

# Exploring Learning Complexity for Efficient Downstream Dataset Pruning

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# Background

## Prohibitive Model Development Cost from Neural Scaling Laws

The paradigm of pre-training and fine-tuning (PT-FT) is increasingly popular with the rapid advancements in foundation models. Unfortunately,

- **Training costs are ever-increasing** due to the neural scaling laws

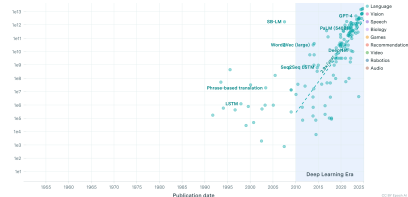
$$(N^{\text{opt}}, D^{\text{opt}}) = \operatorname{argmin}_{N, D} \mathcal{L}(N, D) \quad (1)$$

$$\text{s.t. } \text{FLOPs}(N, D) = C \quad (2)$$

, where  $N$  is the model parameter,  $D$  is the training dataset and  $C$  is computing power. We aim to allocate  $C$  between  $N$  and  $D$  optimally.

Notable AI Models

Training dataset size (words)

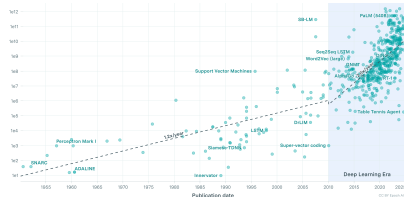


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Notable AI Models

Number of trainable parameters



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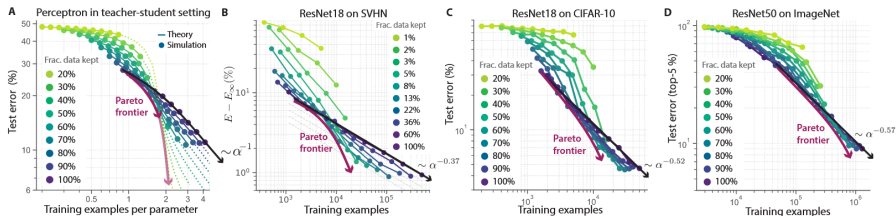
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# Background

## Beating Neural Scaling Laws via Dataset Pruning

From the perspective of dataset size, recent work [1] demonstrates that we can break beyond power laws and potentially even reduce it to exponential scaling instead if we have access to

- **A high-quality dataset pruning metric** that ranks the order in which training examples should be discarded to achieve any size.



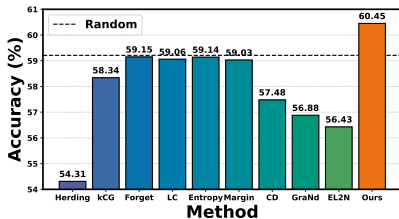
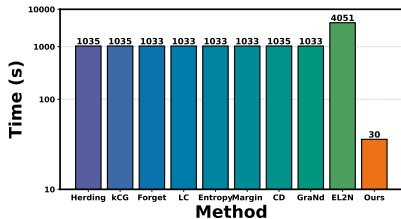
# Background

## Concerns of Efficiency and Efficacy

Existing dataset pruning methods propose diverse metrics to quantify the sample importance through a scoring function  $S(\mathbf{x})$ , which are generally designed for training from scratch.

When transferring to the PT-FT, we face the following challenges:

- **Inefficiency:** Fine-tuning the entire dataset for estimating  $S(\mathbf{x})$  can be prohibitively expensive due to the computationally intensive back-propagation on the huge parameters.
- **Ineffectiveness:** Existing methods empirically show inferior performance than the random on the diverse PT-FT benchmarks.



# Method

## DLC: Distorting-based Learning Complexity (I)

To design an efficient and effective  $S(\mathbf{x})$ , we first define the Learning Complexity from the hardness perspective based on:

### Learning Path

A sequence of model parameters  $\Theta = \{\theta(t) \mid t \in \mathcal{T}\}$  can be defined as a learning path if there exists a positive constant  $r < \mathcal{R}_{\mathcal{L}}(f_{\theta(0)})$  such that  $\lim_{t \rightarrow \infty} \mathcal{R}_{\mathcal{L}}(f_{\theta(t)}) = r$ .

, and the above Learning Complexity can be formally defined as follows:

### Learning Complexity

$$S_{\text{LC}}((\mathbf{x}, y)) = \int_{t \in \mathcal{T}} \mathcal{L}(f(\mathbf{x}; \theta(t)), y) dt$$

# Method

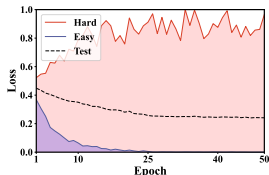
## DLC: Distorting-based Learning Complexity (II)

Existing optimization-based learning complexity quantifies the sample hardness from the perspective that:

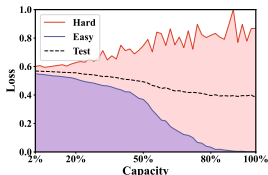
- Easy samples have larger  $\frac{d\mathcal{L}}{dC}$  than the hard as shown in Figure (a).

Instead, we implement the learning complexity with a lightweight distorting process for efficiency, by the observation that:

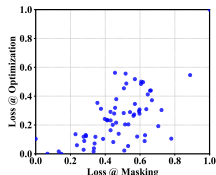
- Easy samples have larger  $\frac{d\mathcal{L}}{dN}$  than the hard as shown in Figure (b).



(a)



(b)



(c)

In Figure (c), the ranking of DLC is **highly correlated** with the learning complexity based on optimization.

# Method

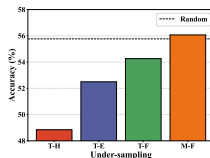
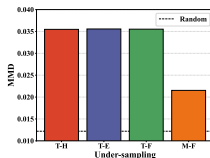
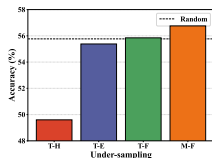
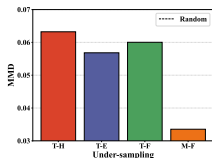
## FlexRand: Flexible Under-sampling with Randomness

To identify informative samples with DLC, we further design a flexible under-sampling strategy with randomness, named **FlexRand** as follows:

$$p((\mathbf{x}, y)) = \begin{cases} \frac{M}{2N*\gamma}, & \text{if } S_{LC}((\mathbf{x}, y)) < S_{\gamma} \\ \frac{M}{2N*(1-\gamma)}, & \text{if } S_{LC}((\mathbf{x}, y)) \geq S_{\gamma} \end{cases}$$

which offers two advantages

- **FlexRand can adapt to different data regimes.**
- **FlexRand avoids severe distribution shift.**



# Method

## Extension to Instruction Dataset Pruning

When extending the learning complexity to prune instruction datasets for efficient LLMs fine-tuning, we replace the original loss function with:

$$S_{LC}((\mathbf{x}, \mathbf{y})) = \frac{1}{C} \sum_{j=0}^{C-1} \mathcal{L}(f(y_{j-1} : \dots : y_0 : \mathbf{x}; \boldsymbol{\theta}(t)), y_j)$$

where  $C$  is the length of the output  $\mathbf{y}$ , due to the prediction difference in image classification and text generation. Empirical results are presented in the following table:

Base Model	Alpaca Cleaned				Dolly & HH-RLHF			
	Humanity	Social Science	STEM	Other	Humanity	Social Science	STEM	Other
Mistral 7B	52.44 / <b>54.75</b>	71.89 / <b>72.64</b>	51.74 / <b>52.74</b>	68.88 / <b>70.20</b>	52.50 / <b>53.82</b>	69.58 / <b>71.47</b>	51.18 / <b>53.30</b>	68.01 / <b>68.91</b>
Llama3 8B	54.24 / <b>56.75</b>	71.99 / <b>72.05</b>	52.33 / <b>54.84</b>	69.78 / <b>70.20</b>	52.52 / <b>53.94</b>	69.13 / <b>72.60</b>	49.92 / <b>53.60</b>	68.39 / <b>69.65</b>
Gemma2 9B	56.37 / <b>58.79</b>	73.29 / <b>75.25</b>	54.14 / <b>56.30</b>	71.13 / <b>71.52</b>	55.21 / <b>56.08</b>	71.43 / <b>73.32</b>	50.23 / <b>52.99</b>	69.51 / <b>70.60</b>

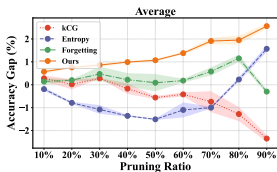
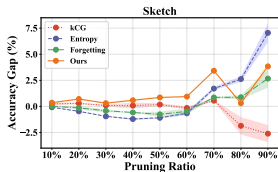
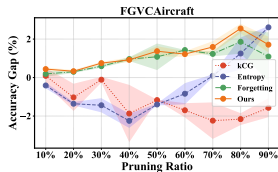
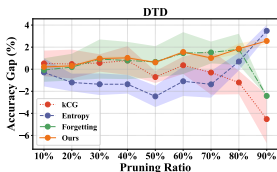
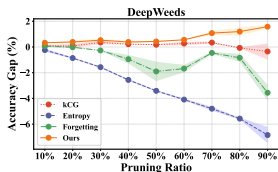
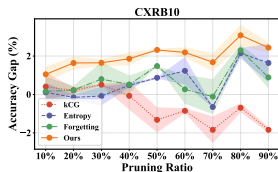
We can find that **our method consistently outperforms the random with various pre-trained models and instruction fine-tuning datasets.**

# Experiments

## Main Results

In the downstream image dataset pruning benchmark, the empirical results demonstrate that our method

- achieves superior accuracy with different architectures.
- consistently outperforms the random with diverse setups.
- significantly reduces the time cost of dataset pruning by 35x.

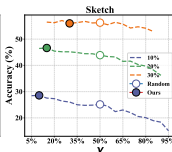
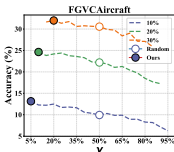
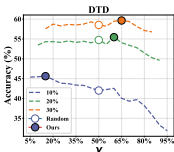
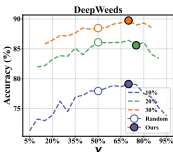
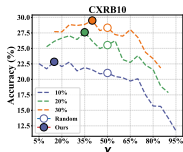
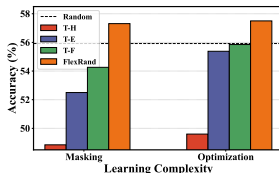
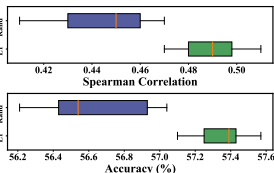
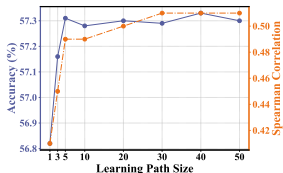


# Experiments

## Ablation Studies

To better understand why our method can obtain superior efficiency and efficacy, we perform extensive ablation studies on the

- **Learning path size**
- **Weight masking principle**
- **Under-sampling strategy**
- **Interval splitting**



# Discussions

## Relationship with the pre-trained models

### • Is the proposed method affected by the pre-training dataset?

Method	10%~30%					40%~60%					70%~90%					Average
	CXR	DW	DTD	FA	Sk	CXR	DW	DTD	FA	Sk	CXR	DW	DTD	FA	Sk	
Random	27.27	<u>87.42</u>	54.67	32.15	56.89	32.80	92.91	66.32	55.36	72.81	34.68	94.45	69.44	66.97	77.35	61.43
Herding	24.77	49.83	32.31	25.32	44.74	31.90	78.43	56.41	50.32	67.55	<u>36.28</u>	91.89	67.55	65.71	76.40	53.29
kCG	25.48	87.30	49.13	28.50	55.83	31.27	93.25	65.67	54.74	73.63	<u>35.30</u>	94.66	70.29	67.42	77.60	60.67
Forgetting	28.60	86.53	54.99	<b>35.94</b>	<b>58.75</b>	<u>34.17</u>	91.89	66.86	59.86	73.12	36.18	94.33	70.29	68.39	76.92	62.45
Least Conf	27.13	83.48	55.60	30.63	58.07	<u>32.93</u>	89.71	64.49	51.20	71.09	36.20	93.26	69.18	<u>64.24</u>	76.68	60.26
Entropy	28.42	82.95	55.52	31.09	<u>58.45</u>	32.88	89.93	64.41	51.28	71.23	35.72	93.55	68.86	64.27	76.80	60.36
Margin	28.12	83.20	55.80	30.52	58.43	33.92	89.85	64.21	50.59	71.35	36.52	93.41	68.63	64.30	76.61	60.36
CD	23.00	87.07	<u>52.97</u>	34.49	54.85	32.03	<u>94.13</u>	66.14	59.53	<b>73.73</b>	36.07	<b>95.11</b>	<u>70.52</u>	68.67	<b>78.20</b>	61.77
GraNd	21.77	86.40	53.43	<u>35.08</u>	54.24	30.70	<u>94.04</u>	66.02	60.38	73.38	36.03	94.85	<u>70.35</u>	<b>68.91</b>	<u>78.00</u>	61.57
EL2N	19.62	87.13	52.91	34.45	53.70	31.70	<b>94.31</b>	66.24	<b>60.94</b>	73.13	36.17	<u>95.08</u>	70.35	<b>68.91</b>	77.75	61.49
Ours	<b>29.69</b>	<b>88.49</b>	<b>57.45</b>	34.67	58.41	<b>34.79</b>	93.40	<b>67.12</b>	56.97	<u>73.65</u>	<b>37.42</b>	94.90	<b>70.66</b>	67.29	77.79	<b>62.85</b>

### • Can we use small models to select samples for large models?

$S((x, y))$	ResNet-50					ViT-Small					ViT-Base					Average
	CXR	DW	DTD	FA	Sk	CXR	DW	DTD	FA	Sk	CXR	DW	DTD	FA	Sk	
Random	31.73	<u>91.99</u>	67.44	46.75	63.63	33.13	92.60	66.56	48.02	66.27	31.88	<u>91.86</u>	64.81	44.94	64.10	60.38
Original	<b>32.90</b>	<b>92.50</b>	<b>68.29</b>	<b>47.61</b>	<b>64.48</b>	<u>34.12</u>	<b>92.99</b>	<u>67.29</u>	<b>48.41</b>	<b>66.93</b>	<u>32.63</u>	<b>92.17</b>	<b>65.26</b>	<b>45.63</b>	<b>65.06</b>	<b>61.08</b>
Transfer (RN18)	<u>31.61</u>	90.43	<u>68.03</u>	<u>46.78</u>	<u>63.98</u>	<b>34.71</b>	<u>92.93</u>	<b>67.45</b>	<u>48.37</u>	<u>66.69</u>	<b>32.94</b>	91.82	<u>65.12</u>	<u>44.99</u>	<u>64.61</u>	<u>60.70</u>

- **Contribution**

- We propose Distorted-based Learning Complexity (**DLC**), a novel and straightforward hardness score without relying on fine-tuning.
- We design the **FlexRand** under-sampling, which can adapt to different data regimes while avoiding severe distribution shifts.
- Comprehensive experiments verify the effectiveness and efficiency of the proposed method on comprehensive benchmarks.

- Learn More!

- Paper: <https://arxiv.org/pdf/2402.05356.pdf>



Ben Sorscher, Robert Geirhos, Shashank Shekhar, Surya Ganguli, and Ari S. Morcos.

Beyond neural scaling laws: beating power law scaling via data pruning.

In Alice H. Oh, Alekh Agarwal, Danielle Belgrave, and Kyunghyun Cho, editors, *Advances in Neural Information Processing Systems*, 2022.



Ziheng Qin, Kai Wang, Zangwei Zheng, Jianyang Gu, Xiangyu Peng, Daquan Zhou, and Yang You.

Infobatch: Lossless training speed up by unbiased dynamic data pruning.

*arXiv preprint arXiv:2303.04947*, 2023.



Max Welling.

Herding dynamical weights to learn.

In *International Conference on Machine Learning*, pages 1121–1128, 2009.



Ozan Sener and Silvio Savarese.

Active learning for convolutional neural networks: A core-set approach.

In *International Conference on Learning Representations*, 2018.



Sharat Agarwal, Himanshu Arora, Saket Anand, and Chetan Arora.

Contextual diversity for active learning.

In *European Conference on Computer Vision*, pages 137–153, 2020.



Gao Huang, Danlu Chen, Tianhong Li, Felix Wu, Laurens van der Maaten, and Kilian Q. Weinberger.

Multi-scale dense networks for resource efficient image classification.  
*In International Conference on Learning Representations, 2017.*



Ji Xin, Raphael Tang, Jaejun Lee, Yaoliang Yu, and Jimmy J. Lin.

Deebert: Dynamic early exiting for accelerating bert inference.  
*In Annual Meeting of the Association for Computational Linguistics, 2020.*