant and risk dominant equilibria coincide**:

- **Gradient Descent outperforms Replicator Dynamics**
in terms of APoA (Theorem 4.6)
- The **APoA of Gradient Descent is upper bounded by 2**
(Theorem 4.8)

Thank you!

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