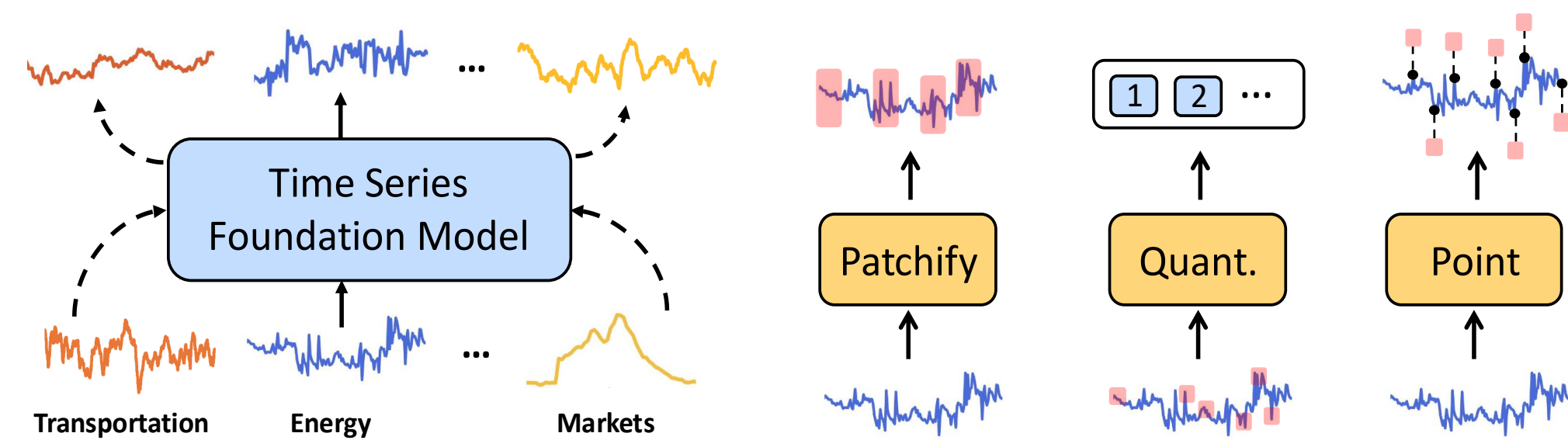


# Time-MoE: Billion-Scale Time Series Foundation Models with Mixture of Experts

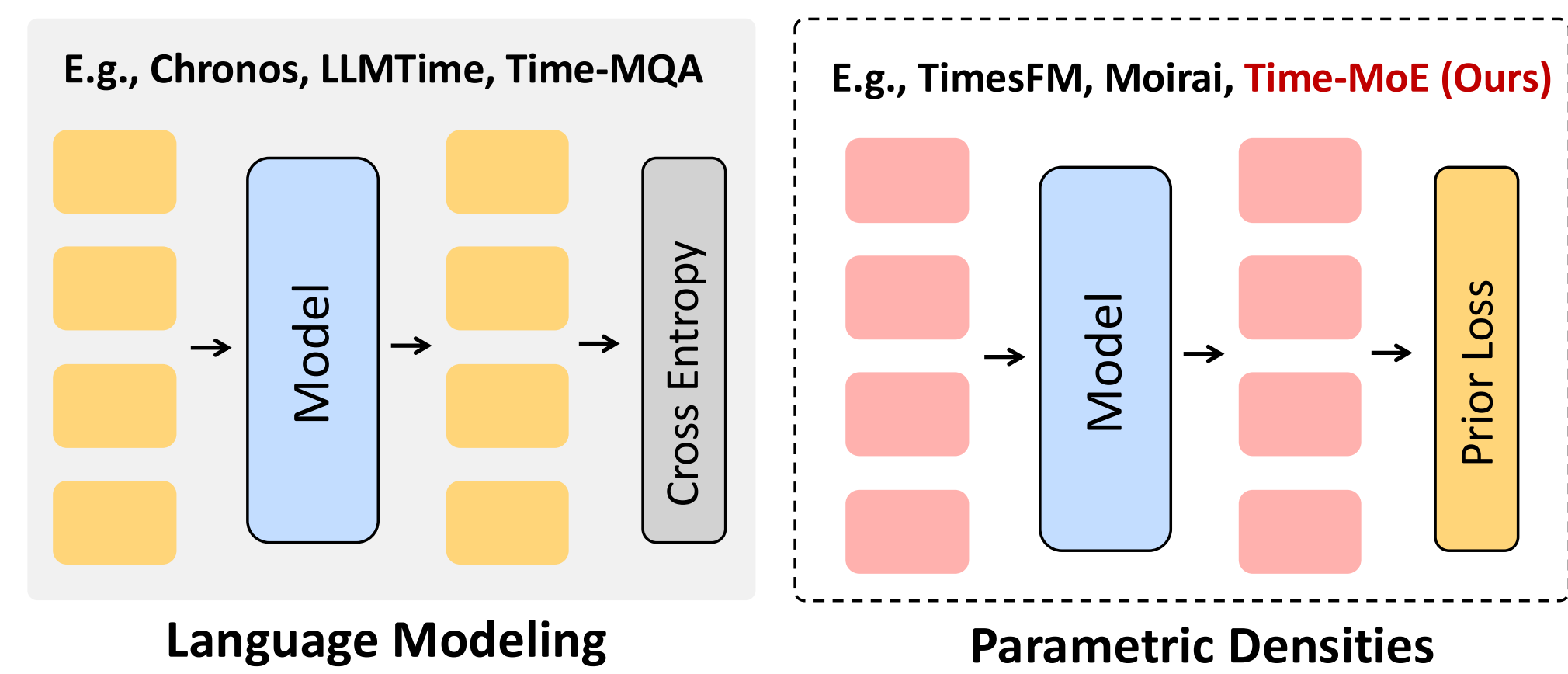
Xiaoming Shi\*, Shiyu Wang\*, Yuqi Nie \*, Dianqi Li, Zhou Ye, Qingsong Wen, Ming Jin

## ① Time Series Foundation Models

### Time series forecasting using a unified model

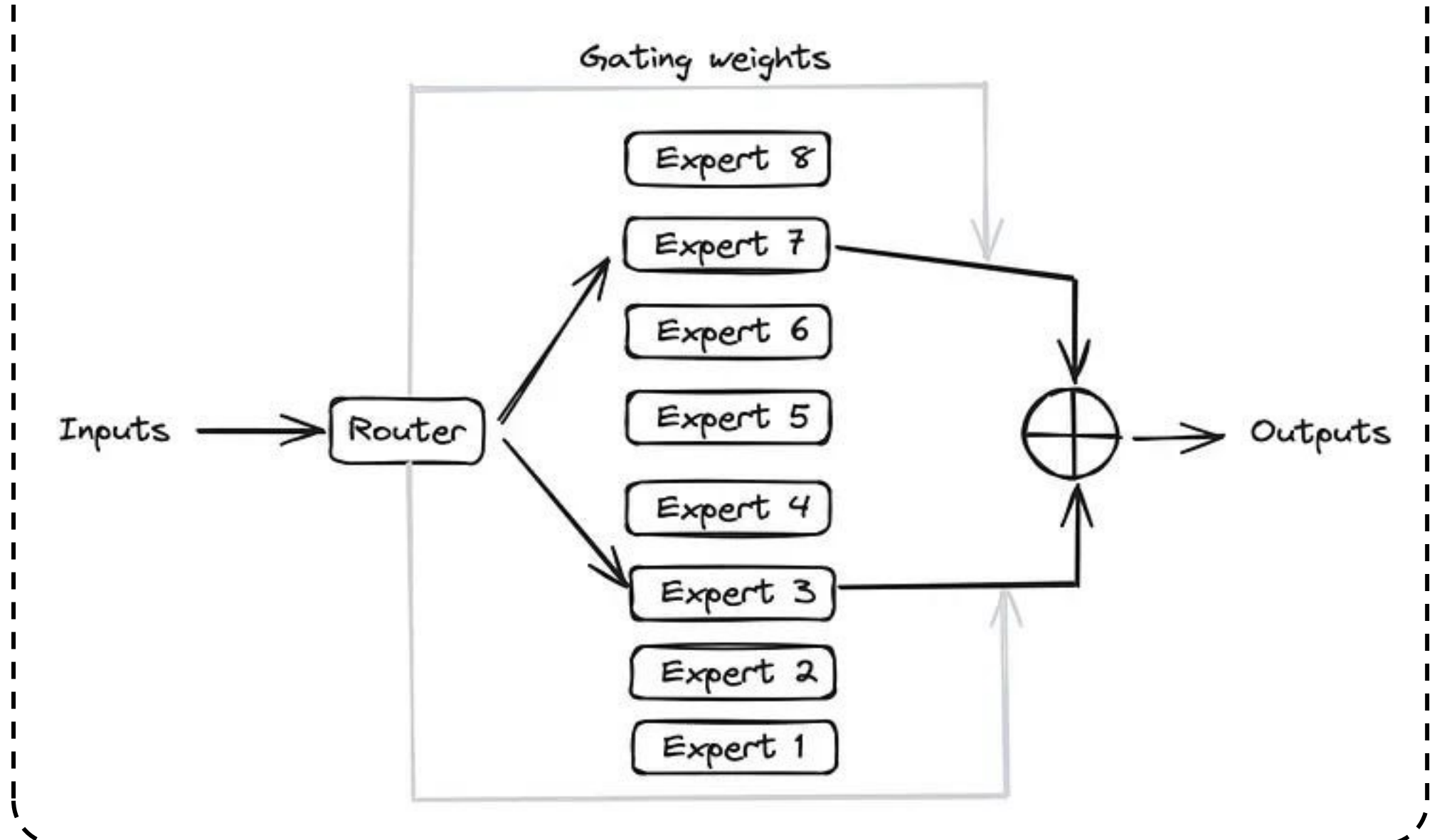


### Two time series foundation model paradigms

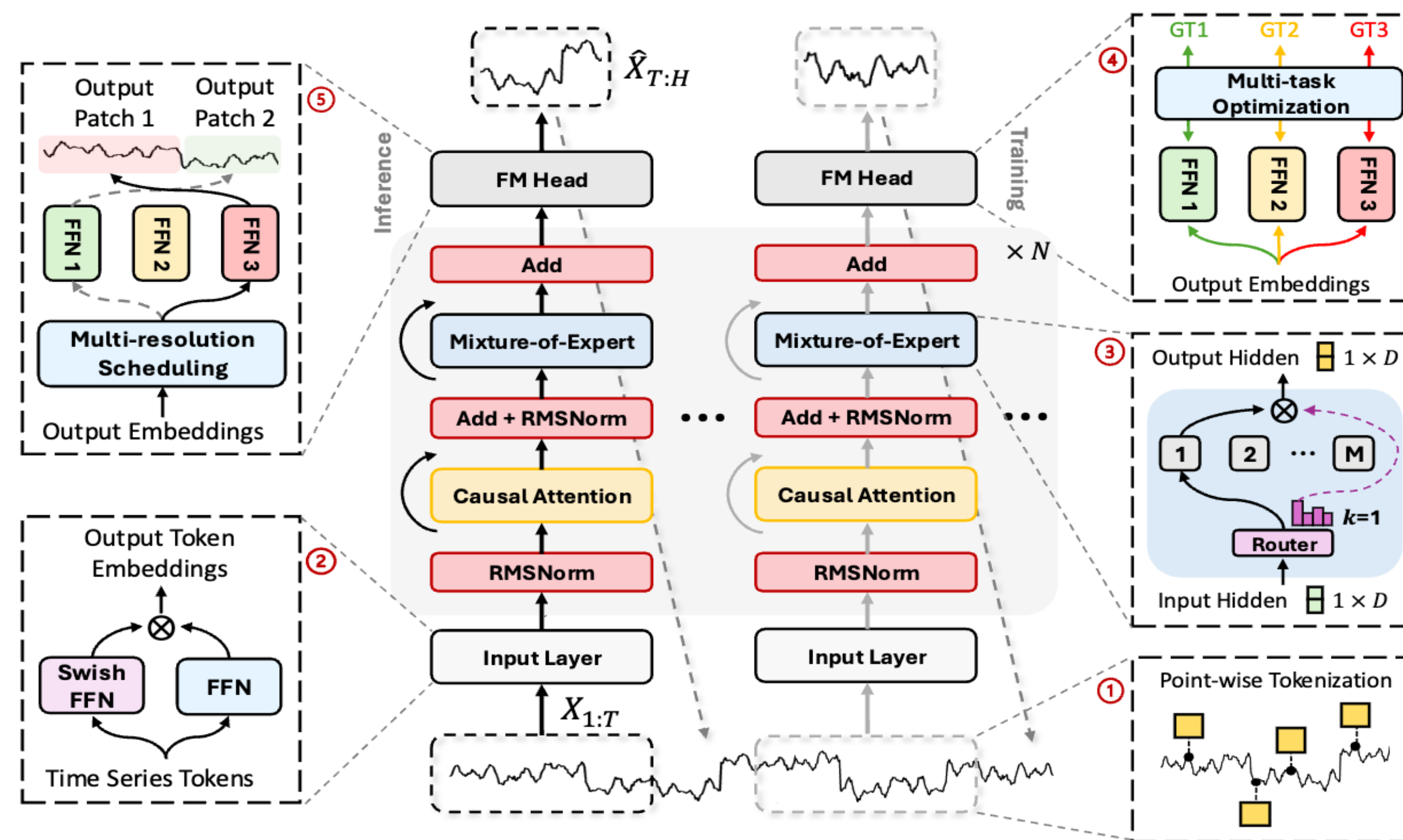


## ② Why Mixture-of-Experts?

MoE architecture makes TSFMs **computationally efficient** while maintaining **high model capacity** for time series tasks



## ③ Methodology

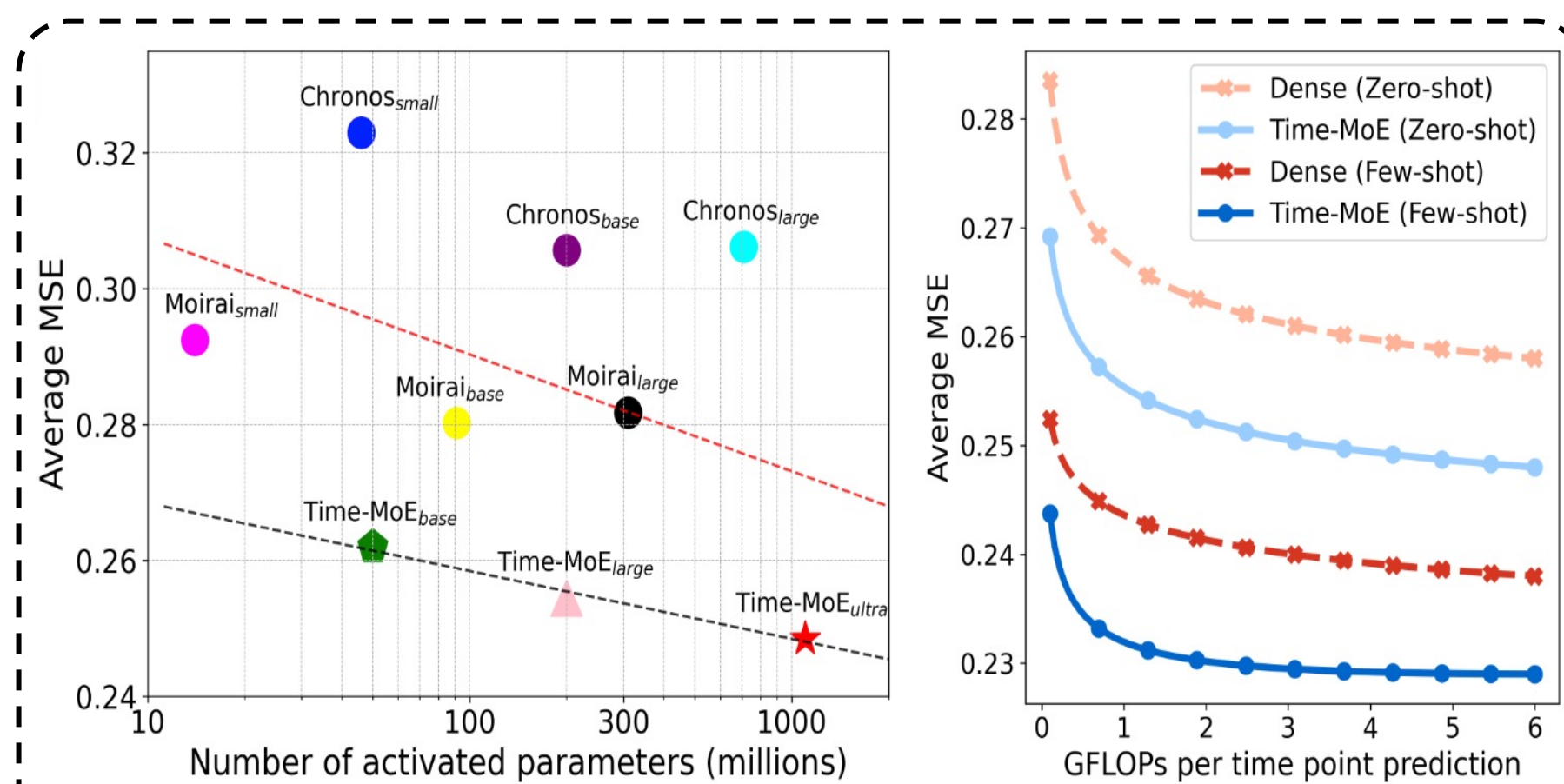


Given an input time series, ① we first tokenize it into a sequence of data points, ② which are then encoded. These tokens are processed through N-stacked backbone layers, primarily consisting of casual multi-head self-attention and ③ sparse temporal mixture-of-expert layers. During training, ④ we optimize forecasting heads at multiple resolutions. For model inference, Time-MoE provides forecasts of flexible length by ⑤ dynamically scheduling these heads.

## ④ Zero-shot Forecasting

**Zero-shot forecasting results.** All results are from four different forecasting horizons:  $H \in \{96, 192, 336, 720\}$ ; **Red**: the best, **Blue**: the 2<sup>nd</sup> best

Models	TIME-MoE (Ours)				Zero-shot Time Series Models											
	TIME-MoE <sub>base</sub>	TIME-MoE <sub>large</sub>	TIME-MoE <sub>ultra</sub>		MoE <sub>small</sub>	MoE <sub>base</sub>	MoE <sub>large</sub>	TimesFM	Moment	Chronos <sub>small</sub>	Chronos <sub>base</sub>	Chronos <sub>large</sub>	MoE <sub>small</sub>	MoE <sub>base</sub>	MoE <sub>large</sub>	
ETTh1	96	0.357	0.381	0.350	0.382	0.349	0.379	0.401	0.402	0.376	0.392	0.381	0.388	0.365	0.375	0.400
	192	0.384	0.404	0.388	0.412	0.395	0.413	0.435	0.421	0.412	0.413	0.434	0.415	0.465	0.434	0.450
	336	0.411	0.434	0.411	0.430	0.447	0.455	0.457	0.462	0.453	0.458	0.465	0.455	0.563	0.570	0.486
	720	0.449	0.477	0.427	0.455	0.457	0.462	0.611	0.511	0.481	0.683	0.585	0.615	0.581	0.853	0.583
ETTh2	96	0.305	0.359	0.302	0.354	0.297	0.336	0.294	0.330	0.296	0.330	0.315	0.349	0.342	0.396	0.307
	192	0.351	0.386	0.364	0.385	0.347	0.379	0.368	0.381	0.365	0.375	0.361	0.371	0.388	0.393	0.402
	336	0.391	0.418	0.417	0.425	0.406	0.419	0.370	0.393	0.376	0.390	0.390	0.390	0.422	0.427	0.492
	720	0.419	0.454	0.537	0.496	0.439	0.447	0.411	0.426	0.416	0.433	0.423	0.416	0.463	0.454	0.533
ETTm1	96	0.338	0.368	0.309	0.357	0.281	0.341	0.418	0.392	0.363	0.356	0.380	0.361	0.361	0.370	0.547
	192	0.353	0.388	0.346	0.381	0.305	0.358	0.431	0.405	0.388	0.375	0.412	0.383	0.414	0.405	0.662
	336	0.381	0.413	0.408	0.369	0.395	0.403	0.433	0.412	0.416	0.392	0.436	0.400	0.445	0.429	0.672
	720	0.504	0.493	0.475	0.477	0.469	0.472	0.462	0.432	0.460	0.418	0.462	0.420	0.512	0.471	0.692
ETTm2	96	0.394	0.415	0.376	0.405	0.366	0.391	0.436	0.410	0.406	0.385	0.422	0.391	0.443	0.418	0.676
	192	0.201	0.291	0.197	0.286	0.198	0.288	0.214	0.288	0.205	0.273	0.211	0.274	0.202	0.270	0.260
	336	0.324	0.373	0.337	0.375	0.293	0.348	0.331	0.362	0.329	0.350	0.341	0.355	0.360	0.349	0.354
	720	0.488	0.464	0.480	0.461	0.427	0.428	0.402	0.408	0.437	0.411	0.485	0.428	0.462	0.430	0.394
Weather	96	0.160	0.210	0.159	0.213	0.157	0.213	0.198	0.222	0.220	0.217	0.199	0.211	-	-	0.243
	192	0.210	0.264	0.215	0.266	0.208	0.256	0.247	0.265	0.271	0.259	0.246	0.251	-	-	0.278
	336	0.324	0.309	0.291	0.322	0.285	0.290	0.283	0.303	0.286	0.297	0.274	0.291	-	-	0.306
	720	0.418	0.405	0.415	0.400	0.405	0.397	0.373	0.354	0.373	0.354	0.337	0.340	-	-	0.350
Global Temp	96	0.275	0.290	0.270	0.300	0.256	0.288	0.275	0.286	0.287	0.281	0.264	0.273	-	-	0.292
	192	0.211	0.343	0.210	0.342	0.214	0.345	0.227	0.354	0.224	0.351	0.225	0.375	0.363	0.472	0.234
	336	0.281	0.405	0.267	0.395	0.269	0.396	0.269	0.396	0.266	0.394	0.267	0.395	0.313	0.423	0.387
	720	0.354	0.465	0.299	0.420	0.288	0.421	0.292	0.419	0.296	0.420	0.291	0.417	0.362	0.460	0.430
Average	96	0.336	0.384	0.336	0.380	0.322	0.372	0.349	0.377	0.347	0.370	0.359	0.373	0.396	0.413	0.461
	192	0.358	0.405	0.358	0.405	0.358	0.405	0.358	0.405	0.358	0.405	0.358	0.405	0.358	0.405	0.358
	336	0.384	0.405	0.384	0.405	0.384	0.405	0.384	0.405	0.384	0.405	0.384	0.405	0.384	0.405	0.384
	720	0.405	0.405	0.405	0.405	0.405	0.405	0.405	0.405	0.405	0.405	0.405	0.405	0.405	0.405	0.405
1 <sup>st</sup> Count	3	10	28	2	11	10	1	4	0	0	0	0	0	0	0	1



Performance overview. (Left) Comparison between Time-MoE models and SOAT TSFMs, reporting the average zero-shot performance across six datasets; (Right) Comparison of few- and zero-shot performance between Time-MoE and dense variants, with similar effective FLOPs per token, across the same six benchmarks.

Our models were pre-trained using **Time-300B** and has **three versions**: Base (113M), Large (453M), and Ultra (2.4B)

	Energy	Finance	Healthcare	Nature	Sales	Synthetic	Transport	Web	Other	Total
# Params	2,875,335	1,715	1,752	31,621,183	110,210	11,968,625	622,414	972,158	40,265	48,220,929
# Obs	15,981 B	413,696 K	471,040 K	26,382 M	279,724 B	9,222 B	2,130 B	20,332 M	309,09 B	
Percent %	5.17 %	0.0001 %	0.0001 %	90.50 %	0.008 %	2.98 %	0.69 %	1.804 B	0.006 %	100 %

## ⑤ In-domain Forecasting

**In-domain forecasting results.** All results are from four different forecasting horizons:  $H \in \{96, 192, 336, 720\}$ ; **Red**: the best, **Blue**: the 2<sup>nd</sup> best

Models	TIME-MoE (Ours)						Full-shot Time Series Models																
	TIME-MoE <sub>base</sub>	TIME-MoE <sub>large</sub>	TIME-MoE <sub>ultra</sub>	Transformer	TimeMixer	TimeSnet	PatchTST	Crossformer	TIDE	DLinear	FEDformer	TIME-MoE <sub>base</sub>	TIME-MoE <sub>large</sub>	TIME-MoE <sub>ultra</sub>	Transformer	TimeMixer	TimeSnet	PatchTST	Crossformer	TIDE	DLinear	FEDformer	
ETTh1	96	0.345	0.373	0.335	0.371	0.323	0.365	0.386	0.405	0.375	0.400	0.384	0.402	0.414	0.419	0.423	0.448	0.479	0.464	0.386	0.400	0.376	0.411
	192	0.372	0.396	0.374	0.400	0.359	0.391	0.441	0.436	0.436	0.429	0.421	0.429	0.460	0.445	0.471	0.474	0.525	0.492	0.437	0.432	0.420	0.461
	336	0.389	0.412	0.390	0.412	0.388	0.418	0.487	0.458	0.484	0.458	0.491	0.469	0.501	0.466	0.570	0.546	0.565	0.515	0.481	0.459	0.449	0.485
	720	0.410	0.443	0.402	0.433	0.425	0.450	0.503	0.491	0.498	0.482	0.521	0.500	0.488	0.653	0.621	0.603	0.570	0.545	0.451	0.440	0.455	0.480
	Avg.	0.379	0.401	0.375	0.404	0.373	0.406	0.454	0.447	0.448	0.442	0.454	0.450	0.468	0.544	0.529	0.522	0.540	0.507	0.455	0.451	0.440	0.455
ETTh2	96	0.276	0.340	0.278	0.335	0.274	0.338	0.297	0.349	0.289	0.341	0.304	0.374	0.302	0.348	0.745	0.584	0.600	0.440	0.333	0.387	0.358	0.435
	192	0.331	0.371	0.345	0.373	0.330	0.370	0.380	0.400	0.372	0.392	0.404	0.414	0.388	0.400	0.877	0.656	0.528	0.509	0.477	0.476	0.479	0.478
	336	0.373	0.402	0.384	0.402	0.362	0.396	0.428	0.432	0.386	0.414	0.452	0.451	0.426	0.433	1.043	0.731	0.643	0.571	0.594	0.541	0.496	0.485
	720	0.440	0.431	0.437	0.437	0.430	0.416	0.427	0.445	0.441	0.434	0.462	0.657	0.431	0.446	1.104	0.763	0.874	0.679	0.831	0.657	0.643	0.651
	Avg.	0.346	0.386	0.361	0.386	0.334	0.380	0.383	0.406	0.364	0.395	0.414	0.496	0.386	0.406	0.942	0.683	0.611	0.519	0.558	0.515	0.436	0.444
ETTm1	96	0.286	0.334	0.264	0.325	0.256	0.323	0.334	0.368	0.320	0.357	0.338	0.375	0.329	0.367	0.404	0.426	0.364	0.387	0.345	0.372	0.379	0.413
	192	0.307	0.358	0.295	0.350	0.281	0.343	0.377	0.391	0.361	0.381	0.374	0.387	0.363	0.450	0.511	0.500	0.404	0.380	0.389	0.506	0.464	0.464
	336	0.354	0.390	0.323	0.376	0.326	0.374	0.426	0.420	0.390	0.404	0.410	0.411	0.399	0.410	0.532	0.515	0.428	0.425	0.413	0.413	0.445	0.445
	720	0.433	0.445	0.409	0.435	0.454	0.452	0.491	0.459	0.454	0.441	0.478	0.450	0.454	0.439	0.666	0.589	0.487	0.461	0.474	0.454	0.543	0.543
	Avg.	0.345	0.381	0.322	0.371	0.329	0.373	0.407	0.409	0.381	0.395	0.400	0.405	0.387	0.400	0.513	0.495	0.419	0.419	0.403	0.406	0.448	0.448
ETTm2	96	0.172	0.265	0.169	0.259	0.183	0.273	0.180	0.267	0.175	0.258	0.187	0.267	0.175	0.259	0.287	0.366	0.207	0.305	0.193	0.292	0.203	0.285
	192	0.228	0.306	0.223	0.298	0.223	0.301	0.250	0.309	0.237	0.299	0.249	0.301	0.241	0.302	0.414	0.492	0.290	0.364	0.284	0.362	0.269	0.372
	336	0.281	0.345	0.282	0.343	0.278	0.339	0.311	0.348	0.288	0.340	0.321	0.351	0.306	0.343	0.597	0.542	0.422	0.462	0.389	0.427	0.325	0.425
	720	0.403	0.424	0.451	0.453	0.452	0.424	0.412	0.407	0.391	0.396	0.403	0.403	0.402	0.400	1.730	1.042	0.558	0.540	0.525	0.522	0.421	0.441
	Avg.	0.271	0.335	0.284	0.332	0.277	0.334	0.288	0.332	0.275	0.323	0.291	0.332	0.280	0.326	0.757	0.610	0.358	0.405	0.350	0.400	0.304	0.334
Weather	96	0.151	0.203	0.149	0.201	0.154	0.208	0.174	0.214	0.163	0.209	0.172	0.220	0.177	0.218	0.158	0.230	0.202	0.261	0.196	0.225	0.217	0.271
	192	0.195	0.246	0.192	0.244	0.192	0.251	0.221	0.254	0.208	0.250	0.219	0.261	0.225	0.259	0.236	0.277	0.242	0.298	0.237	0.239	0.276	0.313
	336	0.247	0.288	0.248	0.288	0.252	0.287	0.278	0.296	0.251	0.287	0.280	0.296	0.278	0.297	0.272	0.335	0.287	0.333	0.283	0.335	0.296	0.378
	720	0.352	0.366	0.352	0.365	0.392	0.376	0.358	0.349	0.339	0.341	0.365	0.359	0.355	0.348	0.988	0.418	0.551	0.386	0.345	0.381	0.414	0.414
	Avg.	0.236	0.275	0.236	0.275	0.237	0.275	0.237	0.275	0.237	0.275	0.237	0.275	0.237	0.275	0.427	0.300	0.362	0.265	0.251	0.254	0.261	0.304
Global Temp	96	0.192	0.238	0.192	0.239	0.189	0.322	0.223	0.251	0.215	0.246	0.250	0.381	0.219	0.349	0.272	0.406	0.223	0.352	0.221	0.354	0.261	0.375
	192	0.238	0.275	0.236	0.275	0.234	0.376	0.242	0.304	0.266	0.393	0.298	0.414	0.269	0.395	0.305	0.435	0.278	0.401	0.257	0.388	0.299	0.472
	336	0.259	0.397	0.256	0.397	0.253	0.399	0.313	0.431	0.313	0.430	0.315	0.434	0.319	0.435	0.352	0.468	0.320	0.404	0.294	0.418	0.341	0.455
	720	0.345	0.465	0.322	0.451	0.292	0.426	0.393	0.488	0.468	0.536	0.407	0.497	0.452	0.526	0.508	0.562	0.485	0.544	0.380	0.479	0.399	0.476
	Avg.	0.258	0.391	0.251	0.388	0.242	0.380	0.305	0.419	0.316	0.426	0.318	0.433	0.315	0.426	0.359	0.448	0.329	0.434	0.288	0.410	0.315	0.435
Average	0.306	0.362	0.304	0.359	0.301	0.358	0.349	0.382	0.337	0.375	0.356	0.400	0.349	0.382	0.560	0.516	0.421	0.439	0.387	0.416	0.375	0.401	
1st Count	4	2	4	21	33	40	2	4	2	40	2	4	2	40	2	4	2	4	2	4	2	4	2