





# Outlier Synthesis via Hamiltonian Monte Carlo for Out-of-Distribution Detection

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#### Introduction

- Task: fine-tuning based out-of-distribution (OOD) detection without access to auxiliary OOD dataset
- Outlier synthesis: synthesize virtual outliers which serve as surrogated OOD supervision signals
- Results: our proposed framework HamOS synthesizes high quality outliers and outperforms previous baselines

#### Motivation

- Pixel space outlier synthesis
  - E.g., Dream-OOD [1]
  - To generate pixel space outliers through the generative models, e.g., diffusion model.
- Feature space outlier synthesis
  - E.g., VOS [2], NPOS [3]
  - To generate outliers in the feature space through sampling algorithms,
     e.g. Gaussian.

- [1] Du, et al. Dream the impossible: Outlier imagination with diffusion models. In NIPS, 2023.
- [2] Du, et al. Vos: Learning what you don't know by virtual outlier synthesis. In ICLR, 2022.
- [3] Tao, et al. Non-parametric outlier synthesis. In ICLR, 2023.

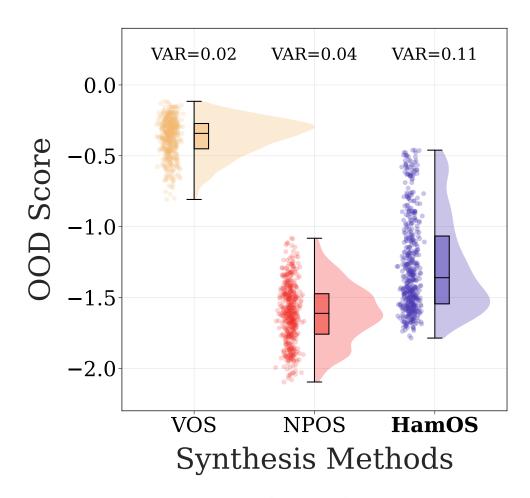
#### Motivation

#### Our goal

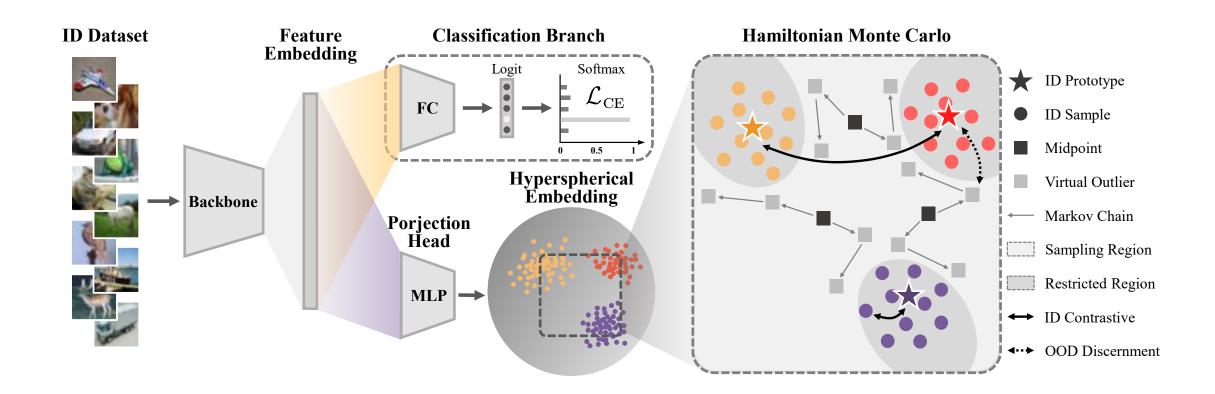
 To efficiently synthesize diverse and representative outliers based solely on the ID data

#### Idea

 Modeling the synthesis process as Markov chain



OOD score distributions



- Synthesizing Outliers via Hamiltonian Monte Carlo (HMC)
  - Estimating OOD density via the distance to the k-th nearest neighbor: we design a quantitative characterizing of the likelihood that a sample is OOD rather than ID.

$$egin{aligned} P^{ ext{OOD}}(oldsymbol{z}; oldsymbol{\mathcal{Z}}_{c}) &= \|oldsymbol{z} - oldsymbol{z}_{c(k)}\|_{2} & P^{ ext{OOD}}(oldsymbol{z}; oldsymbol{\mathcal{Z}}_{u}, oldsymbol{\mathcal{Z}}_{v}) = rac{P^{ ext{OOD}}(oldsymbol{z}; oldsymbol{\mathcal{Z}}_{u}) + P^{ ext{OOD}}(oldsymbol{z}; oldsymbol{\mathcal{Z}}_{v})}{2} \ U^{ ext{OOD}}(oldsymbol{z}; oldsymbol{\mathcal{Z}}_{u}, oldsymbol{\mathcal{Z}}_{v}) = -\log \sum_{i=u,v} P^{ ext{OOD}}(oldsymbol{z}; oldsymbol{\mathcal{Z}}_{i}) + ext{constant} \end{aligned}$$

• Synthesizing outliers by OOD density estimation via HMC: we generate virtual outliers along the Markov chains by solving the Hamilton's Equation.

$$H(oldsymbol{z},oldsymbol{q}) = U^{ ext{OOD}}(oldsymbol{z}) + rac{1}{2} \|oldsymbol{q}\|_2^2$$

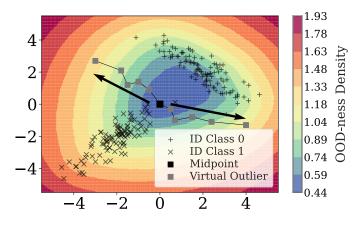
Rejecting erroneous outliers located within ID clusters: we reject false outliers that
conflate with ID embeddings by applying a hard margin according to the ID
probability.

$$egin{aligned} t_- = -\log \max_c P_c^{ ext{ID}}(\mathbf{b}_{u,v}) - \delta \quad \mathbf{b}_{u,v} = rac{oldsymbol{\mu}_u + oldsymbol{\mu}_v}{\|oldsymbol{\mu}_u + oldsymbol{\mu}_v\|_2} \end{aligned}$$

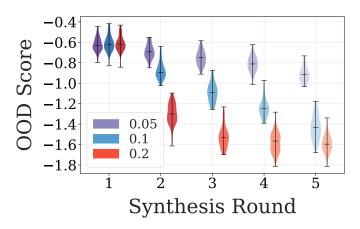
- Training with Synthesized Outliers
  - We fine-tune the model with the OOD discernment loss, the contrastive loss, and the cross-entropy loss to help broaden the gap between ID and OOD data.

$$\mathcal{L}_{ ext{OOD-disc}} = rac{1}{M} \sum_{i=1}^{M} rac{1}{C} \sum_{j=1}^{C} \log rac{\exp{(oldsymbol{z}_i^ op oldsymbol{\mu}_j/ au)}}{\sum_{l=1}^{C} \exp{(oldsymbol{z}_i^ op oldsymbol{\mu}_l/ au)}}$$

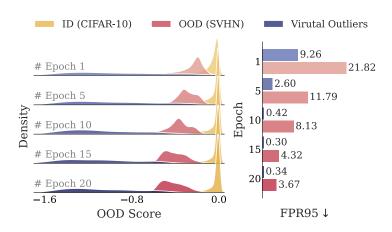
$$\mathcal{L}_{ ext{HamOS}} = \mathcal{L}_{ ext{CE}} + \mathcal{L}_{ ext{ID-con}} + \lambda_d \mathcal{L}_{ ext{OOD-disc}}$$



Depiction of the designed OODness density estimation.



Varied OOD scores of the generated outliers at different synthesis rounds.



OOD performance is improved continuously along the training process.

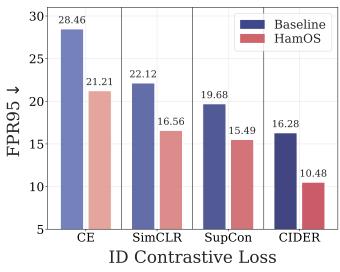
## Results

#### Main results: CIFAR10/100 benchmarks

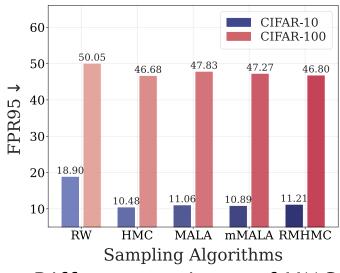
Methods	CIFAR-10				CIFAR-100			
	FPR95↓	AUROC↑	AUPR↑	ID-ACC↑	FPR95↓	AUROC↑	AUPR↑	ID-ACC↑
Post-hoc Methods								
MSP ODIN EBO KNN ASH Scale Relation	$\begin{array}{c c} 32.17_{\pm 6.38} \\ 58.04_{\pm 18.46} \\ 41.85_{\pm 13.78} \\ 22.86_{\pm 1.12} \\ 54.22_{\pm 26.06} \\ 63.18_{\pm 23.64} \\ 26.28_{\pm 1.63} \end{array}$	$\begin{array}{c} 91.10_{\pm 0.71} \\ 85.70_{\pm 4.17} \\ 91.79_{\pm 1.54} \\ 92.98_{\pm 0.42} \\ 87.37_{\pm 6.60} \\ 77.74_{\pm 16.24} \\ 92.31_{\pm 0.43} \end{array}$	$\begin{array}{c} 81.70_{\pm 5.82} \\ 70.08_{\pm 11.84} \\ 79.70_{\pm 8.10} \\ 88.74_{\pm 0.79} \\ 72.33_{\pm 16.40} \\ 63.03_{\pm 20.52} \\ 86.75_{\pm 0.98} \end{array}$	$\begin{array}{c} 95.17_{\pm 0.16} \\ 95.17_{\pm 0.16} \\ 95.17_{\pm 0.16} \\ 95.17_{\pm 0.16} \\ 95.10_{\pm 0.14} \\ 95.15_{\pm 0.16} \\ 95.17_{\pm 0.16} \end{array}$	$\begin{array}{c c} 59.78 \pm 2.16 \\ 63.49 \pm 2.51 \\ 60.86 \pm 1.87 \\ 56.96 \pm 2.96 \\ 66.84 \pm 0.87 \\ 69.27 \pm 2.31 \\ 59.64 \pm 2.48 \end{array}$	$77.25_{\pm 1.28} \\78.01_{\pm 1.62} \\78.32_{\pm 1.31} \\81.01_{\pm 1.19} \\77.14_{\pm 1.12} \\77.25_{\pm 1.01} \\79.69_{\pm 1.08}$	$\begin{array}{c} 66.86_{\pm 1.58} \\ 65.20_{\pm 2.19} \\ 66.73_{\pm 1.35} \\ 70.60_{\pm 2.29} \\ 62.24_{\pm 0.73} \\ 61.42_{\pm 1.42} \\ 68.76_{\pm 1.78} \end{array}$	$76.69_{\pm 0.24} \\76.69_{\pm 0.25} \\76.69_{\pm 0.24} \\76.69_{\pm 0.24} \\76.20_{\pm 0.23} \\76.69_{\pm 0.24} \\76.69_{\pm 0.24}$
Regularization-based Methods								
CSI SSD+ KNN+ VOS CIDER NPOS PALM HamOS(ours)	$\begin{array}{c c} 21.21_{\pm 1.68} \\ 18.49_{\pm 1.20} \\ 19.68_{\pm 1.86} \\ 42.37_{\pm 21.13} \\ 16.28_{\pm 0.68} \\ 14.39_{\pm 0.87} \\ 32.25_{\pm 4.14} \\ \textbf{10.48}_{\pm 0.76} \end{array}$	$\begin{array}{c} 93.73_{\pm 0.33} \\ 94.85_{\pm 0.57} \\ 94.41_{\pm 0.66} \\ 91.42_{\pm 3.38} \\ 95.76_{\pm 0.37} \\ 96.61_{\pm 0.26} \\ 90.54_{\pm 1.46} \\ \textbf{97.11}_{\pm 0.26} \end{array}$	$\begin{array}{c} 89.74_{\pm 0.68} \\ 90.88_{\pm 0.83} \\ 90.46_{\pm 0.66} \\ 79.16_{\pm 11.62} \\ 92.36_{\pm 0.06} \\ 93.35_{\pm 0.74} \\ 84.44_{\pm 2.14} \\ 94.94_{\pm 0.86} \end{array}$	$\begin{array}{c} 92.03_{\pm 0.72} \\ 93.95_{\pm 0.57} \\ 93.79_{\pm 0.63} \\ 95.05_{\pm 0.05} \\ 93.98_{\pm 0.16} \\ 93.95_{\pm 0.13} \\ 93.93_{\pm 0.98} \\ 94.67_{\pm 0.15} \end{array}$	$\begin{array}{c} 69.34_{\pm 0.86} \\ 54.03_{\pm 1.92} \\ 61.25_{\pm 0.81} \\ 58.55_{\pm 1.53} \\ 49.64_{\pm 1.80} \\ 51.41_{\pm 1.88} \\ 55.13_{\pm 0.97} \\ \textbf{46.68}_{\pm 1.44} \end{array}$	$\begin{array}{c} 73.46_{\pm 0.37} \\ 80.64_{\pm 0.60} \\ 78.24_{\pm 0.93} \\ 81.40_{\pm 0.62} \\ 81.77_{\pm 0.95} \\ 81.02_{\pm 0.98} \\ 79.95_{\pm 1.26} \\ \textbf{83.64}_{\pm 0.64} \end{array}$	$\begin{array}{c} 61.57_{\pm 0.75} \\ 69.73_{\pm 1.09} \\ 66.64_{\pm 0.88} \\ 68.33_{\pm 1.61} \\ 73.22_{\pm 1.12} \\ 72.49_{\pm 1.54} \\ 70.21_{\pm 1.38} \\ \textbf{75.52}_{\pm 1.30} \end{array}$	$\begin{array}{c} 61.75_{\pm 0.15} \\ 75.63_{\pm 0.39} \\ 72.18_{\pm 0.58} \\ 74.71_{\pm 0.07} \\ 75.09_{\pm 0.49} \\ 74.53_{\pm 0.62} \\ 74.67_{\pm 0.36} \\ 76.12_{\pm 0.14} \end{array}$

#### Results

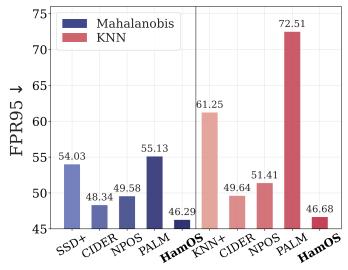
#### Ablation study



Different contrastive loss



Different variants of HMC

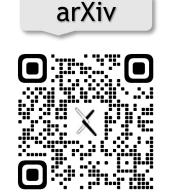


Different scoring functions

#### Conclusion

 We propose a novel framework HamOS to synthesize virtual outliers for OOD detection

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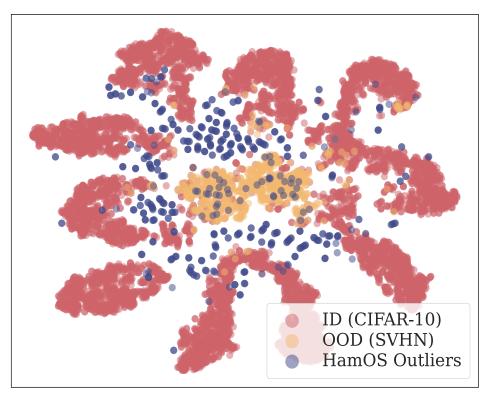






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Feature visualization via t-SNE