

Physics of Language Models: Part 3.3

Knowledge Capacity **Scaling Laws**

Result 1/2/3/5

a *universal* law: “all” LLMs can store 2bit/param knowledge
⇒ predict: 7B model can store all English wiki + textbooks knowledge

Result 4/6/7

scaling laws for insufficient training
e.g. LLaMA/Mistral architectures *30% worse* than GPT2_{rotary} in capacity

Result 8/9

scaling laws for quantization + mixture-of-expert (MoE)
e.g. 2bit/param holds *even for* int8 parameters

Result 10/11/12

scaling laws for mixed-quality data (wikipedia vs internet)
e.g. a technique to improve LLM’s capacity – sometimes by 10x

calculate amount of learned knowledge (in *bits*)



a universal scaling law

supported by a *lower-bound Theorem*

pretrain LLMs (varied sizes)

LLMs can “consistently” achieve 2bit/param in storing knowledge after sufficient training

varying N and hyperparameters (K,T,C,L,D)

for a wide range of model sizes / depths / widths

synthetic English data describing knowledge tuples

e.g. (Anya Forger, birthday, 10/2/1996)
(USA, capital, Washington D.C.)

e.g. only size matters

– Result 1

bioS: N human biographies from templates

bioR: N human biographies generated by LLaMA2

bioD: a synthetic data with hyperparameters:

K – number of knowledge attributes

T – vocabulary size

C,L – values in C chunks, each of length L

D – value has diversity D

regardless of data types (bioS/bioR/bioD)

– Result 2

e.g. rewriting pretrain data 40x times
does not need bigger model

for a wide range of hyperparameters (K/T/C/L/D)

– Result 3



predict: a 7B model can store all English wiki + textbooks knowledge if sufficiently trained

** by “storage” we do not mean word-by-word memorization; we mean “generalizable” knowledge: those flexibly extractable for all fine-tune tasks*

scaling law (sufficient training)

“all” LLMs consistently achieve *2bit/param* in storing knowledge that are seen for **1000 exposures**

– Result 5

1000 exposures \neq 1000 passes

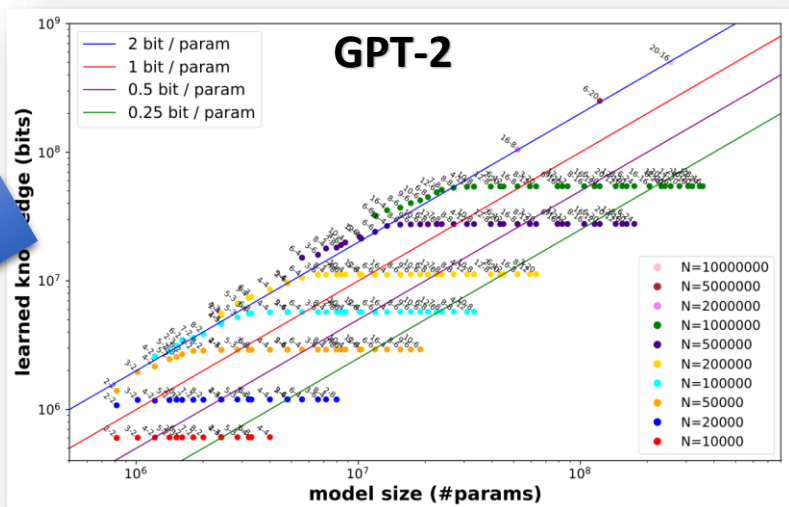
– e.g. (US, capital, Washington DC) has been exposed 1,000,000+ times in 1-pass of the internet pretrain data

scaling law (**insufficient** training)

GPT-2* consistently achieves *1bit/param* in storing knowledge that are seen for **100 exposures**

* adding rotary embedding

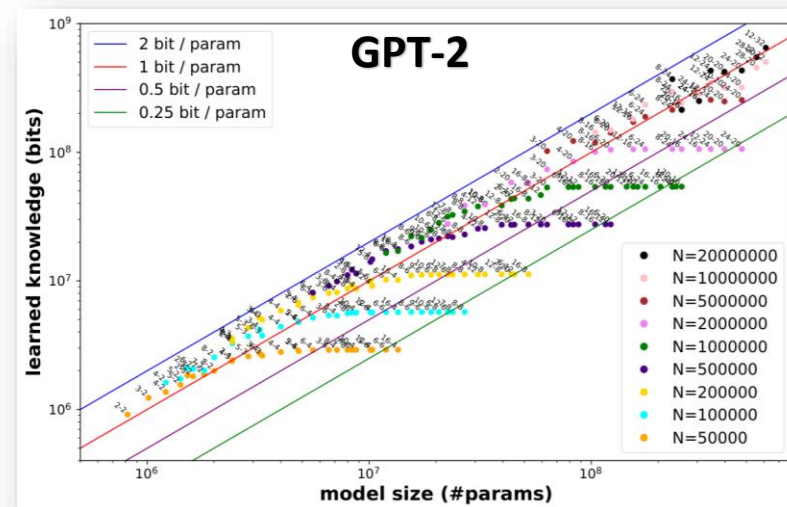
– Result 4



1000 \Rightarrow **100** exposures
(**insufficient** training)



ratio 2 \Rightarrow 1 bit/param



GO WORSE

if you use **LLaMA** or **Mistral**
even if you completely remove MLP layers!

Corollary: Attention layers can store knowledge

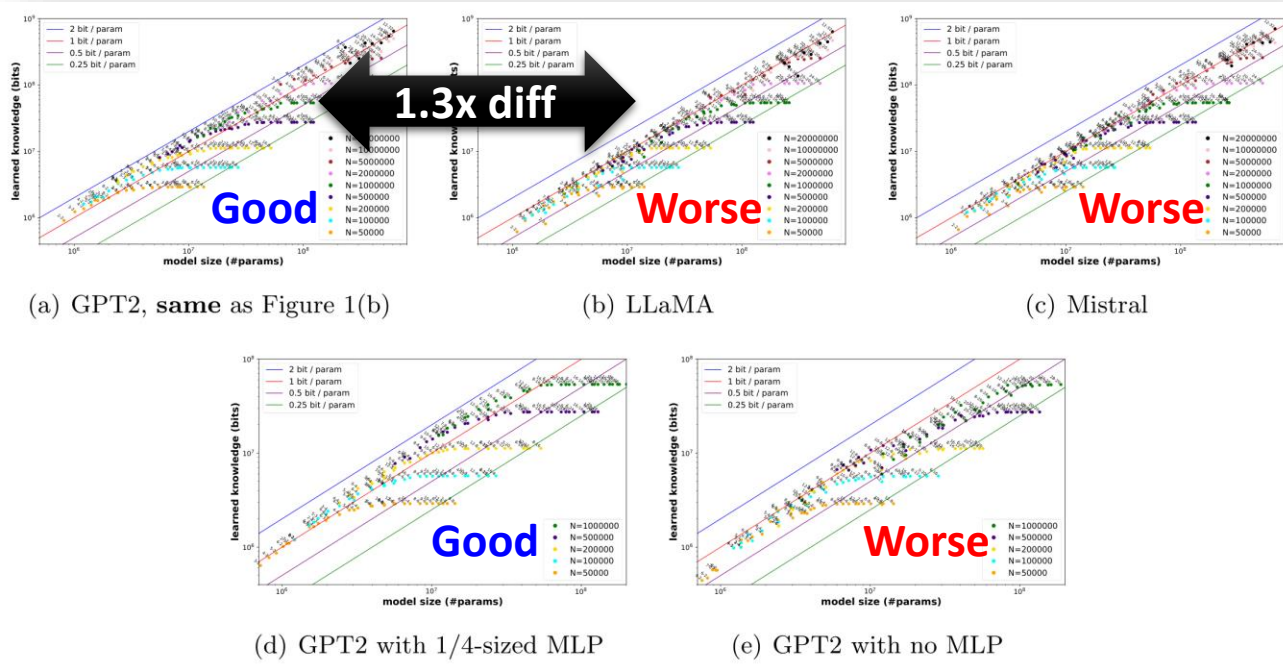
if you use **LLaMA/Mistral** architectures,
see Results 6+7

scaling law (insufficient training)

In the **100**-exposure setting, some architectures are worse in knowledge capacity: e.g., LLaMA/Mistral architectures can be **1.3x worse** than GPT2_{rotary}

– Result 6

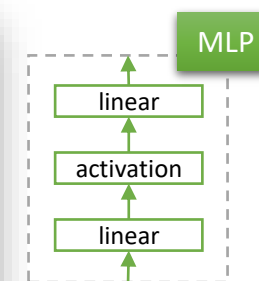
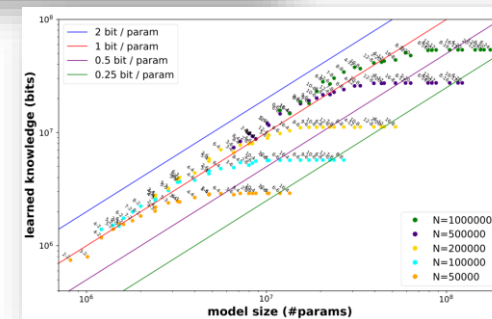
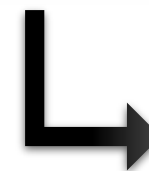
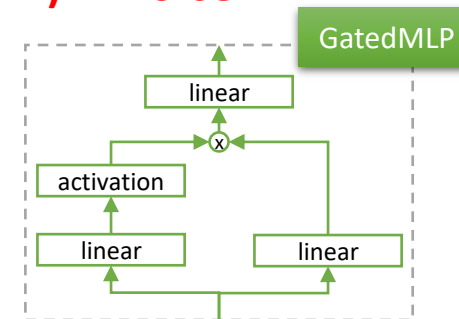
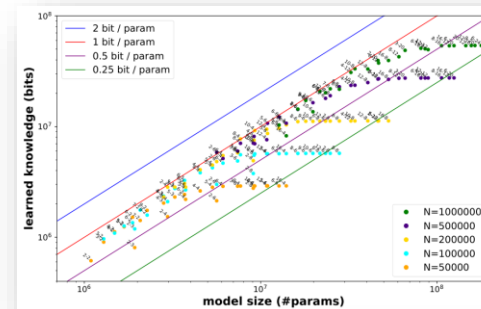
Controlled experiments reveal that **GatedMLP** contributes to this **performance loss**; it is less stable, needs longer training time – Result 7



Disclaimer 1: this comparison is for knowledge capacity only

Disclaimer 2: there will be **no difference** if sufficiently trained, see Result 5

LLaMA/Mistral (using GatedMLP) = Worse



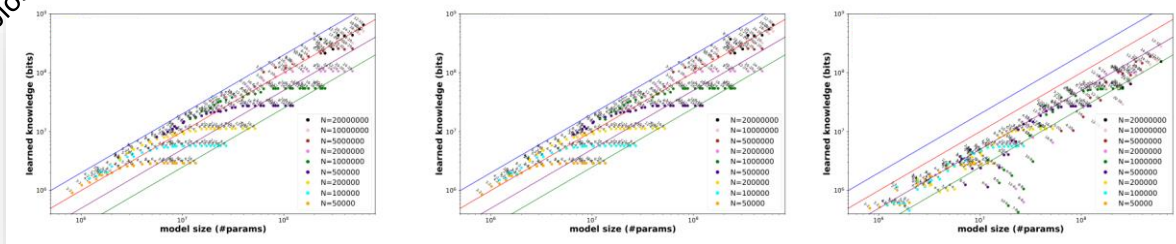
LLaMA (replaced with standard MLP) = Good

scaling law (quantization)

– Result 8

quantizing → int8 **does not affect** scaling laws **at all**
even for models at maximum capacity
 quantizing → int4 hurts capacity by more than 2x

bioS data



float16/32

1000101010101010
0100110101010111

no diff

int8

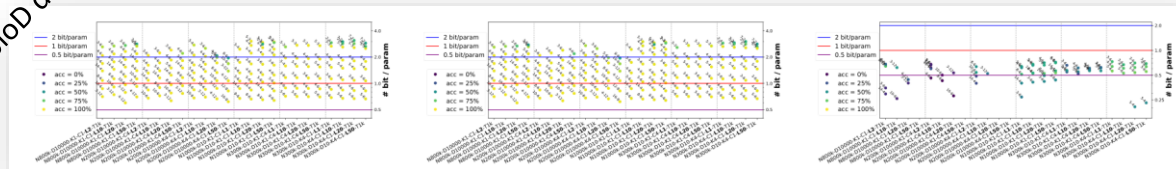
01111010

worsen >2x

int4

1101

bioD data

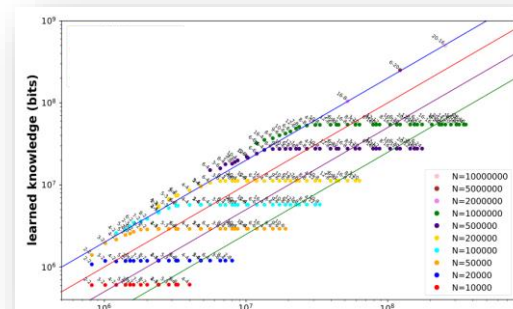


Conclusion: int8 quantization is a free lunch;
 to int4 or below requires training techniques

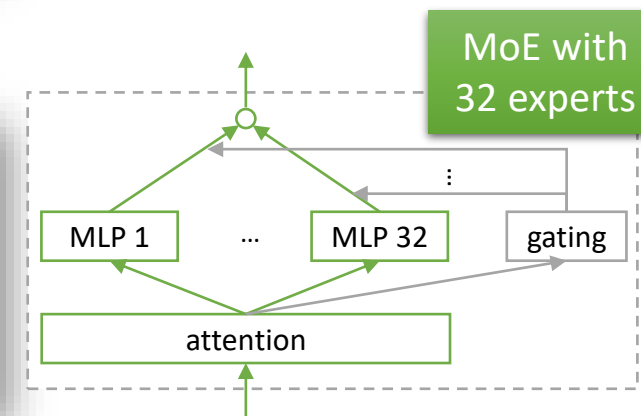
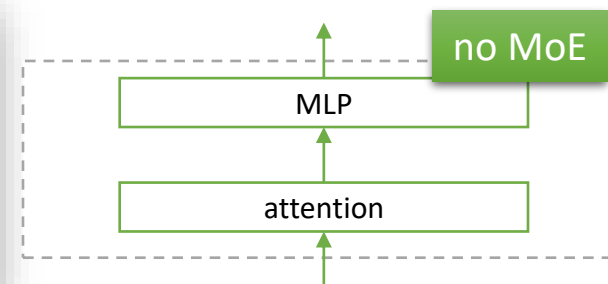
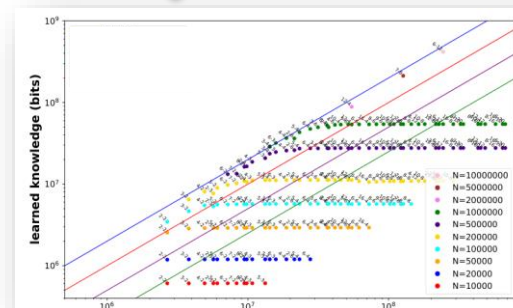
scaling law (MoE)

– Result 9

LLMs with **mixture of even 32 experts** can be very
 efficient in storing knowledge



only 1.3x worse



despite using 8.8% of total params during inference!

⇒ the 32 experts must have very “evenly” stored knowledge

scaling laws (pretrain data of mixed qualities)

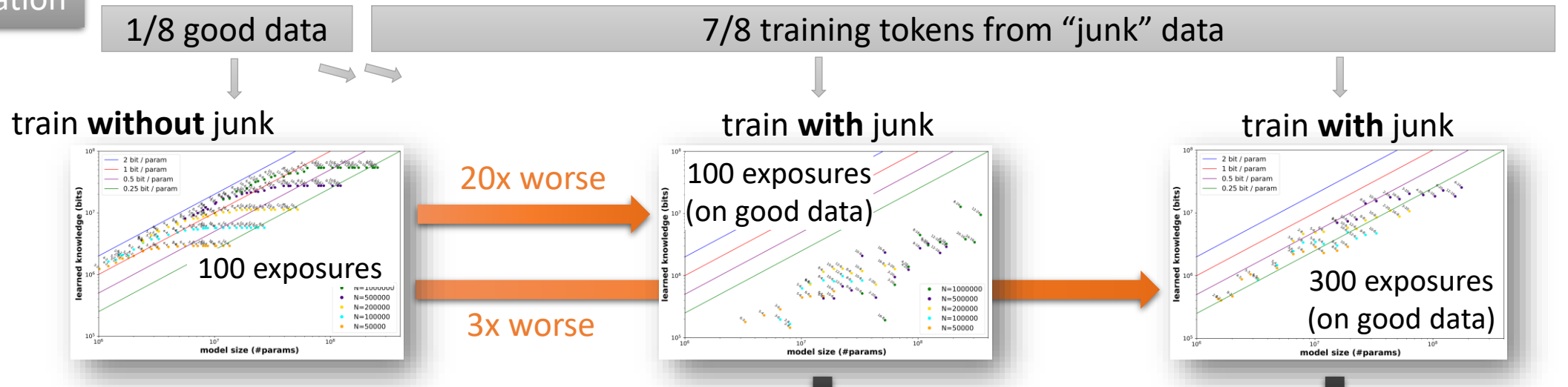
“Junk” data significantly **harm** LLM’s knowledge capacity on **good data** (sometimes by 20x times!)
e.g. common crawls, internet “junks” e.g. Wikipedia

– Result 10

repetitive knowledge ... *does not harm* ...

– Result 11

illustration



a simple fix!

add domain tokens (e.g., “wikipedia.org”) at front of all pretrain data paragraphs

LLMs can **automatically** detect domains rich in high-quality knowledge and prioritize learning from them

– Result 12