



# Theoretical Analysis of Contrastive Learning under Imbalanced Data: From Training Dynamics to a Pruning Solution

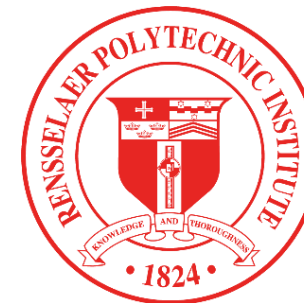
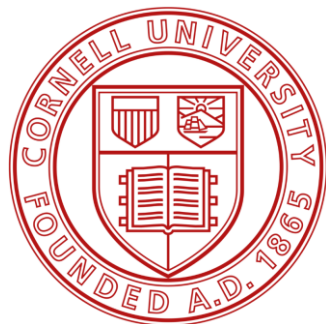
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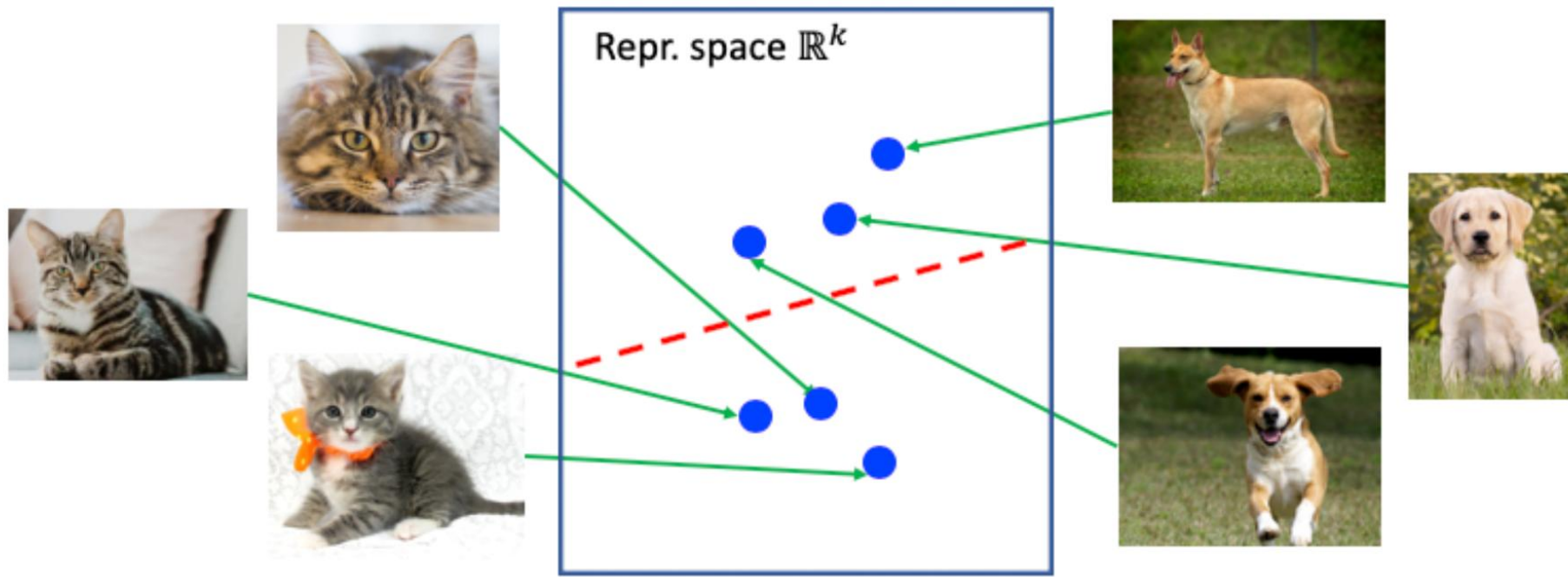
<sup>3</sup> University of Louisiana at Lafayette

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# Background: Contrastive Learning

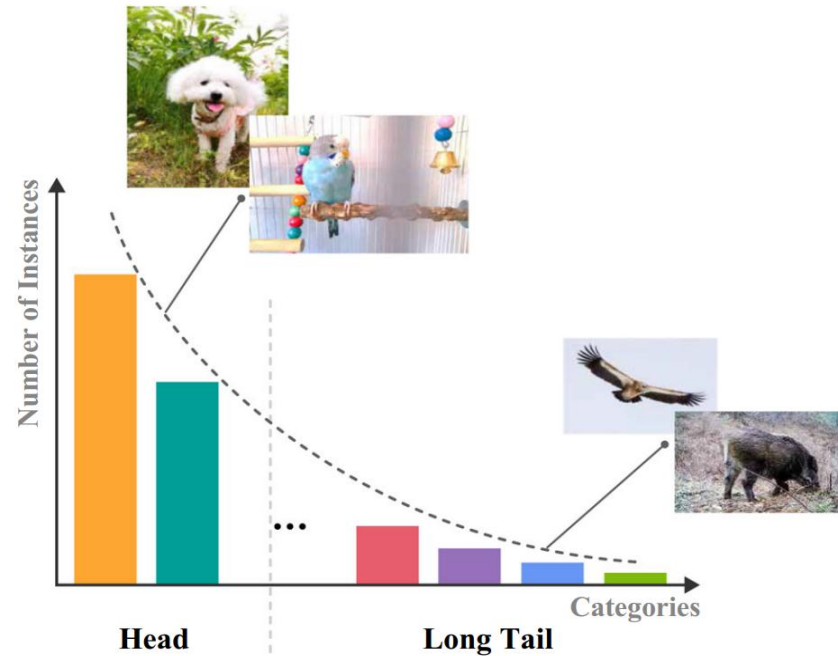
- Contrastive learning makes similar images closer together in the representation space



# Background: Imbalanced Data

Long-tailed datasets exist in many real-world scenarios

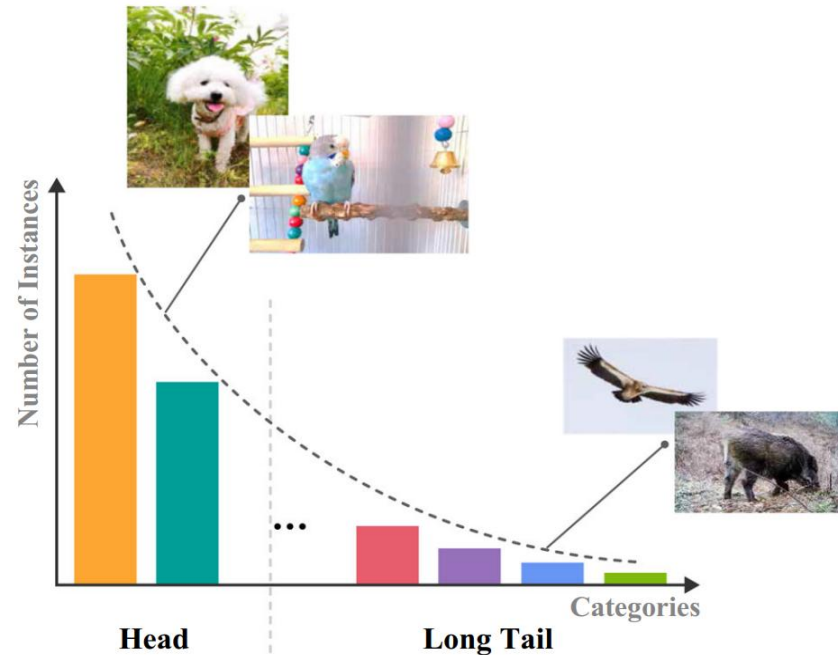
- Common classes: dog, budgie, and others
- Uncommon classes: eagle and many more



# Background: Imbalanced Data

Long-tailed datasets exist in many real-world scenarios

- Common classes: dog, budgie, and others
- Uncommon classes: eagle and many more



However, contrastive learning still struggles with class imbalance in real-world datasets

# Main contribution: Training Dynamics

Contribution 1: we build a theoretical framework to understand how contrastive learning behaves during training

- Stage 1: All neurons grow in feature directions but non-feature directions are ignored
- Stage 2: Lucky neurons then specialize in single features, and ordinary neurons learn a mix of features
- Stage 3: Each neuron becomes strongly aligned with one or more features, weakly aligned with other features, and remaining small in non-feature directions

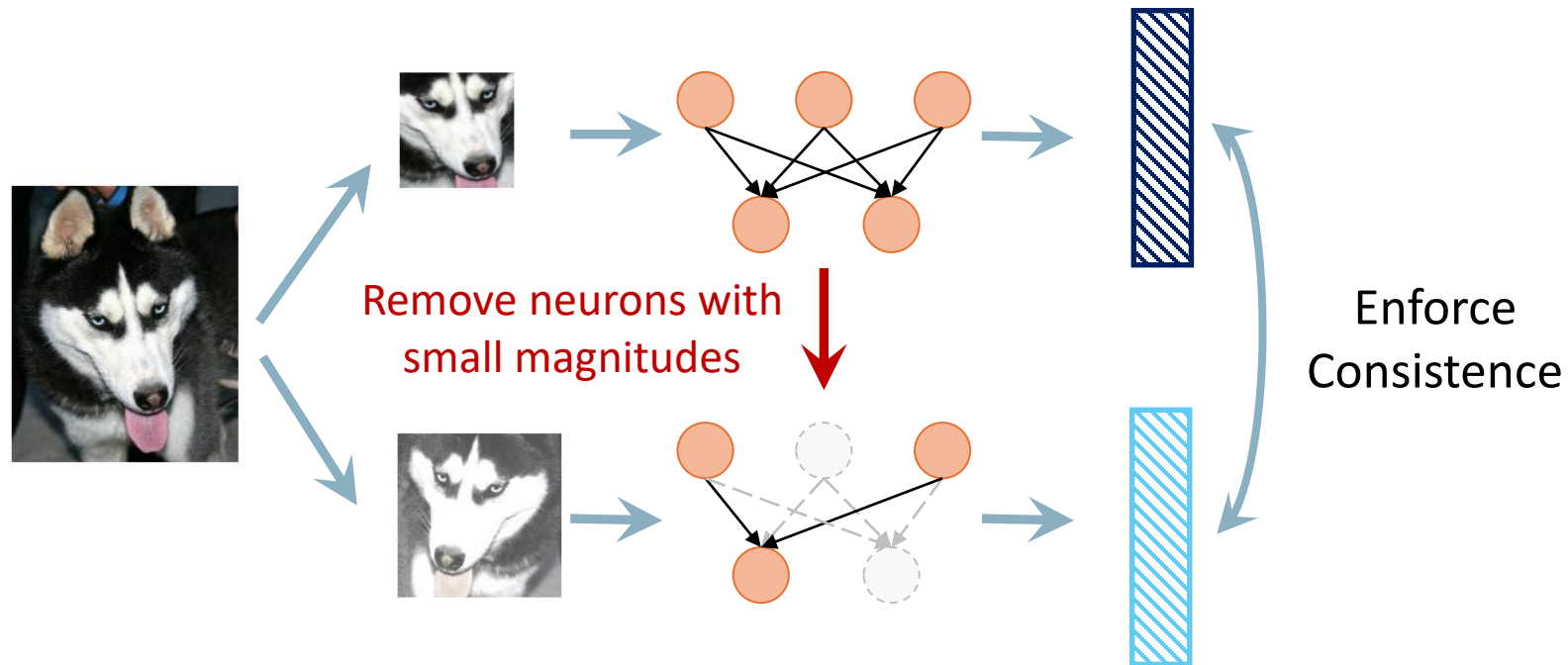
# Main contribution: Data Imbalance

Contribution 2: our analysis shows that data imbalance hurts the quality of representations in several ways

- Slower learning of minority features requires a longer time to converge
- Fewer neurons specializing in single features
- Higher model complexity needed to capture all features, which implies longer training time and more neurons

# Pruning Algorithm

- Dynamically removes small-magnitude neuron weights during the forward pass
- Keeps all parameters trainable during the backward pass



*Credit:*  
*Jiang et al., ICML 2021;*  
*Qian et al., NeurIPS 2022.*

# Main contribution: Pruning

Contribution 3: magnitude-based pruning can enhance the learning of minority features

- Enhanced neuron updates along minority-feature directions
- More neurons focusing on pure minority features
- More balanced and robust representations

# Numerical Result: Pruning

- Consistently improves accuracy across all datasets
- Narrows performance gap between head and tail classes

| Dataset     | $\rho$ | Accuracy         |                  | $\Delta_{20}$   |                 |
|-------------|--------|------------------|------------------|-----------------|-----------------|
|             |        | w/o pruning      | w/ pruning       | w/o pruning     | w/ pruning      |
| CIFAR10-LT  | 10     | 79.25 $\pm$ 1.03 | 84.92 $\pm$ 0.67 | 3.42 $\pm$ 1.02 | 2.99 $\pm$ 0.92 |
|             | 50     | 75.58 $\pm$ 0.84 | 83.60 $\pm$ 1.02 | 3.92 $\pm$ 1.21 | 3.35 $\pm$ 0.76 |
|             | 100    | 74.24 $\pm$ 0.82 | 81.31 $\pm$ 0.94 | 5.69 $\pm$ 1.35 | 5.62 $\pm$ 0.99 |
| CIFAR100-LT | 10     | 51.21 $\pm$ 1.21 | 56.33 $\pm$ 1.51 | 2.45 $\pm$ 0.57 | 1.37 $\pm$ 0.46 |
|             | 50     | 49.32 $\pm$ 0.45 | 56.12 $\pm$ 0.32 | 4.95 $\pm$ 1.02 | 2.57 $\pm$ 0.92 |
|             | 100    | 47.12 $\pm$ 0.51 | 54.93 $\pm$ 0.50 | 7.11 $\pm$ 0.45 | 4.38 $\pm$ 0.22 |
| ImageNet-LT | 256    | 63.21            | 65.12            | 8.47            | 7.21            |