

### Spreading Out-of-Distribution on Graphs

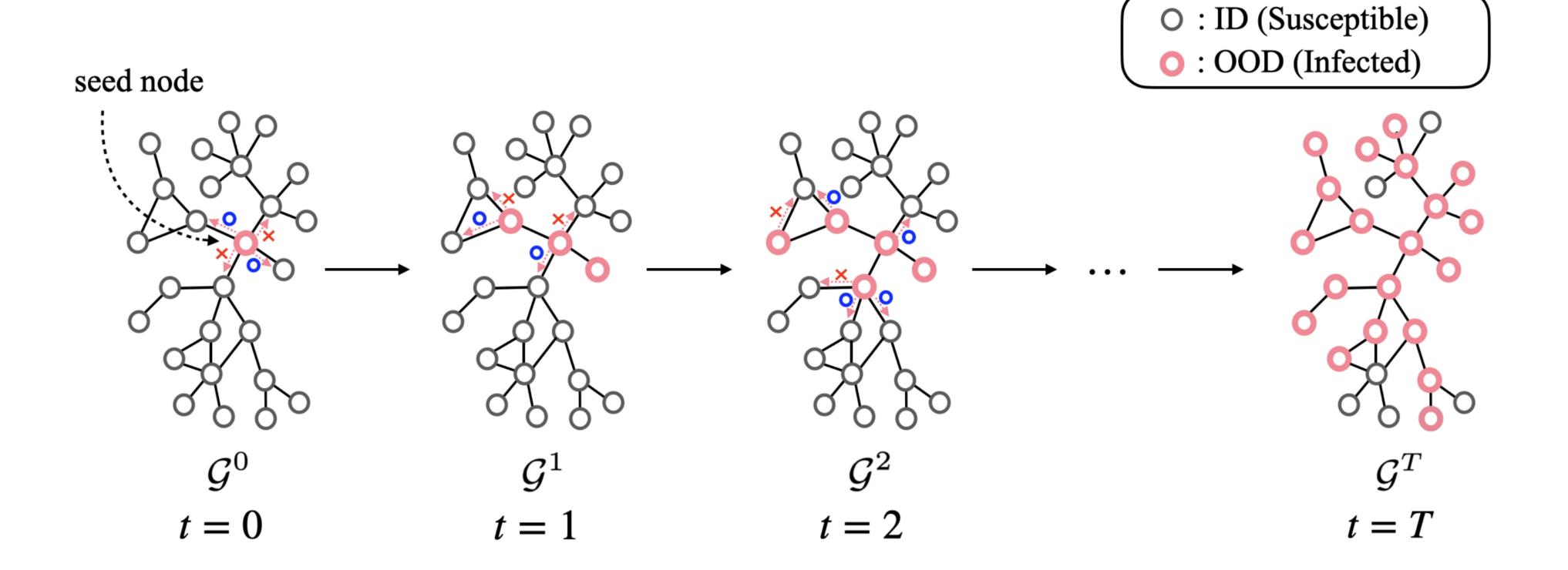
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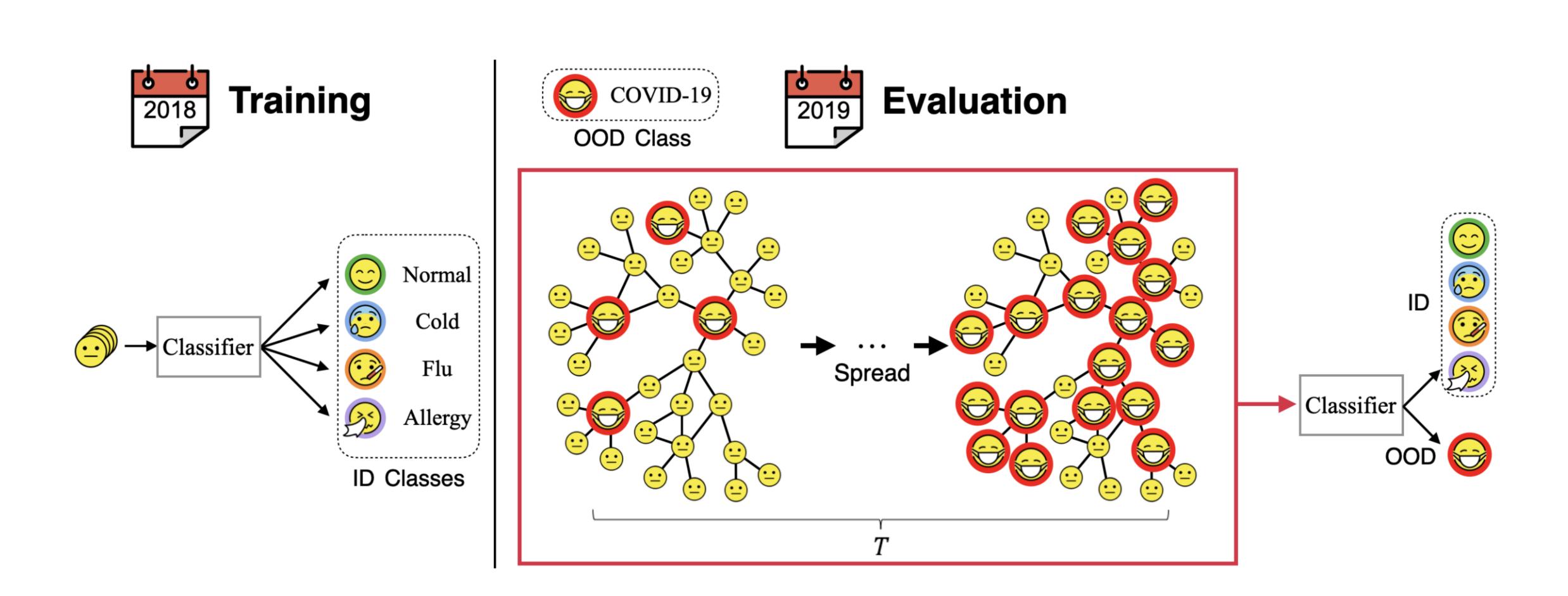
### Node-Level OOD Detection Benchmark

- Node-level OOD detection methods are commonly evaluated on synthetic graph datasets where OOD samples are assigned to randomly selected nodes.
- Nodes belonging to randomly selected classes or randomly selected nodes are designated as OOD.
- These previous evaluation scenarios fail to reflect interactions with the various nodes associated with OOD samples.

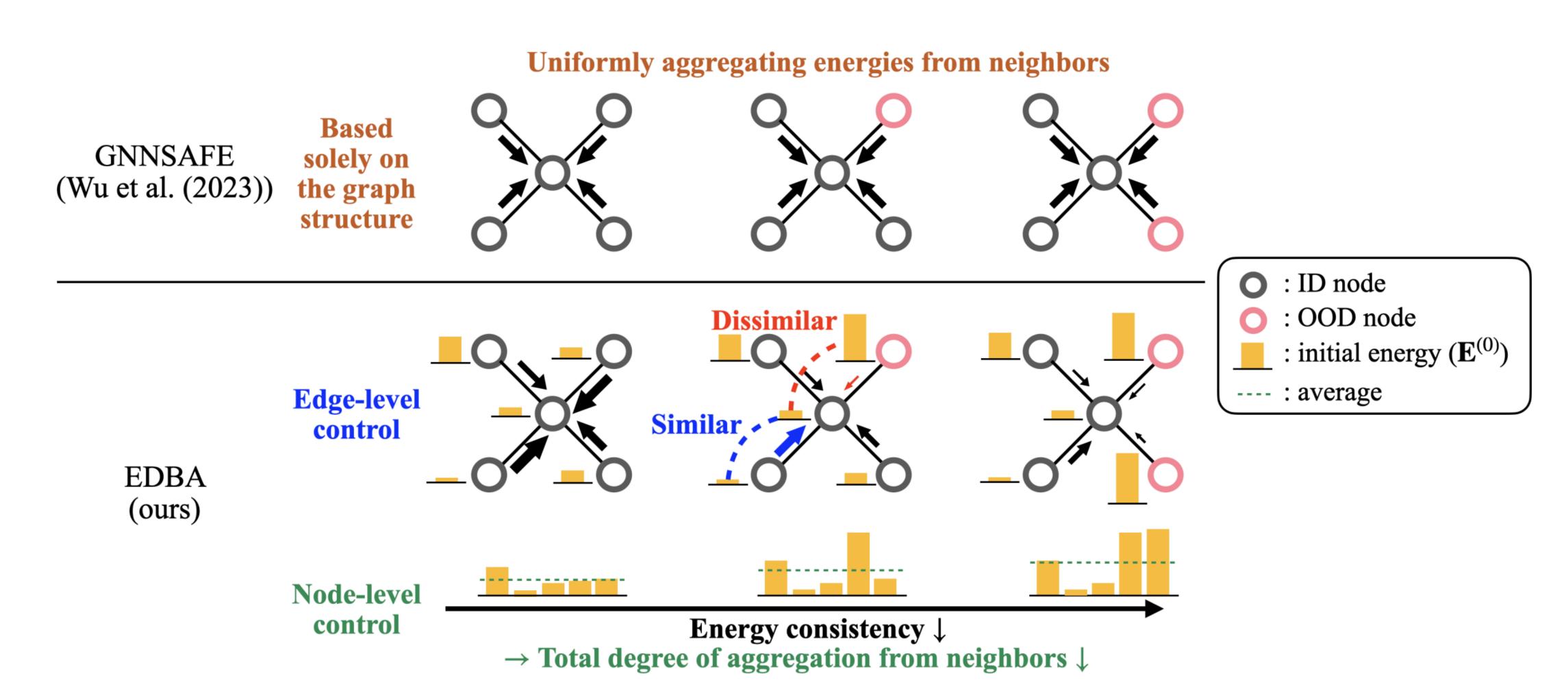
## Spreading OOD Detection



### Spreading COVID-19 Dataset



# Energy Distribution-Based Aggregation (EDBA)



# Experiments

#### Label leave-out

Dataset	CORA			AMAZON-PHOTO			
Method	FPR95(↓)	AUROC(↑)	AUPR(↑)	FPR95(↓)	AUROC(↑)	AUPR(↑)	
MSP	$40.37 \pm 2.19$	$91.13 \pm 0.22$	$78.16 \pm 0.19$	$28.87 \pm 1.65$	$94.41 \pm 0.61$	$92.44 \pm 0.75$	
ODIN	$100.00 \pm 0.00$	$49.05 \pm 0.57$	$24.18 \pm 0.08$	$92.72 \pm 8.43$	$63.30 \pm 7.61$	$51.72 \pm 7.43$	
Mahalanobis	$86.11 \pm 6.19$	$66.93 \pm 1.95$	$40.56 \pm 3.77$	$56.11 \pm 16.06$	$82.51 \pm 4.83$	$75.73 \pm 7.09$	
Energy	$38.36 \pm 3.46$	$91.46 \pm 0.33$	$78.10 \pm 0.29$	$30.49 \pm 3.93$	$93.96 \pm 0.68$	$91.73 \pm 0.75$	
GKDE	$60.88 \pm 2.25$	$87.15 \pm 0.60$	$72.12 \pm 1.10$	$91.60 \pm 8.81$	$60.00 \pm 11.43$	$56.61 \pm 12.77$	
GPN	$44.04 \pm 5.85$	$87.48 \pm 6.38$	$81.21 \pm 7.40$	$35.54 \pm 11.48$	$91.48 \pm 2.71$	$88.04 \pm 3.41$	
OODGAT	$85.21 \pm 1.66$	$64.81 \pm 0.87$	$62.65 \pm 1.01$	$13.33 \pm 0.46$	$97.27 \pm 0.33$	$95.01 \pm 0.60$	
<b>GNNSAFE</b>	$31.31 \pm 1.11$	$92.84 \pm 0.38$	$82.22 \pm 0.40$	$6.57 \pm 0.38$	$97.36 \pm 0.04$	$97.13 \pm 0.10$	
EDBD	$30.48\pm1.11$	$92.95 \pm 0.38$	$82.31 \pm 0.38$	$ \boxed{ 5.82 \pm 0.66 }$	$97.48 \pm 0.07$	$97.60 \pm 0.06$	
	AMAZON-COMPUTERS			COAUTHOR-CS			
Dataset	AM	IAZON-COMPUTI	ERS		COAUTHOR-CS		
Dataset  Method	AM   FPR95(↓)	IAZON-COMPUTI AUROC(†)	ERS AUPR(†)	   FPR95(↓)	COAUTHOR-CS AUROC(↑)	AUPR(†)	
	I			FPR95( $\downarrow$ )   29.07 $\pm$ 3.53		$AUPR(\uparrow)$ $97.73 \pm 0.28$	
Method	FPR95(↓)	AUROC(†)	AUPR(†)		AUROC(†)		
Method	FPR95( $\downarrow$ )   70.77 $\pm$ 3.54	$\begin{array}{c} \text{AUROC}(\uparrow) \\ \hline 76.81 \pm 2.31 \end{array}$	AUPR(†) 71.01 ± 2.23	$29.07 \pm 3.53$	$\begin{array}{c} \text{AUROC}(\uparrow) \\ 94.15 \pm 0.73 \end{array}$	$97.73 \pm 0.28$	
Method MSP ODIN	FPR95( $\downarrow$ )	AUROC( $\uparrow$ ) $76.81 \pm 2.31$ $53.36 \pm 1.91$	AUPR( $\uparrow$ ) $71.01 \pm 2.23$ $45.93 \pm 2.83$	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	AUROC( $\uparrow$ ) $94.15 \pm 0.73$ $52.35 \pm 4.36$	$97.73 \pm 0.28$ $75.26 \pm 1.96$	
Method  MSP ODIN Mahalanobis	FPR95( $\downarrow$ )	AUROC( $\uparrow$ ) $76.81 \pm 2.31$ $53.36 \pm 1.91$ $73.14 \pm 1.27$	AUPR( $\uparrow$ ) $71.01 \pm 2.23$ $45.93 \pm 2.83$ $62.63 \pm 2.43$	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	AUROC( $\uparrow$ ) $94.15 \pm 0.73$ $52.35 \pm 4.36$ $81.73 \pm 3.53$	$97.73 \pm 0.28$ $75.26 \pm 1.96$ $84.30 \pm 15.80$	
Method  MSP ODIN Mahalanobis Energy	FPR95( $\downarrow$ )  70.77 ± 3.54  98.72 ± 2.56  71.09 ± 1.90  58.40 ± 3.41	AUROC( $\uparrow$ )  76.81 $\pm$ 2.31  53.36 $\pm$ 1.91  73.14 $\pm$ 1.27  84.72 $\pm$ 1.50	AUPR( $\uparrow$ ) $71.01 \pm 2.23$ $45.93 \pm 2.83$ $62.63 \pm 2.43$ $79.36 \pm 1.66$	$egin{array}{ c c c c c c c c c c c c c c c c c c c$	AUROC( $\uparrow$ )  94.15 $\pm$ 0.73  52.35 $\pm$ 4.36  81.73 $\pm$ 3.53  95.98 $\pm$ 0.71	$97.73 \pm 0.28$ $75.26 \pm 1.96$ $84.30 \pm 15.80$ $98.39 \pm 0.29$	
Method  MSP ODIN Mahalanobis Energy GKDE	FPR95( $\downarrow$ )  70.77 ± 3.54  98.72 ± 2.56  71.09 ± 1.90  58.40 ± 3.41  90.64 ± 7.22	AUROC( $\uparrow$ )  76.81 $\pm$ 2.31  53.36 $\pm$ 1.91  73.14 $\pm$ 1.27  84.72 $\pm$ 1.50  58.59 $\pm$ 10.46	AUPR( $\uparrow$ ) $71.01 \pm 2.23$ $45.93 \pm 2.83$ $62.63 \pm 2.43$ $79.36 \pm 1.66$ $49.23 \pm 8.10$	$ \begin{array}{c c} 29.07 \pm 3.53 \\ 100.00 \pm 0.00 \\ 64.40 \pm 14.83 \\ 18.60 \pm 3.87 \\ 59.70 \pm 7.83 \end{array} $	AUROC( $\uparrow$ )  94.15 ± 0.73 52.35 ± 4.36 81.73 ± 3.53 95.98 ± 0.71 88.02 ± 1.77 93.54 ± 3.35 96.83 ± 0.21	$97.73 \pm 0.28$ $75.26 \pm 1.96$ $84.30 \pm 15.80$ $98.39 \pm 0.29$ $95.50 \pm 0.65$	
Method  MSP ODIN Mahalanobis Energy GKDE GPN	FPR95( $\downarrow$ )  70.77 ± 3.54  98.72 ± 2.56  71.09 ± 1.90  58.40 ± 3.41  90.64 ± 7.22  80.55 ± 16.98	AUROC( $\uparrow$ ) $76.81 \pm 2.31$ $53.36 \pm 1.91$ $73.14 \pm 1.27$ $84.72 \pm 1.50$ $58.59 \pm 10.46$ $74.08 \pm 15.09$	AUPR( $\uparrow$ )  71.01 ± 2.23 45.93 ± 2.83 62.63 ± 2.43 79.36 ± 1.66 49.23 ± 8.10 69.27 ± 17.30	$\begin{array}{c c} 29.07 \pm 3.53 \\ 100.00 \pm 0.00 \\ 64.40 \pm 14.83 \\ 18.60 \pm 3.87 \\ 59.70 \pm 7.83 \\ 26.68 \pm 11.56 \end{array}$	AUROC( $\uparrow$ )  94.15 ± 0.73  52.35 ± 4.36  81.73 ± 3.53  95.98 ± 0.71  88.02 ± 1.77  93.54 ± 3.35	$97.73 \pm 0.28$ $75.26 \pm 1.96$ $84.30 \pm 15.80$ $98.39 \pm 0.29$ $95.50 \pm 0.65$ $97.40 \pm 1.47$	

### Experiments

#### Spreading OOD detection in the COVID-19 dataset

#### Single-seed setting

Epidemic model		SI			SIS			
Method	FPR95-T (↓)	AUROC-T (↑)	AUPR-T (↑)	FPR95-T (↓)	AUROC-T (↑)	AUPR-T (†)		
MSP	$94.25 \pm 4.56$	$38.51 \pm 5.41$	$70.17 \pm 4.55$	$97.98 \pm 1.38$	$34.45 \pm 5.87$	$70.01 \pm 2.73$		
ODIN	$93.19 \pm 5.00$	$61.82 \pm 11.50$	$78.08 \pm 6.05$	$89.87 \pm 5.76$	$65.86\pm10.63$	$80.26 \pm 5.54$		
Mahalanobis	$63.64 \pm 44.93$	$47.29 \pm 42.24$	$79.46\pm15.28$	$72.71 \pm 36.33$	$46.61 \pm 34.07$	$78.95 \pm 12.00$		
Energy	$54.82 \pm 17.43$	$80.46 \pm 8.54$	$88.00 \pm 5.52$	$67.94 \pm 18.98$	$73.94 \pm 14.49$	$85.51 \pm 5.70$		
GPN	$95.29 \pm 2.36$	$50.35 \pm 13.69$	$79.55 \pm 65.45$	$87.07 \pm 14.50$	$67.20 \pm 12.68$	$83.03 \pm 4.40$		
GNNSAFE	$69.76 \pm 15.23$	$80.65 \pm 6.07$	$87.40 \pm 4.12$	$77.76 \pm 14.64$	$76.02\pm12.65$	$85.53 \pm 5.30$		
EDBD	$oxed{  54.67 \pm 17.58  }$	$81.60 \pm 8.35$	$88.22 \pm 5.59$	$ \boxed{ \textbf{67.42} \pm \textbf{19.75} }$	$\textbf{76.22} \pm \textbf{14.58}$	$\textbf{85.94} \pm \textbf{5.94}$		

#### Multi-seed setting

Epidemic model		SI		SIS			
Method	FPR95-T (↓)	AUROC-T (↑)	AUPR-T (↑)	FPR95-T (↓)	AUROC-T (↑)	AUPR-T (†)	
MSP	$96.29 \pm 1.94$	$36.41 \pm 5.86$	$58.63 \pm 3.18$	$96.14 \pm 1.87$	$37.49 \pm 5.36$	$55.23 \pm 2.98$	
ODIN	$92.61 \pm 3.42$	$63.15\pm12.07$	$72.47 \pm 6.61$	$91.93 \pm 4.69$	$64.59 \pm 10.37$	$69.05 \pm 6.80$	
Mahalanobis	$90.44 \pm 0.53$	$27.93 \pm 0.67$	$53.78 \pm 0.95$	$90.55 \pm 0.50$	$31.09 \pm 0.63$	$54.08 \pm 0.62$	
Energy	$49.78 \pm 14.73$	$82.66 \pm 6.79$	$85.94 \pm 4.92$	$60.40 \pm 10.33$	$80.18 \pm 6.24$	$81.63 \pm 4.84$	
GPN	$87.72 \pm 6.17$	$62.81 \pm 9.26$	$75.13 \pm 5.38$	$89.29 \pm 5.18$	$61.85 \pm 8.69$	$71.39 \pm 5.29$	
<b>GNNSAFE</b>	$63.42 \pm 14.09$	$82.21 \pm 5.91$	$86.11 \pm 4.33$	$63.32 \pm 1.14$	$77.80 \pm 5.16$	$80.40 \pm 3.96$	
EDBD	$oxed{ }~ \mathbf{49.62 \pm 15.22}$	$83.29 \pm 6.68$	$86.11 \pm 5.01$	$ \boxed{ 59.93 \pm 10.47 } $	$80.68 \pm 6.16$	$81.70 \pm 4.92$	

## Experiments

Spreading OOD detection in benchmark datasets

Epidemic	Dataset	CORA			LASTFM ASIA			
model	Method	FPR95-T (↓)	AUROC-T (↑)	AUPR-T (↑)	FPR95-T (↓)	AUROC-T (↑)	AUPR-T (↑)	
	MSP	$24.80 \pm 16.38$	$96.04 \pm 2.26$	$97.73 \pm 1.13$	$52.98 \pm 0.41$	$93.71 \pm 1.80$	$97.96 \pm 0.44$	
	ODIN	$100.00 \pm 0.00$	$45.65 \pm 10.85$	$74.03 \pm 4.70$	$100.00 \pm 0.00$	$17.35 \pm 6.96$	$68.61 \pm 4.08$	
	Mahalanobis	$65.32 \pm 44.90$	$65.50 \pm 32.93$	$88.21 \pm 11.85$	$59.29 \pm 48.43$	$87.34 \pm 15.97$	$96.66 \pm 3.92$	
SI	Energy	$22.79 \pm 18.21$	$96.36 \pm 2.12$	$98.03 \pm 1.07$	$54.44 \pm 16.82$	$93.56 \pm 1.71$	$97.86 \pm 0.45$	
	GPN	$100.00 \pm 0.00$	$53.71 \pm 4.38$	$73.93 \pm 2.67$	$100.00 \pm 0.00$	$19.70 \pm 9.19$	$75.05 \pm 18.16$	
	GNNSAFE	$31.15\pm10.74$	$93.45 \pm 2.16$	$97.59 \pm 0.71$	$64.83 \pm 8.52$	$83.73 \pm 4.22$	$93.94 \pm 1.05$	
	EDBD	$14.99 \pm 14.53$	$97.54 \pm 1.81$	$98.68 \pm 0.85$	$46.68 \pm 14.83$	$94.10 \pm 1.71$	$98.11 \pm 0.41$	
	MSP	$40.47 \pm 8.78$	$92.91 \pm 1.34$	$93.22 \pm 1.59$	$57.19 \pm 18.25$	$91.48 \pm 2.88$	$94.26 \pm 1.43$	
	ODIN	$95.52 \pm 8.97$	$52.14 \pm 11.24$	$69.25 \pm 6.79$	$100.00 \pm 0.00$	$20.71 \pm 9.38$	$61.54 \pm 5.78$	
	Mahalanobis	$74.28 \pm 40.81$	$68.97 \pm 25.99$	$88.02 \pm 10.64$	$86.86 \pm 28.32$	$83.20 \pm 6.94$	$94.87 \pm 1.96$	
SIS	Energy	$38.95 \pm 9.16$	$93.27 \pm 1.34$	$93.59 \pm 1.55$	$58.12 \pm 18.99$	$91.08 \pm 3.27$	$94.07 \pm 1.57$	
	GPN	$100.00 \pm 0.00$	$47.38 \pm 4.39$	$69.93 \pm 6.55$	$100.00 \pm 0.00$	$22.41 \pm 13.41$	$87.30 \pm 9.84$	
	GNNSAFE	$47.55 \pm 11.24$	$90.91 \pm 2.78$	$93.19 \pm 1.54$	$73.94 \pm 8.07$	$82.73 \pm 4.55$	$90.17 \pm 1.64$	
	EDBD	$32.61 \pm 7.18$	$94.17 \pm 1.22$	$94.19 \pm 1.39$	$52.37 \pm 19.93$	$91.78 \pm 3.04$	$94.40 \pm 1.52$	

#### Conclusion

- ✓ We introduce spreading OOD detection, a problem that facilitates the evaluation of node-level OOD detection under realistic settings.
- ✓ To highlight the significance of this problem, we then present the Spreading COVID-19 dataset.
- ✓ We propose EDBD that achieves state-of-the-art performance in both spreading OOD detection and conventional node-level OOD detection tasks.
- ✓ We hope that our work will inspire the creation of datasets for practical node-level OOD detection research within the machine learning community.